

## TRANSIENT SOLUTION OF EQUATIONS OF HYDRODYNAMICS IN GAS CLOUDS

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### ABSTRACT

We have presented numerical results of transient phenomenon in incompressible fluids. This has been obtained by solving the equations of conservation of momentum, energy and mass in X and Y geometry. We have used the explicit techniques in solving the partial differential equations. Initially a non-steady state is assumed and it is found that one obtains a steady state solution after several time steps.

### 1. Introduction

When two gas clouds which are in motion, whether they are in stellar atmospheres or in interstellar space, collide, there will be exchange in energy between the two clouds and the ionization structure in the two clouds will get modified. This problem is an extremely complicated one because, one has to consider the transient hydrodynamic effects, so that one can predict the temperature and velocity changes which in turn, will allow us to determine the ionization structure of the mixture of the two clouds. There are several ways of obtaining numerical solution since an analytical approach fails to give any meaningful answer. We have made an attempt of obtaining a numerical solution of the problem of radial motion of gas flows in stellar atmospheres (Peraliah 1982). The problem requires a careful study of the evolution of the numerical solution. Various methods have been devised to suit the different kinds of physical situations. There are mainly two kinds of approaches eg. (1) explicit procedures and (2) implicit procedures in the discrete methods.

In this paper we shall consider explicit techniques for obtaining the numerical solution of the equations of continuity, momentum and energy.

### 2. Equations of motion and the method of obtaining solution

We shall consider a simple problem of fluids which are incompressible and we shall write the equations in dimensionless variables. Let T, U and V represent the dimensionless variables of temperature and velocity components in X and Y directions. Then we have (Hellums and Churchill 1962)

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \quad \text{Equation of continuity} \quad (1)$$

$$\frac{\partial T}{\partial \tau} + U \frac{\partial T}{\partial X} + V \frac{\partial T}{\partial Y} = \frac{1}{Pr} \frac{\partial^2 T}{\partial Y^2} \quad \text{Equation of energy} \quad (2)$$

and

$$\frac{\partial U}{\partial \tau} + U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = T + \frac{\partial^2 U}{\partial Y^2} \quad \text{Equation of momentum} \quad (3)$$

Here  $\tau$ , X and Y are dimensionless time and distance coordinates respectively and  $Pr$  is the Prandtl number.

We would like to solve the equations (1), (2) and (3) subject to the boundary conditions :

$$\begin{aligned}
 X=0 & : U=V=T=0 \\
 Y=0 & : U=V=0, T=1 \\
 Y=\infty & : U=V=T=0 \\
 \tau=0 & : U=V=T=0
 \end{aligned}
 \tag{4}$$

We should obtain the solution to the partial differential equations (1) to (3) for the dependent variables U, V, and T as functions of X, Y and  $\tau$ . Obviously we intend to obtain a non-steady solution to these equations. If we set  $\partial U/\partial \tau$  and  $\partial T/\partial \tau$  to zero, we will obtain a steady state solution. When the two clouds reach a common temperature and hence ionization structure, the non-steady solution would tend to the steady state solution. Therefore, it is essential that we should consider the non-steady state problem. As we increase the steps in time, we approach the steady state solution. We shall follow the method of solution described by Carnehan et al. (1989). We select the discrete points on X and Y axes and obtain the solution in successive time steps. An explicit scheme can be written as,

$$\frac{U'_{i,j} - U_{i,j}}{\Delta \tau} + \frac{U_{i,j} - U_{i-1,j}}{\Delta X} + V_{i,j} \frac{U_{i,j+1} - U_{i,j}}{\Delta Y} - T'_{i,j} + \frac{U_{i,j+1} - 2U_{i,j} + U_{i,j-1}}{(\Delta Y)^2}
 \tag{5}$$

$$\frac{T'_{i,j} - T_{i,j}}{\Delta \tau} + U_{i,j} \frac{T_{i,j} - T_{i-1,j}}{\Delta X} + V_{i,j} \frac{T_{i,j+1} - T_{i,j}}{\Delta Y} = \frac{1}{P_r} \frac{T_{i,j+1} - 2T_{i,j} + T_{i,j-1}}{(\Delta Y)^2}
 \tag{6}$$

$$\frac{U'_{i,j} - U'_{i-1,j}}{\Delta X} + \frac{V'_{i,j} - V'_{i,j-1}}{\Delta Y} = 0
 \tag{7}$$

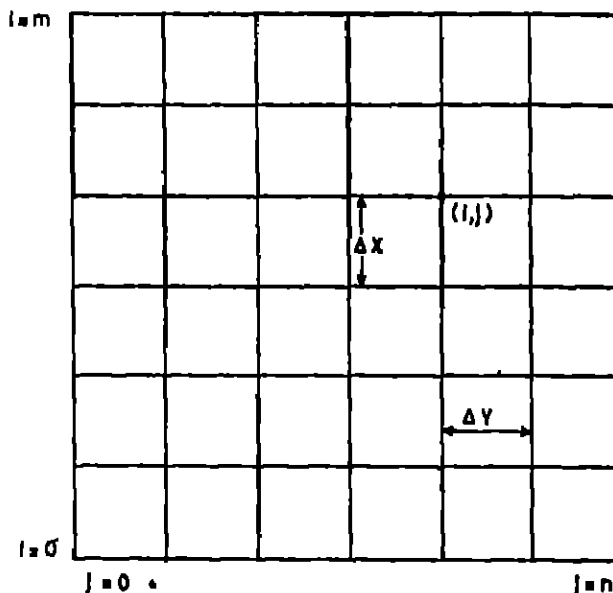
The stability condition is given by

$$\frac{U \Delta \tau}{\Delta X} + \frac{|V| \Delta \tau}{\Delta Y} + \frac{1}{P_r} \frac{2 \Delta \tau}{(\Delta Y)^2} \ll 1$$

(see Carnehan et al. 1989).

In this problem we shall consider that the Prandtl number to be equal to unity (Glatzmaier and Gilman 1981 a, b; Gilman and Glatzmaier 1981). We have computed the U, V and T fields at each step of  $\tau = .5$ , on the grid shown in Fig. 1. We have presented the results in the form of U, V, T grids in tables at  $\tau = .5, 1, 2, 3, 4, 5, 10, 15, 20, 25, 30, 35, 40, 45$  and 50. One can see that, initially, the changes are quite large and with successive time steps there is convergence and one obtains a steady state solution.

In the next paper, we shall present how this procedure could be applied to compressible fluids.



The difference grid

FIG. 1

## References

- Carnahan, B., Luther, H.A., Wilkes J.O. 1969, *Applied Numerical Methods*, John Wiley.  
 Glatzmaier, G.A., Gilman, P.A. 1981 (a) *Astrophys. J. Suppl. Ser.* 45, 351.  
 Glatzmaier, G.A., Gilman, P.A. 1981 (b) *Astrophys. J. Suppl. Ser.* 45, 381.  
 Gilman P.A., Glatzmaier, G.A. 1981, *Astrophys. J. Suppl. Ser.* 45, 395.  
 Hellums, J.D., Churchill, S.W. 1952, *A. J. Chem. Eng. J.*, 8, 690.















TAU=10.0

U COMPONENT OF VELOCITY

.0000E+00	.39827E+01	.29771E+01	.13807E+01	.47201E+00	.12605E+00	.27059E-01	.47476E-02	.68784E-03	.62114E-04	.00000E+00
.0000E+00	.39818E+01	.29762E+01	.13803E+01	.47189E+00	.12602E+00	.27052E-01	.47465E-02	.68769E-03	.62095E-04	.00000E+00
.0000E+00	.39774E+01	.29718E+01	.13783E+01	.47127E+00	.12586E+00	.27019E-01	.47408E-02	.68691E-03	.62002E-04	.00000E+00
.0000E+00	.39600E+01	.29545E+01	.13707E+01	.46882E+00	.12523E+00	.26889E-01	.47187E-02	.68586E-03	.61638E-04	.00000E+00
.0000E+00	.39059E+01	.29014E+01	.13469E+01	.46116E+00	.12327E+00	.26481E-01	.46501E-02	.67440E-03	.60520E-04	.00000E+00
.0000E+00	.37724E+01	.27733E+01	.12881E+01	.44214E+00	.11841E+00	.25876E-01	.44898E-02	.65104E-03	.77787E-04	.00000E+00
.0000E+00	.35067E+01	.25268E+01	.11719E+01	.40397E+00	.10865E+00	.23462E-01	.41418E-02	.60422E-03	.72360E-04	.00000E+00
.0000E+00	.30628E+01	.21331E+01	.98180E+00	.34883E+00	.92148E-01	.20851E-01	.35673E-02	.52467E-03	.63205E-04	.00000E+00
.0000E+00	.24018E+01	.15834E+01	.71372E+00	.24718E+00	.67640E-01	.14921E-01	.26957E-02	.48386E-03	.49219E-04	.00000E+00
.0000E+00	.14532E+01	.87440E+00	.37576E+00	.12790E+00	.35159E-01	.79053E-02	.14694E-02	.22734E-03	.28667E-04	.00000E+00
.0000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

V COMPONENT OF VELOCITY

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.0000E+00	.11060E-02	.22169E-02	.28561E-02	.28961E-02	.29044E-02	.29058E-02	.29058E-02	.29060E-02	.29061E-02	.29061E-02
.0000E+00	.4323E-02	.66834E-02	.10594E-01	.11207E-01	.11364E-01	.11397E-01	.11402E-01	.11403E-01	.11403E-01	.11403E-01
.0000E+00	.15200E-01	.26882E-01	.32758E-01	.35163E-01	.35264E-01	.35281E-01	.35284E-01	.35284E-01	.35284E-01	.35284E-01
.0000E+00	.33362E-01	.65371E-01	.80065E-01	.84819E-01	.86034E-01	.86285E-01	.86328E-01	.86334E-01	.86334E-01	.86334E-01
.0000E+00	.66427E-01	.12807E+00	.15713E+00	.16667E+00	.16912E+00	.16926E+00	.16970E+00	.16972E+00	.16972E+00	.16972E+00
.0000E+00	.11896E+00	.20937E+00	.25688E+00	.27267E+00	.27799E+00	.27799E+00	.27799E+00	.27801E+00	.27801E+00	.27801E+00
.0000E+00	.16525E+00	.30268E+00	.36970E+00	.39291E+00	.39904E+00	.40032E+00	.40054E+00	.40057E+00	.40057E+00	.40057E+00
.0000E+00	.23716E+00	.41442E+00	.49891E+00	.52673E+00	.53685E+00	.53860E+00	.53891E+00	.53895E+00	.53896E+00	.53896E+00
.0000E+00	.36330E+00	.58189E+00	.67583E+00	.70781E+00	.71660E+00	.71857E+00	.71894E+00	.71900E+00	.71901E+00	.71901E+00
.0000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

TEMPERATURE

.1000E+01	.57905E+00	.27062E+00	.10180E+00	.31008E-01	.77063E-02	.15770E-02	.26752E-03	.37811E-04	.44304E-05	.00000E+00
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.1000E+01	.57837E+00	.27015E+00	.10163E+00	.30951E-01	.76946E-02	.15747E-02	.26715E-03	.37760E-04	.44244E-05	.00000E+00
.1000E+01	.57631E+00	.26862E+00	.10107E+00	.30791E-01	.76564E-02	.15671E-02	.26591E-03	.37593E-04	.44050E-05	.00000E+00
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U COMPONENT OF VELOCITY

.00000E+00	.62489E+01	.59999E+01	.40407E+01	.22490E+01	.10733E+01	.48483E+00	.16114E+00	.51227E-01	.13273E-01	.00000E+00
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.00000E+00	.56114E+01	.51656E+01	.33741E+01	.18425E+01	.87000E+00	.35841E+00	.12959E+00	.41061E-01	.10534E-01	.00000E+00
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V COMPONENT OF VELOCITY

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.00000E+00	.83806E-01	.19183E+00	.27747E+00	.32960E+00	.35565E+00	.36668E+00	.37073E+00	.37203E+00	.37238E+00	.37238E+00
.00000E+00	.92564E-01	.20832E+00	.29844E+00	.35291E+00	.38010E+00	.39163E+00	.39507E+00	.39722E+00	.39758E+00	.39758E+00
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.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

TEMPERATURE

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U COMPONENT OF VELOCITY

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.0000E+00	.48251E+01	.42534E+01	.27292E+01	.15456E+01	.80393E+00	.36738E+00	.17174E+00	.67887E-01	.20748E-01	.00000E+00
.0000E+00	.43652E+01	.36917E+01	.23070E+01	.12723E+01	.64658E+00	.30530E+00	.13299E+00	.51753E-01	.15583E-01	.00000E+00
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.0000E+00	.14670E+01	.92753E+00	.45806E+00	.20382E+00	.84598E-01	.33091E-01	.12149E-01	.40542E-02	.10611E-02	.00000E+00
.0000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

V COMPONENT OF VELOCITY

.0000E+00	.78250E-01	.18392E+00	.27540E+00	.33977E+00	.37929E+00	.40093E+00	.41154E+00	.41611E+00	.41763E+00	.41763E+00
.0000E+00	.84711E-01	.19630E+00	.29089E+00	.35638E+00	.39611E+00	.41769E+00	.42820E+00	.43270E+00	.43419E+00	.43419E+00
.0000E+00	.92504E-01	.21102E+00	.30899E+00	.37555E+00	.41536E+00	.43676E+00	.44710E+00	.45149E+00	.45293E+00	.45293E+00
.0000E+00	.10240E+00	.22884E+00	.33046E+00	.39799E+00	.43770E+00	.45876E+00	.46883E+00	.47308E+00	.47445E+00	.47445E+00
.0000E+00	.11497E+00	.25089E+00	.35645E+00	.42476E+00	.46418E+00	.48462E+00	.49431E+00	.49834E+00	.49963E+00	.49963E+00
.0000E+00	.13146E+00	.27904E+00	.38880E+00	.45754E+00	.49611E+00	.51579E+00	.52492E+00	.52867E+00	.52984E+00	.52984E+00
.0000E+00	.15494E+00	.31646E+00	.43055E+00	.49909E+00	.53623E+00	.55466E+00	.56127E+00	.56309E+00	.56635E+00	.56738E+00
.0000E+00	.18981E+00	.36925E+00	.48735E+00	.55441E+00	.58907E+00	.60556E+00	.61277E+00	.61556E+00	.61640E+00	.61640E+00
.0000E+00	.24815E+00	.45084E+00	.57113E+00	.63190E+00	.66443E+00	.67747E+00	.68301E+00	.68505E+00	.68564E+00	.68564E+00
.0000E+00	.36675E+00	.59863E+00	.71315E+00	.76410E+00	.78525E+00	.79352E+00	.79656E+00	.79758E+00	.79784E+00	.79784E+00
.0000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

TEMPERATURE

.1000E+01	.61454E+00	.32708E+00	.16227E+00	.78268E-01	.36983E-01	.16899E-01	.73022E-02	.28684E-02	.88785E-03	.00000E+00
.1000E+01	.60327E+00	.31377E+00	.15222E+00	.71934E-01	.33388E-01	.15033E-01	.64216E-02	.24992E-02	.76708E-03	.00000E+00
.1000E+01	.59040E+00	.29913E+00	.14154E+00	.65382E-01	.29744E-01	.13169E-01	.55497E-02	.21362E-02	.64906E-03	.00000E+00
.1000E+01	.57543E+00	.28285E+00	.13018E+00	.58580E-01	.26049E-01	.11311E-01	.46907E-02	.17818E-02	.53498E-03	.00000E+00
.1000E+01	.55760E+00	.26447E+00	.11775E+00	.51486E-01	.22300E-01	.94641E-02	.38500E-02	.14391E-02	.42592E-03	.00000E+00
.1000E+01	.53573E+00	.24333E+00	.10426E+00	.44052E-01	.18499E-01	.76362E-02	.30350E-02	.11119E-02	.32333E-03	.00000E+00
.1000E+01	.50775E+00	.21841E+00	.89323E-01	.36219E-01	.14649E-01	.58476E-02	.22557E-02	.80359E-03	.22905E-03	.00000E+00
.1000E+01	.46967E+00	.18800E+00	.72483E-01	.27915E-01	.10770E-01	.41163E-02	.15273E-02	.52726E-03	.14553E-03	.00000E+00
.1000E+01	.41235E+00	.14885E+00	.53011E-01	.19667E-01	.69043E-02	.24867E-02	.87391E-03	.28749E-03	.76091E-04	.00000E+00
.1000E+01	.30770E+00	.93670E-01	.29642E-01	.96454E-02	.31774E-02	.10450E-02	.33725E-03	.10273E-03	.25435E-04	.00000E+00
.1000E+01	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00



U COMPONENT OF VELOCITY

.00000E+00	.62501E+01	.60875E+01	.43029E+01	.26670E+01	.15281E+01	.81956E+00	.40767E+00	.18044E+00	.60611E-01	.00000E+00
.00000E+00	.59386E+01	.56649E+01	.39323E+01	.23987E+01	.13547E+01	.71715E+00	.35251E+00	.15434E+00	.51327E-01	.00000E+00
.00000E+00	.56013E+01	.52183E+01	.35494E+01	.21267E+01	.11818E+01	.61635E+00	.29887E+00	.12924E+00	.42891E-01	.00000E+00
.00000E+00	.52320E+01	.47882E+01	.31534E+01	.18513E+01	.10098E+01	.51767E+00	.24710E+00	.10532E+00	.34173E-01	.00000E+00
.00000E+00	.48233E+01	.42380E+01	.27431E+01	.15729E+01	.83951E+00	.42180E+00	.19762E+00	.82808E-01	.26455E-01	.00000E+00
.00000E+00	.43640E+01	.36938E+01	.23174E+01	.12924E+01	.67215E+00	.32962E+00	.15099E+00	.61977E-01	.19435E-01	.00000E+00
.00000E+00	.38379E+01	.31038E+01	.18753E+01	.10110E+01	.58939E+00	.28239E+00	.10795E+00	.43184E-01	.13232E-01	.00000E+00
.00000E+00	.32105E+01	.24572E+01	.14163E+01	.75160E+00	.35385E+00	.16193E+00	.69509E-01	.26863E-01	.79937E-02	.00000E+00
.00000E+00	.24595E+01	.17390E+01	.94173E+00	.45920E+00	.20999E+00	.90996E-01	.37096E-01	.13683E-01	.39021E-02	.00000E+00
.00000E+00	.14670E+01	.92784E+00	.45899E+00	.20523E+00	.86046E-01	.34224E-01	.12854E-01	.13979E-02	.11743E-02	.00000E+00
.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

V COMPONENT OF VELOCITY

.00000E+00	.77829E-01	.18349E+00	.27615E+00	.34322E+00	.38656E+00	.41216E+00	.42595E+00	.43248E+00	.43480E+00	.43480E+00
.00000E+00	.84370E-01	.19601E+00	.29172E+00	.35971E+00	.40295E+00	.42815E+00	.44156E+00	.44784E+00	.45004E+00	.45004E+00
.00000E+00	.92317E-01	.21084E+00	.30984E+00	.37870E+00	.42170E+00	.44637E+00	.45931E+00	.46529E+00	.46737E+00	.46737E+00
.00000E+00	.10219E+00	.22874E+00	.33131E+00	.40091E+00	.46744E+00	.47981E+00	.48584E+00	.48737E+00	.48737E+00	.48737E+00
.00000E+00	.11481E+00	.25085E+00	.35728E+00	.42743E+00	.49231E+00	.50396E+00	.50917E+00	.51093E+00	.51093E+00	.51093E+00
.00000E+00	.13154E+00	.27904E+00	.38957E+00	.45990E+00	.50060E+00	.52240E+00	.53316E+00	.53786E+00	.53941E+00	.53941E+00
.00000E+00	.15485E+00	.31650E+00	.43125E+00	.50111E+00	.53999E+00	.56011E+00	.56972E+00	.57380E+00	.57511E+00	.57511E+00
.00000E+00	.18975E+00	.36931E+00	.48795E+00	.55605E+00	.59201E+00	.60975E+00	.61785E+00	.62115E+00	.62217E+00	.62217E+00
.00000E+00	.24812E+00	.45091E+00	.57160E+00	.63509E+00	.66608E+00	.68027E+00	.68633E+00	.68865E+00	.68933E+00	.68933E+00
.00000E+00	.36674E+00	.59870E+00	.71345E+00	.76476E+00	.78627E+00	.79883E+00	.79914E+00	.79943E+00	.79943E+00	.79943E+00
.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00

TEMPERATURE

.10000E+01	.61272E+00	.32397E+00	.15882E+00	.75580E-01	.35555E-01	.16506E-01	.74169E-02	.30705E-02	.99298E-03	.00000E+00
.10000E+01	.60176E+00	.31117E+00	.14934E+00	.69698E-01	.32199E-01	.14698E-01	.65043E-02	.26564E-02	.84900E-03	.00000E+00
.10000E+01	.58917E+00	.29701E+00	.13918E+00	.63560E-01	.28776E-01	.12890E-01	.56068E-02	.22549E-02	.71114E-03	.00000E+00
.10000E+01	.57444E+00	.28114E+00	.12822E+00	.57132E-01	.25282E-01	.11086E-01	.47280E-02	.18682E-02	.58024E-03	.00000E+00
.10000E+01	.55684E+00	.26314E+00	.11629E+00	.50375E-01	.21716E-01	.92904E-02	.38727E-02	.14991E-02	.45736E-03	.00000E+00
.10000E+01	.53515E+00	.24233E+00	.10318E+00	.43240E-01	.18076E-01	.75118E-02	.30875E-02	.11510E-02	.34379E-03	.00000E+00
.10000E+01	.50734E+00	.21770E+00	.88588E-01	.35664E-01	.14367E-01	.57634E-02	.22619E-02	.82891E-03	.24118E-03	.00000E+00
.10000E+01	.46940E+00	.18753E+00	.72005E-01	.27577E-01	.10603E-01	.40675E-02	.15301E-02	.53940E-03	.15176E-03	.00000E+00
.10000E+01	.41219E+00	.14859E+00	.52758E-01	.18899E-01	.68257E-02	.24650E-02	.87511E-03	.29251E-03	.78580E-04	.00000E+00
.10000E+01	.30763E+00	.93567E-01	.29553E-01	.95931E-02	.31559E-02	.10398E-02	.33761E-03	.10359E-03	.26009E-04	.00000E+00
.10000E+01	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00	.00000E+00





TAU=50.0

U COMPONENT OF VELOCITY

.00000E+00 .62480E+01 .60867E+01 .43074E+01 .26796E+01 .15877E+01 .84141E+00 .42609E+00 .19210E+00 .65394E-01 .00000E+00  
 .00000E+00 .59371E+01 .56643E+01 .39360E+01 .24091E+01 .13707E+01 .73476E+00 .36723E+00 .16357E+00 .55080E-01 .00000E+00  
 .00000E+00 .56000E+01 .52179E+01 .35259E+01 .21351E+01 .11945E+01 .63017E+00 .31030E+00 .13634E+00 .45347E-01 .00000E+00  
 .00000E+00 .52311E+01 .47440E+01 .31559E+01 .18578E+01 .10195E+01 .52817E+00 .25566E+00 .11057E+00 .36264E-01 .00000E+00  
 .00000E+00 .46226E+01 .42379E+01 .27450E+01 .15778E+01 .84672E+00 .42942E+00 .20377E-01 .86508E-01 .27909E-01 .00000E+00  
 .00000E+00 .43634E+01 .36938E+01 .23188E+01 .12959E+01 .67719E+00 .33483E+00 .15310E+00 .64415E-01 .20377E-01 .00000E+00  
 .00000E+00 .38376E+01 .31038E+01 .18763E+01 .10134E+01 .51283E+00 .24566E+00 .11046E+00 .44639E-01 .13784E-01 .00000E+00  
 .00000E+00 .32163E+01 .24573E+01 .14169E+01 .73297E+00 .35569E+00 .16371E+00 .70832E-01 .27428E-01 .82688E-02 .00000E+00  
 .00000E+00 .24594E+01 .17390E+01 .94205E+00 .45986E+00 .21082E+00 .91758E-01 .37634E-01 .13973E-01 .40053E-02 .00000E+00  
 .00000E+00 .14669E+01 .92786E+00 .45911E+00 .20543E+00 .86272E-01 .34411E-01 .12976E-01 .44588E-02 .11947E-02 .00000E+00  
 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00

V COMPONENT OF VELOCITY

.00000E+00 .77717E-01 .18332E+00 .27616E+00 .34380E+00 .38806E+00 .41472E+00 .42943E+00 .43657E+00 .43915E+00 .43915E+00  
 .00000E+00 .84273E-01 .19587E+00 .29175E+00 .36025E+00 .40432E+00 .43046E+00 .44469E+00 .45150E+00 .45394E+00 .45394E+00  
 .00000E+00 .92237E-01 .21072E+00 .30989E+00 .37919E+00 .42293E+00 .44843E+00 .46209E+00 .46853E+00 .47080E+00 .47080E+00  
 .00000E+00 .10212E+00 .22864E+00 .33136E+00 .40136E+00 .44456E+00 .46925E+00 .48223E+00 .48825E+00 .49034E+00 .49034E+00  
 .00000E+00 .11475E+00 .25078E+00 .35734E+00 .42163E+00 .47621E+00 .49386E+00 .50602E+00 .51154E+00 .51342E+00 .51342E+00  
 .00000E+00 .13150E+00 .27899E+00 .38963E+00 .46025E+00 .50139E+00 .52369E+00 .53485E+00 .53979E+00 .54144E+00 .54144E+00  
 .00000E+00 .15482E+00 .31646E+00 .43130E+00 .50140E+00 .54063E+00 .56112E+00 .57103E+00 .57528E+00 .57666E+00 .57666E+00  
 .00000E+00 .18973E+00 .36929E+00 .48800E+00 .55627E+00 .59249E+00 .61046E+00 .61878E+00 .62219E+00 .62326E+00 .62326E+00  
 .00000E+00 .24811E+00 .45090E+00 .57164E+00 .63325E+00 .66638E+00 .68072E+00 .68689E+00 .68926E+00 .68997E+00 .68997E+00  
 .00000E+00 .36674E+00 .59870E+00 .71348E+00 .74848E+00 .78640E+00 .79501E+00 .79825E+00 .79937E+00 .79967E+00 .79967E+00  
 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00

TEMPERATURE

.10000E+01 .61231E+00 .32319E+00 .15781E+00 .74608E-01 .34824E-01 .16068E-01 .72067E-02 .29897E-02 .96955E-03 .00000E+00  
 .10000E+01 .60142E+00 .31053E+00 .14851E+00 .68893E-01 .31597E-01 .14339E-01 .63321E-02 .25899E-02 .82966E-03 .00000E+00  
 .10000E+01 .58889E+00 .29648E+00 .13850E+00 .62908E-01 .28292E-01 .12604E-01 .54697E-02 .22019E-02 .69570E-03 .00000E+00  
 .10000E+01 .57422E+00 .28072E+00 .12768E+00 .56621E-01 .24906E-01 .10865E-01 .46227E-02 .18276E-02 .56843E-03 .00000E+00  
 .10000E+01 .55667E+00 .26281E+00 .11588E+00 .49989E-01 .21436E-01 .91274E-02 .37957E-02 .14693E-02 .44881E-03 .00000E+00  
 .10000E+01 .53503E+00 .24209E+00 .10288E+00 .42962E-01 .17879E-01 .73991E-02 .29949E-02 .11310E-02 .33606E-03 .00000E+00  
 .10000E+01 .50725E+00 .21753E+00 .88363E-01 .42962E-01 .14239E-01 .56923E-02 .22293E-02 .81673E-03 .23775E-03 .00000E+00  
 .10000E+01 .46935E+00 .18743E+00 .71881E-01 .27470E-01 .10531E-01 .54088E-02 .15129E-02 .53314E-03 .15004E-03 .00000E+00  
 .10000E+01 .41216E+00 .14454E+00 .52696E-01 .18849E-01 .67442E-02 .24489E-02 .86833E-03 .29014E-03 .77958E-04 .00000E+00  
 .10000E+01 .38762E+00 .93547E-01 .29533E-01 .95791E-02 .31481E-02 .10363E-02 .33645E-03 .10355E-03 .25905E-04 .00000E+00  
 .10000E+01 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00 .00000E+00