# Spectroscopic study of CEMP-(s \& r/s) stars 

# Revisiting classification criteria and formation scenarios, highlighting i-process nucleosynthesis ${ }^{\star}, \star \star, \star \star \star$ 

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#### Abstract

Context. The origin of the enhanced abundances of both $s$ - and $r$-process elements observed in a subclass of carbon-enhanced metalpoor (CEMP) stars, denoted CEMP-r/s stars, still remains poorly understood. The $i$-process nucleosynthesis has been suggested as one of the most promising mechanisms for the origin of these stars. Aims. Our aim is to better understand the chemical signatures and formation mechanism(s) of five previously claimed potential CH star candidates HE $0017+0055$, HE 2144-1832, HE 2339-0837, HD 145777, and CD-27 14351 through a detailed systematic follow-up spectroscopic study based on high-resolution spectra. Methods. The stellar atmospheric parameters, the effective temperature $T_{\text {eff }}$, the microturbulent velocity $\zeta$, the surface gravity $\log g$, and the metallicity $[\mathrm{Fe} / \mathrm{H}]$ are derived from local thermodynamic equilibrium analyses using model atmospheres. Elemental abundances of $\mathrm{C}, \mathrm{N}, \alpha$-elements, iron-peak elements, and several neutron-capture elements are estimated using the equivalent width measurement technique as well as spectrum synthesis calculations in some cases. In the context of the double enhancement observed in four of the programme stars, we have critically examined whether the literature $i$-process model yields ( $[\mathrm{X} / \mathrm{Fe}]$ ) of heavy elements can explain the observed abundance distribution. Results. The estimated metallicity $[\mathrm{Fe} / \mathrm{H}]$ of the programme stars ranges from -1.63 to -2.74 . All five stars show enhanced abundance for Ba, and four of them exhibit enhanced abundance for Eu. Based on our analysis, HE 0017+0055, HE 2144-1832, and HE 2339-0837 are found to be CEMP-r/s stars, whereas HD 145777 and CD-27 14351 show characteristic properties of CEMP-s stars. From a detailed analysis of different classifiers of CEMP stars, we have identified the one which best describes the CEMP-s and CEMP-r/s stars. We found that for both CEMP-s and CEMP-r/s stars, $[\mathrm{Ba} / \mathrm{Eu}]$ and $[\mathrm{La} / \mathrm{Eu}]$ exhibit positive values and $[\mathrm{Ba} / \mathrm{Fe}] \geq 1.0$. However, CEMP$\mathrm{r} / \mathrm{s}$ stars satisfy $[\mathrm{Eu} / \mathrm{Fe}] \geq 1.0,0.0 \leq[\mathrm{Ba} / \mathrm{Eu}] \leq 1.0$, and/or $0.0 \leq[\mathrm{La} / \mathrm{Eu}] \leq 0.7$. CEMP-s stars normally show $[\mathrm{Eu} / \mathrm{Fe}]<1.0$ with $[\mathrm{Ba} / \mathrm{Eu}]>0.0$ and $/$ or $[\mathrm{La} / \mathrm{Eu}]>0.5$. If $[\mathrm{Eu} / \mathrm{Fe}] \geq 1.0$, then the condition on $[\mathrm{Ba} / \mathrm{Eu}]$ and $/$ or $[\mathrm{La} / \mathrm{Eu}]$ for a star to be a CEMP-s star is $[\mathrm{Ba} / \mathrm{Eu}]>1.0 \mathrm{and} /$ or $[\mathrm{La} / \mathrm{Eu}]>0.7$. Using a large sample of similar stars from the literature we have examined whether the ratio of heavy- $s$ to light- $s$ process elements [hs/ls] alone can be used as a classifier, and if there are any limiting values for [hs/ls] that can be used to distinguish between CEMP-s and CEMP-r/s stars. Even though they peak at different values of [hs/ls], CEMP-s and CEMP-r/s stars show an overlap in the range $0.0<[\mathrm{hs} / \mathrm{ls}]<1.5$, and hence this ratio cannot be used to distinguish between CEMP-s and CEMP-r/s stars. We have noticed a similar overlap in the case of $[\mathrm{Sr} / \mathrm{Ba}]$ as well, in the range $-1.6<[\mathrm{Sr} / \mathrm{Ba}]<-0.5$, and hence this ratio also cannot be used to separate the two subclasses.


Key words. stars: abundances - stars: carbon - stars: late-type

## 1. Introduction

The origin and evolution of neutron-capture elements in our Galaxy are still unclear. That is why CH stars, with their metalpoor counterpart carbon-enhanced metal-poor (CEMP) stars have been studied for a very long time. Both CH and CEMP stars are characterised by the presence of a strong $G$ band of CH .

[^0]While the broad category of objects defined to include stars with $[\mathrm{C} / \mathrm{Fe}]^{1}>1.0$ and $[\mathrm{Fe} / \mathrm{H}]<-1.0$ are referred to as CEMP stars (Beers \& Christlieb 2005), CH stars normally exhibit a metallicity range of that of Ba stars. The main differences between CH and Ba stars lie in the carbon abundance and the value of C/O. Unlike CH stars Ba stars do not exhibit enhancement of carbon. It has been pointed out by several authors that the $s$ process enhanced CEMP stars, the so-called CEMP-s stars, are low-metallicity analogues of CH stars and Ba stars (see Lucatello et al. 2005; Starkenburg et al. 2014, and references therein). When a star ascends to the giant branch, the abundance of carbon

[^1]at the surface decreases due to the mixing with the first dredgeup affected internal material. Spite et al. (2005) observed that in highly evolved metal-poor red giants the abundance of carbon decreases further due to the influence of extra mixing in the evolutionary path, which increases the abundance of nitrogen. Including these evolutionary effects, Aoki et al. (2007) put forward a slightly different classification scheme that considers carbon abundance ( $[\mathrm{C} / \mathrm{Fe}] \geq+0.7$ ) along with the luminosity of the star. Some authors (Lee et al. 2013; Skúladóttir et al. 2015) use $[\mathrm{C} / \mathrm{Fe}] \geq+0.7$ to define CEMP stars. The subclasses of CEMP stars help us to uncover the processes by which the neutron-capture elements are produced. Depending upon the enhancement of elements produced by slow (' $s$ ') and rapid (' $r$ ') neutron-capture processes, CEMP stars are divided into different subclasses (Beers \& Christlieb 2005; Jonsell et al. 2006; Masseron et al. 2010; Abate et al. 2016; Frebel 2018; Hansen et al. 2019). The early subclassification of CEMP class was given by Beers \& Christlieb (2005):

- CEMP: [C/Fe] > 1.0;
- CEMP-s: $[\mathrm{Ba} / \mathrm{Fe}]>+1.0$, and $[\mathrm{Ba} / \mathrm{Eu}]>0.5$ (characterised by enhancement of barium, which is an $s$-process indicator);
- CEMP-r: $[\mathrm{Eu} / \mathrm{Fe}]>+1.0$ (characterised by enhancement of europium, which is an $r$-process indicator);
- CEMP-r/s: $0.0<[\mathrm{Ba} / \mathrm{Eu}]<0.5$ (enhanced in both barium and europium);
- CEMP-no: $[\mathrm{Ba} / \mathrm{Fe}]<0$ (not enhanced in heavy elements).

Abate et al. (2016) adopted the following classification:

- CEMP: [C/Fe] > 1.0;
- CEMP-s: $[\mathrm{Ba} / \mathrm{Fe}]>+1.0$ and $[\mathrm{Ba} / \mathrm{Eu}]>0$;
- CEMP-r: $[\mathrm{Eu} / \mathrm{Fe}]>+1.0$ and $[\mathrm{Ba} / \mathrm{Eu}] \leq 0$;
- CEMP-r/s: $[\mathrm{Eu} / \mathrm{Fe}]>+1.0,[\mathrm{Ba} / \mathrm{Fe}]>+1.0$, and $[\mathrm{Ba} / \mathrm{Eu}]>$ 0.0;
- CEMP-no: $[\mathrm{Ba} / \mathrm{Fe}] \leq 1.0$ and $[\mathrm{Eu} / \mathrm{Fe}] \leq 1.0$;

These classification criteria for CEMP-s and CEMP-r/s stars are also adopted by Jonsell et al. (2006) and Masseron et al. (2010).

Frebel (2018) adopted the CEMP star definition of Aoki et al. (2007), and put forward a classification scheme of CEMP stars as follows:

- CEMP: $[\mathrm{C} / \mathrm{Fe}]>0.7$ for $\log \left(L / L_{\odot}\right) \leq 2.3 \&[\mathrm{C} / \mathrm{Fe}] \geq[3.0-$ $\left.\log \left(L / L_{\odot}\right)\right]$ for $\log \left(L / L_{\odot}\right)>2.3$;
- r I: $0.3 \leq[\mathrm{Eu} / \mathrm{Fe}] \leq+1.0$ and $[\mathrm{Ba} / \mathrm{Eu}]<0.0$;
- r II: $[\mathrm{Eu} / \mathrm{Fe}]>+1.0$ and $[\mathrm{Ba} / \mathrm{Eu}]<0.0$;
$-\mathrm{r}_{\text {lim }}:[\mathrm{Eu} / \mathrm{Fe}]<0.3,[\mathrm{Sr} / \mathrm{Ba}]>0.5$, and $[\mathrm{Sr} / \mathrm{Eu}]>0.0$;
- CEMP-s: $[\mathrm{Ba} / \mathrm{Fe}]>+1.0,[\mathrm{Ba} / \mathrm{Eu}]>+0.5,[\mathrm{Ba} / \mathrm{Pb}]>-1.5$;
- CEMP-r+s: $0.0<[\mathrm{Ba} / \mathrm{Eu}]<+0.5$ and $-1.0<[\mathrm{Ba} / \mathrm{Pb}]<-0.5$;
- CEMP-i: $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$ and $[\mathrm{Hf} / \mathrm{Ir}] \sim 1.0$ (some authors use the 'CEMP-i' nomenclature to indicate CEMP-r/s stars). The $r$-process enriched stars may or may not be carbon enhanced.
Hansen et al. (2019) recently gave a new scheme of classification based on [ $\mathrm{Sr} / \mathrm{Ba}$ ]:
- CEMP: [C/Fe] > 1.0;
- CEMP-no: [Sr/Ba] >0.75;
- CEMP-s: $-0.5<[\mathrm{Sr} / \mathrm{Ba}]<0.75$;
- CEMP-r/s: $-1.5<[\mathrm{Sr} / \mathrm{Ba}]<-0.5$;
- CEMP-r: [Sr/Ba] <-1.5.

A number of different scenarios describing the origin of enhanced heavy elements on the surface chemical composition of CEMP-s and CEMP-r/s stars are available in the literature (Jonsell et al. 2006; Lugaro et al. 2009). For $s$-process enrichment a binary AGB nucleosynthesis model is considered where the star we observe (secondary) is in a binary configuration with an evolved star (primary). This primary star completes the AGB
phase and becomes a white dwarf, and in the process expels $s$ process enriched matter which is then accreted by the secondary star via two major mass-transfer mechanisms: Roche-lobe overflow (RLOF) and wind accretion (Abate et al. 2013). Most of the CEMP-s stars are confirmed as binary systems through longterm radial velocity monitoring (McClure 1983, 1984; McClure \& Woodsworth 1990; Lucatello et al. 2005; Jorissen et al. 2016b; Hansen et al. 2016b). In addition, nucleosynthesis occurring in the inter-shell region of the secondary star may also contribute to both the light and heavy $s$-process element enrichment when the synthesised material is brought to the surface via different processes like convective mixing (due to temperature gradient), nonconvective processes like thermohaline mixing (due to density gradient) (Stancliffe et al. 2007), rotation mechanisms, and third dredge-up (TDU). Several proposed scenarios are also being put forward for the origin of the CEMP-r/s stars by several authors: the primary, after passing through the AGB phase, explodes as a type 1.5 supernova (Zijlstra 2004; Wanajo et al. 2006); the enrichment of $r$-process elements is produced via an accretioninduced collapse (Qian \& Wasserburg 2003; Cohen et al. 2003) and enriches the secondary; a triple star system having a massive star is responsible for enriching the secondary star (Cohen et al. 2003); a primordial origin (i.e. the environment, in which the CEMP-r/s star was born, was already enriched by $r$-process elements) (Bisterzo et al. 2011). Another nucleosynthesis process, generally termed the intermediate (i) neutron-capture process, is a neutron-capture regime at neutron densities intermediate between those for $s$-process and $r$-process and has also been invoked (Cowan \& Rose 1977). Multiple stellar sites such as very metal-poor AGB stars (Campbell \& Lattanzio 2008; Cristallo et al. 2009; Campbell et al. 2010; Stancliffe et al. 2011), very late thermal pulse (VLTP) in post-AGB stars (Herwig et al. 2011), super-AGB stars (Doherty et al. 2015; Jones et al. 2016), lowmetallicity massive stars (Banerjee et al. 2018; Clarkson et al. 2018), and rapidly accreting white dwarfs (Denissenkov et al. 2017; Côté et al. 2018; Denissenkov et al. 2019) are expected to meet the conditions necessary for the $i$-process.

From medium-resolution spectroscopic analysis of a sample of carbon star candidates from the Hamburg/ESO survey (Christlieb et al. 2001), several potential CH star candidates were identified by Goswami (2005) and Goswami et al. (2010). In this work we present results from a follow-up high-resolution spectroscopic analysis of three such potential CH star candidates HE 0017+0055, HE 2144-1832, and HE 2339-0837, along with two potential CH star candidates HD 145777 and CD-27 14351 listed in the CH star catalogue of Bartkevicius (1996). A detailed systematic spectroscopic study of these five previously claimed potential CH stars is conducted for a better understanding of their chemical signatures and formation mechanism(s).

The paper is organised as follows. In Sect. 2, we present a brief summary of the earlier studies or any reported measurements on our programme stars available in the literature. The details of observations and data reduction are presented in Sect. 3. Determination of photometric temperatures is discussed in Sect. 4. Estimation of radial velocity and derivation of stellar atmospheric parameters are presented in Sect. 5. Abundance analysis results along with a discussion about abundance uncertainties are presented in Sect. 6. Section 7 discusses the results from the kinematic analysis of our programme stars. A comprehensive discussion on several proposed formation scenarios of CEMP-r/s stars is presented in Sect. 8. A detailed comparison of the observed abundances with $i$-process model predictions is also presented in this section along with a discussion on different classifiers of CEMP-s and CEMP-r/s stars. Details of estimations
of [hs/Fe], [ $\mathrm{ls} / \mathrm{Fe}$ ], and [hs/ls] from heavy element abundances of a sample of CEMP-s and CEMP-r/s stars from the literature are also presented in this section. Conclusions are drawn in Sect. 9.

## 2. Previous studies of the programme stars: a summary, and the novelty of this work

HD 145777. We present the first-time abundance analysis for this object. Bidelman (1956) classified HD 145777 as a CH star differing from the earlier classifications by Mayall \& Cannon (1940) and Sanford (1944), who assigned this object to spectral class R3 and R4 respectively. Bergeat et al. (2001) and McDonald et al. (2012) performed studies on several stars including HD 145777 and derived effective temperature using the spectral energy distribution (SED) method of temperature calibration. Our spectroscopic estimate differs by less than $\sim 100 \mathrm{~K}$ from these studies. First-time abundance estimates for several elements including C through Zn , and neutron-capture elements are presented based on high-resolution spectroscopy.
$C D-27$ 14351. McDonald et al. (2012) reported estimates of effective temperatures for a large sample of Hipparcos stars including CD-27 14351 using the spectral energy distribution (SED) method of temperature calibration. Karinkuzhi et al. (2017) performed a detailed chemical composition study for this object and reported it to be a CEMP-r/s star with a high value of $[\mathrm{Eu} / \mathrm{Fe}]=1.65$. These authors also obtained a negative value $(-0.05)$ for $[\mathrm{hs} / \mathrm{ls}$ ] for this object, in contrast to all CEMP-r/s stars known so far. A survey of the literature shows that, in general, CEMP-r/s stars exhibit a positive value $(\sim 0.4<[\mathrm{hs} / \mathrm{ls}]<$ 1.7) for [hs/ls]. This discrepancy prompted us to re-investigate the nature of this object. We have therefore re-examined its spectrum covering the wavelength range $3500-9000 \AA$. While the temperature estimate of our work differs from McDonald et al. (2012) by $\sim 100 \mathrm{~K}$, our estimates for the atmospheric parameters are similar to those of Karinkuzhi et al. (2017). However, our estimates of elemental abundances for Ce and Eu , differ from those of Karinkuzhi et al. (2017) by 0.74 and 1.26 dex, respectively.

HE 0017+0055. This object was discovered by Stephenson (1989) as an R-type star, and was assigned number 39 in the General Catalogue of Galactic Carbon Stars. The object is also listed in the list of faint high-latitude carbon stars of Christlieb et al. (2001). Kennedy et al. (2011) estimated the atmospheric parameters and the abundances of $\mathrm{C}, \mathrm{N}$, and O for this object. Jorissen et al. (2016a) did a more detailed analysis of this object, deriving the abundances of some of the neutron-capture elements (Y, Zr, La, Ce, Nd, Sm, Eu, Dy, and Er ) along with C and N . The effective temperature value for the object estimated by these authors differ from our estimate (by $\sim 120-180 \mathrm{~K}$ ). While Kennedy et al. (2011) estimated the $\log g$ and $[\mathrm{Fe} / \mathrm{H}]$ to be 0.18 and -2.72 , respectively, Jorissen et al. (2016a) adopted $\log g=1.0$ and estimated $[\mathrm{Fe} / \mathrm{H}]=-2.40$. Both these studies adopt a value of $2 \mathrm{~km} \mathrm{~s}^{-1}$ for microturbulence. Jorissen et al. (2016a) determined a low value ( $\sim 4$ ) for the carbon isotopic ratio ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$, which does not differ much from the value of 1.3 estimated by Goswami (2005) based on medium-resolution spectra. From a long-term radial velocity monitoring programme Jorissen et al. (2016b) found this object to exhibit low-amplitude velocity variations with a period of 384 days superimposed on a long-term trend. The 384-day period was attributed either to a low-mass inner companion or to stellar pulsation. The differences in the estimates of the
different groups prompted us to re-investigate this object based on a high-resolution spectrum.

HE 2144-1832. This object was studied by Stephenson (1989) and found to be an R-type star. Hansen et al. (2016a) reported estimates of stellar atmospheric parameters and abundance estimates for four elements for this object: $\mathrm{C}, \mathrm{N}, \mathrm{Ba}$, and Sr. This study was based on spectra obtained using Xshooter spectrograph (Vernet et al. 2011) covering wavelength regions $3000-5000 \AA, 5500-10000 \AA$, and $10000-25000 \AA$ at spectral resolutions of 4350,7450 , and 5300 respectively. We conducted a detailed chemical composition study for this object using a higher resolution ( $R \sim 60000$ ) spectrum with high signal-to-noise ratio (S/N). New estimates for C, N, Ba, and Sr , and first-time abundance estimates for several other elements including neutron-capture elements are presented in this work. We also estimated ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C} \sim 2.5$ for this object, which is not too different from the estimated value of 2.1 reported by (Goswami 2005) based on a low-resolution spectroscopic study.

HE 2339-0837. Kennedy et al. (2011) reported the atmospheric parameters and the abundances of C and O for this object based on medium-resolution spectra. Detailed chemical abundance studies have not been reported in the literature for this object. We present a first-time detailed abundance analysis for this object based on a high-resolution spectrum.

Regarding the binary nature of the programme stars, HD 145777, HE 2144-1832, and HE 0017+0055 are established as radial velocity variables based on long-term radial velocity monitoring programmes, and hence Jorissen et al. (2016b) suggested these objects to be in long-period binaries. Information on binarity is not available in the literature for HE 2339-0837 and CD-27 14351.

## 3. Observations and data reduction

High-quality high-resolution spectra of HD 145777, HE 0017+ 0055, and HE 2144-1832 were obtained using the Hanle Echelle SPectrograph (HESP) attached to the 2 m Himalayan Chandra Telescope (HCT) at the Indian Astronomical Observatory (IAO), Hanle. The detector is a $4 \mathrm{~K} \times 4 \mathrm{~K}$ CCD with a pixel size of $15 \mu$. The wavelength coverage spans $3500-10000 \AA$ at a spectral resolution $(\lambda / \delta \lambda)$ of 60000 . Data is reduced following a standard procedure using Image Reduction and Analysis Facility (IRAF) software packages. Spectroscopic reduction procedures such as trimming, bias subtraction, flat normalisation, and extraction are applied to the raw data. Wavelength calibration is done using a high-resolution Th-Ar arc spectrum. A high-resolution spectrum ( $R \sim 48000$ ) from the Fiber-fed Extended Range Optical Spectrograph (FEROS), attached to the 1.52 m ESO telescope at La Silla, Chile, is used for CD-27 14351. The spectrum covers 3520-9200 A in the wavelength region. For HE 2339-0837, a high-resolution spectrum $(R \sim 50000)$ is taken from the SUBARU archive ${ }^{2}$ acquired with the High Dispersion Spectrograph (HDS) of the 8.2 m Subaru Telescope. The wavelength coverage of the observed spectra spans from about 4020-6775 $\AA$, with a gap of about $100 \AA$ (from 5340 to $5440 \AA$ ) due to the physical spacing of the CCD detectors. The spectra are continuum fitted using the task continuum in IRAF and dispersion corrected. A few sample spectra are shown in Fig. 1. Table 1 gives the basic data for the programme stars.

[^2]Table 1. Basic data for the programme stars.

| Star name | RA(2000) | $\operatorname{Dec}(2000)$ | $B$ | $V$ | $J$ | $H$ | $K$ | Exposure <br> $(\mathrm{s})$ | Date of Obs. | Source <br> of spectrum |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HD 145777 | 161313.87 | -151201.25 | 11.55 | 10.31 | 7.73 | 7.07 | 6.84 | 2400 | $01-06-2017$ | HESP |
| CD-27 14351 | 195308.00 | -272814.97 | 11.82 | 9.70 | 7.02 | 6.30 | 6.14 | 1200 | $14-07-2000$ | FEROS |
| HE 0017+0055 | 002021.60 | +011206.81 | 12.99 | 11.66 | 9.31 | 8.70 | 8.50 | 2700 | $21-09-2017$ | HESP |
| HE 2144-1832 | 214654.66 | -181815.59 | 12.65 | 10.97 | 8.77 | 8.18 | 7.96 | 2700 | $08-11-2017$ | HESP |
| HE 2339-0837 | 234159.93 | -082118.61 | 15.32 | 14.00 | 12.63 | 12.11 | 12.03 | 900 | $27-06-2004$ | SUBARU/HDS |



Fig. 1. Sample spectra of the programme stars in the wavelength region 5160-5190 Å.

## 4. Photometric temperatures

The photometric temperatures of the programme stars were determined using broad-band colours, optical and IR, with colour-temperature calibrations available for main-sequence stars (Alonso et al. 1996) and giants (Alonso et al. 1999), and are based on the infrared flux method (IRFM). The procedure followed is as described in Goswami et al. (2006, 2015). As Alonso et al. $(1996,1999)$ reported, the uncertainty on temperature calculations using the IRFM method is about $\sim 90 \mathrm{~K}$. Precise photometric data, reliable reddening estimates, and metallicity information are required when using this method. We estimated the photometric temperatures of the stars at several assumed metallicity values. The estimated temperatures, along with the adopted metallicities, are listed in Table 2. Temperature estimates obtained using calibration relations involving $(J-K)$, $(J-H)$, and $(V-K)$ colours give values that differ by about $\pm 200 \mathrm{~K}$. We do not consider the empirical $T_{\text {eff }}$ scale for the $B-V$ colour indices as this calibration relation may not give reliable estimates, due to the effect of CH molecular absorption in the $B$ band. The severe blending of the spectra by molecular lines affects the photometric results to a significant extent (Yoon et al. 2020). The photometric temperature estimates obtained using the $J-K$ calibration relation are used as an initial guess for selecting model atmospheres to estimate spectroscopic
temperature of the objects in an iterative process as this empirical calibration is independent of metallicity (Alonso et al. 1996, 1999).

## 5. Radial velocities and stellar atmospheric parameters

The radial velocities of the programme stars are determined by measuring the shift in the wavelengths with respect to the laboratory wavelengths, for a large number of unblended and clean lines in their spectra. For the rest frame laboratory wavelength we use the Arcturus spectrum (Hinkle et al. 2000) as a template. The object Arcturus was chosen so as to have homogeneity in the analysis as it belongs to the giant class and has a comparable temperature as the objects under study. Except for HD 145777, the rest are found to be high-velocity objects. Estimated mean radial velocities along with the standard deviation from the mean values, after correcting for heliocentric motion are presented in Table 3. The literature values are also presented for comparison. We also use the FXCOR package in IRAF over the whole spectrum to cross-check these calculations and we find them to be consistent with those obtained from line-to-line measurement of clean lines of different elements.

The stellar atmospheric parameters, the effective temperature $T_{\text {eff }}$, the surface gravity $\log g$, the micro-turbulent velocity $\xi$, and the metallicity $[\mathrm{Fe} / \mathrm{H}]$, are determined using a set of clean unblended Fe I and Fe II lines with excitation potential in the range $0.0-6.0 \mathrm{eV}$ and equivalent width $20-180 \mathrm{~m} \AA$. Due to the presence of molecular lines and bands of carbon all over the spectra, the lines of Fe and other elements are severely blended. After strong filtration for clean, unblended, and symmetrical lines in the spectra of the objects, the number of (Fe I, Fe II) lines used for determination of the atmospheric parameters are ( 33,4 ), $(33,3),(21,3),(27,2)$, and $(19,4)$ for HD 145777, CD-27 14351, HE 0017+0055, HE 2144-1832, and HE 2339-0837, respectively. The lines used are presented in Table 4 along with the measured equivalent widths and atomic line information. References to the $\log g f$ values are given in the last column. A few Fe lines that are not severely blended are also included in the list for which we have used the method of de-blending (with the SPLOT task in IRAF) for measuring equivalent widths.

An initial model atmosphere is selected from the Kurucz grid of model atmospheres with no convective overshooting ${ }^{3}$ corresponding to the photometric temperature estimate and the initial guess of $\log g$ value for giants and/or dwarfs. The effective temperature is determined by forcing the slope of Fe abundances versus the excitation potential of the measured Fe I lines to zero (Fig. 2, top panel). At this particular temperature, the microturbulent velocity is fixed to be that value for which there is no

[^3]Table 2. Temperatures from photometry.
$\left.\begin{array}{lllllllll}\hline \hline \text { Star name } & T_{\text {eff }} & \begin{array}{l}T_{\text {eff }} \\ (-1.5)\end{array} & \begin{array}{l}T_{\text {eff }} \\ (-2.0)\end{array} & \begin{array}{l}T_{\text {eff }} \\ (-2.5)\end{array} & \begin{array}{l}T_{\text {eff }} \\ (-1.5)\end{array} & \begin{array}{l}T_{\text {eff }} \\ (-2.0)\end{array} & \begin{array}{l}T_{\text {eff }} \\ (-2.5)\end{array} & \begin{array}{l}\text { Spectroscopic } \\ \text { estimates }\end{array} \\ & (J-K) & (J-H) & (J-H) & (J-H) & (V-K) \\ (V-K) & (V-K)\end{array}\right]$

Notes. The numbers in parentheses below $T_{\text {eff }}$ indicate the metallicity values at which the temperatures are calculated. Temperatures are given in Kelvin.

Table 3. Radial velocities of the programme stars.

| Star name | $\begin{gathered} V_{\mathrm{r}} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right. \text { ) } \\ \text { (our estimates) } \end{gathered}$ | $\underset{(a)}{V_{\mathrm{r}}}$ |
| :---: | :---: | :---: |
| HD 145777 | $16.23 \pm 0.40$ | $20.14 \pm 0.47$ |
| CD-27 14351 | $61.1 \pm 0.50{ }^{(b)}$ | $59.70 \pm 0.90$ |
| HE 0017+0055 | $-80.56 \pm 0.52$ | $-80.73 \pm 0.23$ |
| HE 2144-1832 | $137.19 \pm 0.68$ | $141.24 \pm 0.64$ |
| HE 2339-0837 | $169.83 \pm 0.68$ | - |

References. ${ }^{(a)}$ Gaia Collaboration (2018); ${ }^{(b)}$ Karinkuzhi et al. (2017).
dependence of the abundances derived from the Fe lines on the reduced equivalent width (Fig. 2, bottom panel). At these fixed values of temperature and micro-turbulent velocity, the surface gravity is obtained by demanding the abundances derived from both Fe I and Fe II lines to be nearly the same. The abundances obtained from the Fe I and Fe II lines give the metallicity. Thus, starting with the initially selected model atmosphere, the final model atmosphere is obtained following the iterative method, which is then adopted to carry out further abundance analysis. The analysis is facilitated by using an updated version of MOOG software (Sneden 1973) in its updated 2013 version, which assumes local thermodynamic equilibrium (LTE) conditions. Solar abundances are adopted from Asplund et al. (2009). The absorption lines due to Fe I are affected by 3D non-LTE (NLTE) effects (Amarsi et al. 2016). The NLTE effect is negligible in the case of Fe II lines for $[\mathrm{Fe} / \mathrm{H}] \geq-2.50$, and increases with decreasing metallicity (Amarsi et al. 2016). However, we do not consider the NLTE corrections in our analysis. Ezzeddine et al. (2017) showed that the departure of $[\mathrm{Fe} / \mathrm{H}]_{\text {NLTE }}$ from $[\mathrm{Fe} / \mathrm{H}]_{\text {LTE }}$ anti-correlate with $[\mathrm{Fe} / \mathrm{H}]_{\text {LTE }}$ growing from $\sim 0.0$ dex at $[\mathrm{Fe} / \mathrm{H}] \sim-1.0$ to $\sim 1.0$ dex at $[\mathrm{Fe} / \mathrm{H}] \sim-8.0$. From Fig. 2 and Eq. (1) of Ezzeddine et al. (2017), we see that the NLTE corrections on the metallicity of our programme stars range from 0.08 to 0.23 , which are well within the uncertainty limit of our $[\mathrm{Fe} / \mathrm{H}]$ estimates. The estimated stellar parameters are listed in Table 5.

## 6. Results

### 6.1. Abundance analysis

The abundances of various elements are determined from the measured equivalent widths of absorption lines due to neutral and ionised elements using the local thermodynamic equilibrium (LTE) analysis. Only the symmetric and clean lines are
used for our analysis. As equivalent width measurement results depend on personal bias, to avoid it we also used the Tool for Automatic Measurement of Equivalent width (TAME)
(Kang \& Lee 2012) to verify our measurements. TAME measures equivalent widths, determining the local continuum and using de-blending wherever necessary. A master line list (Table 6) is generated including all the elements, taking the excitation potential and $\log g f$ values from the Kurucz database of atomic line list and the measured equivalent widths. For our analysis we made use of the LTE line analysis and spectrum synthesis code MOOG $2013^{4}$ (Sneden 1973). The adopted model atmospheres are selected from the Kurucz grid of model atmospheres with no convective overshooting ${ }^{5}$. Elemental abundances of C, N, $\alpha$-elements, iron-peak elements, and several neutron-capture elements are estimated. We used spectrum synthesis calculations for the elements showing hyperfine splitting (e.g. Sc, V, Mn, $\mathrm{Ba}, \mathrm{La}$, and Eu). Several studies (Andrievsky et al. 2009, 2011; Hansen et al. 2013; Tremblay et al. 2013; Gallagher et al. 2016; Sitnova et al. 2016; Nordlander et al. 2017) in the past have focused on the 3D or NLTE or 3D-NLTE effects on the abundances of both heavy and light elements. However, we did not apply any NLTE corrections to our LTE estimates as the NLTE correction factors are negligible. The abundance results are presented in Tables 7 and 8. A comparison of our estimated abundance ratios with the literature values is presented in Table 9. We also estimated the carbon isotopic ratio ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ and calculated $[\mathrm{ls} / \mathrm{Fe}]$, $[\mathrm{hs} / \mathrm{Fe}]$, and $[\mathrm{hs} / \mathrm{ls}]$ for the stars, where 1 s represents $\mathrm{Sr}, \mathrm{Y}$, and Zr and hs represents $\mathrm{Ba}, \mathrm{La}, \mathrm{Ce}$, and Nd . These results are presented in Table 10.

### 6.1.1. Carbon, nitrogen, oxygen

The abundance of oxygen could not be estimated as the oxygen lines are found to be blended and not usable for abundance estimates. The abundance of carbon is estimated using the spectrum synthesis calculation of the $\mathrm{C}_{2}$ molecular bands near 5165 and $5635 \AA$, and the CH molecular band near $4310 \AA$. All three bands yield almost the same abundance of carbon for the respective stars (Tables 7 and 8 ). However, the CH molecular band in the spectrum of HE 2339-0837 could not be used as the band is saturated. Carbon is found to be enhanced ( $[\mathrm{C} / \mathrm{Fe}]>1$ ) in all the stars. Our estimates of carbon abundance are higher than the carbon abundance reported for HE 2144-1832 in Hansen et al. (2016a). This discrepancy may be attributed to the lower resolution $(R \sim 7450)$ of the spectra used in Hansen et al. (2016a),

[^4]Table 4. Equivalent widths (in m $\AA$ ) of Fe lines used to derive atmospheric parameters.

| Wavelength <br> $(\AA)$ | Element | $E_{\text {low }}$ <br> $(\mathrm{eV})$ | $\log g f$ | HD 145777 | CD-27 14351 | HE 0017+0055 | HE 2144-1832 | HE 2339-0837 | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4466.573 | Fe I | 0.11 | -4.464 | - | - | $101.9(5.08)$ | - | - | 1 |
| 4476.019 |  | 2.85 | -0.570 | - | $112.1(4.71)$ | - | - | - | 2 |
| 4871.318 |  | 2.87 | -0.410 | $157.0(5.63)$ | - | - | $152.9(5.67)$ | - | 1 |

Notes. The numbers in parentheses in Cols. 5-9 give the derived abundances from the respective lines. This table is available in its entirety at the CDS. A portion is shown here for guidance regarding its form and content.
References. 1. Fuhr et al. (1988), 2. Bridges \& Kornblith (1974).


Fig. 2. Iron abundances of stars for individual Fe I and Fe II lines as a function of excitation potential (top panel) and equivalent width (bottom panel). The solid red circles indicate Fe I lines and solid blue triangles indicate Fe II lines.
whereas the resolution of our spectrum is $R \sim 60000$. One more reason for the discrepancy could be a difference in the adopted oxygen abundance. Estimates of carbon abundance depend on the adopted initial value of oxygen for the spectrum synthesis calculations. As the abundance of oxygen could not be estimated on our spectrum, we consider a solar value for oxygen $(\log \epsilon=$ 8.69). The spectrum synthesis fits of $\mathrm{C}_{2}$ and CH molecular bands for the stars are shown in Figs. 3, 4, and 5.

The abundance of nitrogen is derived using the spectrum synthesis calculations of the only useful CN band at $4215 \AA$ (Fig. 6) using the estimated carbon abundance. Nitrogen is found to be enhanced in HE $0017+0055$ and CD-27 14351 with $[\mathrm{N} / \mathrm{Fe}]=2.83$ and 1.88 , respectively. HD 145777 and HE 2144-1832 show moderate enhancement with $[\mathrm{N} / \mathrm{Fe}]=0.67$ and 0.50 , respectively. The CN band at $4215 \AA$ is saturated in the spectrum of HE 2339-0837, and hence the abundance of N could not be estimated for this object.

We estimated the carbon isotopic ratio ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ using the spectrum synthesis calculation of the ${ }^{12} \mathrm{CN}$ and ${ }^{13} \mathrm{CN}$ features near $8005 \AA$ (Fig. 7) and the ${ }^{12} \mathrm{C}^{13} \mathrm{C}$ and ${ }^{13} \mathrm{C}^{13} \mathrm{C}$ features near $4740 \AA$ (Fig. 8). The values of ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ derived using these two features are presented in Table 10. We used the wavelengths, lower excitation potentials, and $\log g f$ values of different molecular transitions for the $\mathrm{C}_{2}$ band at $5165 \AA$ and CN bands from Brooke et al. (2013), Ram et al. (2014), and Sneden et al. (2014). The line lists of the $C_{2}$ bands at 5635 and $4740 \AA$, and the CH band at $4310 \AA$ are taken from the linemake ${ }^{6}$ atomic and molecular line database.

### 6.1.2. $\mathrm{Na}, \mathrm{Mg}, \mathrm{Ca}, \mathrm{Sc}, \mathrm{Ti}, \mathrm{V}$

While HD 145777 and HE 2144-1832 show moderate enhancement in Na with $[\mathrm{Na} / \mathrm{Fe}]=0.45$ and 0.53 , respectively, HE 2339-0837 and CD-27 14351 exhibit enhanced abundance of Na with $[\mathrm{Na} / \mathrm{Fe}]>1$. Na abundance could not be estimated for HE $0017+0055$ as the Na lines are severely blended and not usable for abundance estimates.

Magnesium and calcium are also found to be moderately enhanced in the stars HD 145777 and HE 2144-1832. While HE 2339-0837 and CD-27 14351 show enhanced abundance of Mg with $[\mathrm{Mg} / \mathrm{Fe}]>1, \mathrm{Ca}$ is found to be moderately enhanced with $[\mathrm{Ca} / \mathrm{Fe}]$ in the range $0.4-0.9$. We could not determine the abundance of Mg and Ca for $\mathrm{HE} \mathrm{0017+0055}$ as no good lines were found.

We could estimate Sc abundance only for HD 145777 using spectrum synthesis calculations of the line Sc II 6245.637 Å considering the hyperfine splitting contributions from Prochaska \& McWilliam (2000). This object shows mild enhancement of Sc with $[\mathrm{Sc} / \mathrm{Fe}]=0.77$.

Titanium is estimated using lines from both neutral and ionised species for all the programme stars except HE 23390837, where Ti abundance is estimated only using Ti II lines.

[^5]P. P. Goswami et al.: Spectroscopic study of CEMP-(s \& r/s) stars

Table 5. Derived atmospheric parameters of our programme stars and literature values.

| Star name | $T_{\text {eff }}$ <br> $(\mathrm{K})$ | $\log g$ <br> $(\mathrm{cgs})$ | $\zeta$ <br> $\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | $[\mathrm{Fe} \mathrm{I/H}]$ | $[\mathrm{Fe} \mathrm{II} / \mathrm{H}]$ | $[\mathrm{Fe} / \mathrm{H}]$ | Ref. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HD 145777 | 4160 | 0.90 | 2.02 | $-2.17 \pm 0.18$ | $-2.17 \pm 0.25$ | -2.17 | 1 |
|  | 4245 | - | - | - | - | - | 2 |
|  | 4216 | - | - | - | - | - | 7 |
| CD-271 4351 | 4320 | 0.50 | 2.58 | $-2.72 \pm 0.16$ | $-2.69 \pm 0.07$ | -2.71 | 1 |
|  | 4335 | 0.50 | 2.42 | - | - | -2.62 | 5 |
|  | 4223 | - | - | - | - | - | 7 |
| HE 0017+0055 | 4370 | 0.80 | 1.94 | $-2.47 \pm 0.12$ | $-2.45 \pm 0.03$ | -2.46 | 1 |
|  | 4250 | 1.00 | 2.00 | - | - | -2.40 | 4 |
|  | 4185 | 0.18 | 2.00 | - | - | -2.72 | 6 |
| HE 2144-1832 | 4190 | 0.60 | 1.87 | $-1.63 \pm 0.15$ | $-1.63 \pm 0.00$ | -1.63 | 1 |
|  | 4200 | 0.60 | 2.20 | - | - | -1.70 | 3 |
| HE 2339-0837 | 4940 | 1.40 | 1.55 | $-2.74 \pm 0.08$ | $-2.74 \pm 0.08$ | -2.74 | 1 |
|  | 4939 | 1.60 | 2.00 | - | - | -2.71 | 6 |

References. 1. Our work, 2. Bergeat et al. (2001), 3. Hansen et al. (2016a), 4. Jorissen et al. (2016a), 5. Karinkuzhi et al. (2017), 6. Kennedy et al. (2011), 7. McDonald et al. (2012).

Table 6. Equivalent widths (in $m \AA$ ) of lines used to calculate elemental abundances.

| Wavelength <br> $(\AA)$ |  | Element | $E_{\text {low }}$ | $\log g f$ | HD 145777 | CD-27 14351 | HE 0017+0055 | HE 2144-1832 | HE 2339-0837 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | Reference

Notes. The numbers in parentheses in Cols. 5-9 give the derived abundances from the respective lines. This table is available in its entirety at the CDS. A portion is shown here for guidance regarding its form and content.
References. 1. Kurucz \& Peytremann (1975), 2. Laughlin \& Victor (1974), 3. Lincke \& Ziegenbein (1971).

While Ti is found to be mildly enhanced in HD 145777, HE 2144-1832, HE 0017+0055, and HE 2339-0837, the object CD-27 14351 shows an overabundance with $[\mathrm{Ti} / \mathrm{Fe}] \sim 0.96$. Although it is seen that due to NLTE effects, the abundances derived from Ti I and Ti II lines may differ (Johnson 2002), we have derived similar abundances from Ti I and Ti II lines for our programme stars. The equal abundances found from Ti I and Ti II lines ensure the $\log g$ values estimated for our programme stars.

The abundances of V are found to be near solar with [V/Fe] ~ -0.11 and 0.06 for HD 145777 and HE 2144-1832, respectively. V is highly abundant in CD-27 14351 with $[\mathrm{V} / \mathrm{Fe}]=1.11$. For HE 0017+0055 and HE 2339-0837 abundance of V could not be estimated.

### 6.1.3. $\mathrm{Cr}, \mathrm{Mn}, \mathrm{Co}, \mathrm{Ni}, \mathrm{Zn}$

The abundance of Cr is derived using seven Cr I lines (Table 6). Cr is underabundant with $[\mathrm{Cr} / \mathrm{Fe}]=-0.21,-0.12,-0.50$, and -0.34 for HD 145777, HE 2144-1832, HE 0017+0055, and HE 2339-0837, respectively. CD-27 14351 shows near solar abundance of Cr .

The abundance of Mn is estimated using spectrum synthesis calculations of the Mn I lines at $4765.846 \AA$ and $4766.418 \AA$ for HE $2144-1832$, and the Mn II $5432.543 \AA$ line is used
for HD 145777. Mn is found to be underabundant in the stars HD 145777 and HE 2144-1832. The abundance of Mn could not be estimated for the other three objects as no suitable lines were detected for abundance determination.

The abundance of Co could be derived only for HD 145777 and HE 2144-1832, for which we obtained near solar values with $[\mathrm{Co} / \mathrm{Fe}]=0.03$ and 0.06 , respectively. The abundance of Co could not be estimated for the other three objects as no good lines were found for abundance estimation.

The abundance of Ni could be estimated only for HE 2144-1832 using equivalent width measurement of five Ni I lines (Table 6). Ni shows moderate enhancement in the star with $[\mathrm{Ni} / \mathrm{Fe}]=0.41$. The abundance of Ni could not be estimated for the other objects as no good lines were found.

The abundance of Zn determined using Zn I 4810.528 Å line gives $[\mathrm{Zn} / \mathrm{Fe}]=0.63,-0.08$, and 0.52 for the stars HD 145777, HE 2144-1832, and HE 0017+0055, respectively. The abundance of Zn could not be estimated for the other two objects as no suitable lines were detected for abundance determination.

### 6.1.4. Sr, Y, Zr

The abundance of Sr is estimated using spectrum synthesis calculations of the Sr I $4607.327 \AA$ line for all the stars except


Fig. 3. Spectral synthesis plot of $C_{2}$ band around $5165 \AA$. The dotted lines indicate the synthesised spectra and the solid lines indicate the observed spectra. Two alternative synthetic spectra are shown corresponding to $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.01$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.01$ (short-dashed line) in panel 1 (for HD 145777); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.05$ (longdashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.05$ (short-dashed line) in panel 2 (for HE 2144-1832); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.10$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=$ -0.10 (short-dashed line) in panel 3 (for HE 0017+0055); $\Delta[\mathrm{C} / \mathrm{Fe}]$ $=+0.3$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.3$ (short-dashed line) in panel 4 (for HE 2339-0837); and $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.01$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.01$ (short-dashed line) in panel 5 (for $\mathrm{CD}-27$ 14351).


Fig. 4. Spectral synthesis plot of $C_{2}$ band around $5635 \AA$. The dotted lines indicate the synthesised spectra and the solid lines indicate the observed spectra. Two alternative synthetic spectra are shown corresponding to $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.02$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.02$ (short-dashed line) in panel 1 (for HD 145777); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.15$ (longdashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.15$ (short-dashed line) in panel 2 (for HE 2144-1832); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.05$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=$ -0.05 (short-dashed line) in panel 3 (for $\mathrm{HE} 0017+0055$ ); $\Delta[\mathrm{C} / \mathrm{Fe}]$ $=+0.3$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.3$ (short-dashed line) in panel 4 (for HE 2339-0837); and $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.03$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.03$ (short-dashed line) in panel 5 (for $\mathrm{CD}-27$ 14351).

HE 0017+0055 as this line is severely blended. While HD 145777 and HE 2144-1832 show moderate enhancement of Sr , it is found to be overabundant with $[\mathrm{Sr} / \mathrm{Fe}]=1.32$ and 1.74 in HE 2339-0837 and CD-27 14351, respectively. The estimated


Fig. 5. Spectral synthesis plot of CH band around $4310 \AA$. The dotted lines indicate the synthesised spectra and the solid lines indicate the observed spectra. Two alternative synthetic spectra are shown corresponding to $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.05$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.05$ (short-dashed line) in panel 1 (for HD 145777); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.15$ (longdashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.15$ (short-dashed line) in panel 2 (for HE 2144-1832); $\Delta[\mathrm{C} / \mathrm{Fe}]=+0.30$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=$ -0.30 (short-dashed line) in panel 3 (for HE 0017+0055); and $\Delta[\mathrm{C} / \mathrm{Fe}]$ $=+0.10$ (long-dashed line) and $\Delta[\mathrm{C} / \mathrm{Fe}]=-0.10$ (short-dashed line) in panel 4 (for CD-27 14351).


Fig. 6. Synthesis of CN band around $4215 \AA$. The dotted line represents synthesised spectra and the solid line indicates the observed spectra. Two alternative fits, the short-dashed line corresponding to $\Delta[\mathrm{N} / \mathrm{Fe}]=$ -0.3 and the long-dashed line corresponding to $\Delta[\mathrm{N} / \mathrm{Fe}]=+0.3$ are shown to illustrate the sensitivity of the line strengths to N abundance.

Sr abundance is found to be $\sim 0.8$ dex lower than that obtained by Hansen et al. (2016a) for the star HE 2144-1832 (Table 9), which they had obtained using the Sr II $4077.709 \AA$ ine on a spectrum of spectral resolution $R \sim 7450$, and $S / N=6$ (at $4000 \AA$ ). This line is severely blended in our spectrum, which was obtained at a higher resolution ( $R \sim 60000$ ), and it could not be used for abundance analysis. The abundance estimated from the blended Sr II


Fig. 7. Spectral synthesis fits (dotted curves) of the CN features around $8005 \AA$ obtained with the adopted C and N abundances and ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ values (dotted curve). The observed spectrum is shown by a solid curve. Two alternative fits with ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C} \sim 1$ (short-dashed line) and 12 (longdashed line) are shown to illustrate the sensitivity of the line strengths to the isotopic carbon abundance ratios.


Fig. 8. Spectral synthesis fits (dotted curves) of the $\mathrm{C}_{2}$ features around $4740 \AA$ obtained with the adopted C abundances and ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ values (dotted curve). The observed spectrum is shown by a solid curve. Two alternative fits with ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C} \sim 1$ (short-dashed line) and 15 (long-dashed line) are shown to illustrate the sensitivity of the line strengths to the isotopic carbon abundance ratios.
line in Hansen et al. (2016a) may be the reason for the observed discrepancy.

We estimated the abundance of Y using six lines (Table 6). HE $0017+0055$ and HE 2339-0837 show mild overabundance with $[\mathrm{Y} / \mathrm{Fe}] \sim 0.58$ and 0.67 , respectively. The other three objects show overabundance of Y with $[\mathrm{Y} / \mathrm{Fe}]>1$.

Four Zr I lines and four Zr II lines (Table 6) are used to derive Zr abundance in the objects. Based on the availability, ZrI lines are used for HD 145777 and HE 2144-1832, and Zr II lines are used for HE 0017+0055 and HE 2339-0837. For the
object CD-27 14351, both Zr I and Zr II lines could be used. Zr is found to be enhanced in all five stars.

We could not detect lines due to niobium ( Nb ) and technetium ( Tc ) in any of the spectra.

### 6.1.5. Ba, La, Ce, Pr, Nd

The abundance of Ba is derived using spectrum synthesis calculations of Ba II $5853.668 \AA$ A line for all five stars. Spectrum synthesis calculation of Ba II $6141.713 \AA$ is also used to find the Ba abundance for HD 145777, HE 2339-0837, and CD-27 14351 (Fig. 9). Both the lines gave similar abundance for the stars with the highest standard deviation of 0.15 for HE 2339-0837. The Ba II $6141.713 \AA$ line could not be used to determine the abundance of Ba for the other two stars as the line is heavily blended in these two stars. The other two frequently used lines Ba II $4554.029 \AA$ and Ba II $4934.076 \AA$ are found to be severely blended in the spectra of the programme stars, and hence could not be used for abundance analysis. Hyperfine splitting contributions of the two lines used in the analysis are taken from McWilliam (1998). Ba is enhanced in all the stars with $1.27 \leq$ $[\mathrm{Ba} / \mathrm{Fe}] \leq 2.30$.

The abundance of La is estimated using the spectrum synthesis calculation of La II $4921.776 \AA$ and found to be overabundant in all five stars with $1.37 \leq[\mathrm{La} / \mathrm{Fe}] \leq 2.46$. La II $4808.996 \AA$ line is also used for HE 0017+0055. Hyperfine splitting contributions of La II $4921.776 \AA$ Å line are taken from Jonsell et al. (2006).

The abundance of $\mathrm{Ce}, \mathrm{Pr}$, and Nd are estimated using the equivalent width measurement technique. Twelve Ce II lines, 3 Pr II lines, and 13 Nd II lines (Table 6) are examined to derive the abundance of $\mathrm{Ce}, \mathrm{Pr}$, and Nd . Ce is found to be overabundant in all five stars. For the object CD-27 14351 we find a much lower value $([\mathrm{Ce} / \mathrm{Fe}]=1.89)$ than the $\sim 2.63$ found by Karinkuzhi et al. (2017). Karinkuzhi et al. (2017) used two lines Ce II 4460.207 and $4527.348 \AA$ for Ce abundance estimate. We used three lines Ce II 4460.207, 4483.893, and 5187.458 A. For the line Ce II $4460.207 \AA$, which is common in both the studies, our measured equivalent width is $\sim 160 \mathrm{~m} \AA$, about $14 \mathrm{~m} \AA$ higher than in Karinkuzhi et al. (2017). This line, however, returned an abundance value that is $\sim 0.7$ dex lower. In order to check whether the difference in abundance is due to the adopted model atmosphere, we calculated the abundance of Ce using the measured equivalent width ( $\sim 146 \mathrm{~mA}$ ) of this line by Karinkuzhi et al. (2017) and also the model atmosphere adopted by them. The derived abundance is found to be $[\mathrm{Ce} / \mathrm{Fe}]=1.72$, which is closer to our estimated value. The other line, Ce II 4527.348 Å, used in their study is found to be severely blended in our spectrum.

Praseodymium ( Pr ) is found to be overabundant in all the stars with $1.67 \leq[\mathrm{Pr} / \mathrm{Fe}] \leq 2.42$. Neodymium $(\mathrm{Nd})$ is also found to be enhanced in all the stars with $1.37 \leq[\mathrm{Nd} / \mathrm{Fe}] \leq 2.55$.

### 6.1.6. Sm, Eu

The abundance of Sm is derived using six Sm II lines (Table 6). No Sm lines could be found for CD-27 14351, hence Sm abundance could not be estimated for this object. The other four objects show enhanced abundance of Sm.

The abundance of Eu is derived using the spectrum synthesis calculation of the Eu II 6645.064 Å line (Fig. 10) considering hyperfine splitting contributions from Worley et al. (2013). The other frequently used lines, Eu II $4129.725 \AA$ A., $4205.042 \AA$ A, and $6437.640 \AA$, are severely blended, and hence could not be used for abundance analysis. Eu shows overabundance with $0.80 \leq$



Fig. 9. Spectral synthesis of Ba II 5853 and $6141 \AA$ lines. Dotted line represents synthesised spectra and the solid line indicates the observed spectra. Two alternative fits, short dashed line corresponding to $\Delta[\mathrm{BaII} / \mathrm{Fe}]=-0.3$ and long dashed line corresponding to $\Delta[\mathrm{Ba} I \mathrm{II} / \mathrm{Fe}]=+0.3$ are shown to illustrate the sensitivity of line strength to Ba abundance.


Fig. 10. Synthesis of Eu II $6645 \AA$ line. Dotted line represents synthesised spectra and the solid line indicates the observed spectra. Two alternative fits, short dashed line corresponding to $\Delta[\mathrm{Eu} \mathrm{II} / \mathrm{Fe}]=-0.3$ and long dashed line corresponding to $\Delta[\mathrm{Eu} \mathrm{II} / \mathrm{Fe}]=+0.3$ are shown to illustrate the sensitivity of line strength to Eu abundance.
$[\mathrm{Eu} / \mathrm{Fe}] \leq 2.14$, except in CD-27 14351, for which we could estimate an upper limit with $[\mathrm{Eu} / \mathrm{Fe}] \sim 0.39$. As shown in Fig. 10, the Eu II $6645.064 \AA$ A line is blended with two CN lines. It can be clearly seen that the Eu II $6645.064 \AA$ line is absent in the spectrum of the object CD-27 14351; a misidentification of the CN line at $6644.750 \AA$ as the Eu II $6645.064 \AA$ ine could result in a much higher abundance of Eu; this may explain the very high abundance recorded for Eu by Karinkuzhi et al. (2017).

### 6.2. Abundance uncertainties

Two components contribute to the total uncertainties on elemental abundances: random error and systematic error. In order to
derive the uncertainties on the elemental abundances, we followed the procedure mentioned in Shejeelammal et al. (2020). We estimated the total uncertainties on $\log \epsilon$ using the equation

$$
\begin{align*}
\sigma_{\log \epsilon}^{2}= & \sigma_{\text {ran }}^{2}+\left(\frac{\delta \log \epsilon}{\delta T}\right)^{2} \sigma_{T_{\mathrm{eff}}}^{2}+\left(\frac{\delta \log \epsilon}{\delta \log g}\right)^{2} \sigma_{\log g}^{2}  \tag{1}\\
& +\left(\frac{\delta \log \epsilon}{\delta \zeta}\right)^{2} \sigma_{\zeta}^{2}+\left(\frac{\delta \log \epsilon}{\delta[\mathrm{Fe} / \mathrm{H}]}\right)^{2} \sigma_{[\mathrm{Fe} / \mathrm{H}]}^{2}
\end{align*}
$$

where $\sigma_{\text {ran }}$ is the random error that arises due to the uncertainties on the factors like equivalent width measurement, oscillator strength, and line blending. We adopted $\sigma_{\text {ran }}=\frac{\sigma_{\mathrm{s}}}{\sqrt{N}}$, where $\sigma_{\mathrm{s}}$ is the standard deviation of the abundance of a particular species estimated using N number of lines of that species.

The typical uncertainties on the stellar atmospheric parameters $T_{\text {eff }}, \log g, \zeta$, and $[\mathrm{Fe} / \mathrm{H}]$ are denoted $\sigma_{T_{\text {eff }}}, \sigma_{\log g}, \sigma_{\zeta}$, and $\sigma_{[\mathrm{Fe} / \mathrm{H}]}$, respectively. We evaluated the partial derivatives appearing in Eq. (1) for the star HE 2144-1832, varying the stellar parameters $T_{\text {eff }}, \log g, \zeta$, and $[\mathrm{Fe} / \mathrm{H}]$ by $\pm 100 \mathrm{~K}, \pm 0.2$ dex, $\pm 0.2 \mathrm{~km} \mathrm{~s}^{-1}$, and $\pm 0.2$ dex, respectively. Finally, the uncertainties on $[\mathrm{X} / \mathrm{Fe}]$ are derived as
$\sigma_{[\mathrm{X} / \mathrm{Fe}]}^{2}=\sigma_{\mathrm{X}}^{2}+\sigma_{[\mathrm{Fe} / \mathrm{H}]}^{2}$.
The resulting differential abundances and the derived uncertainties on $[\mathrm{X} / \mathrm{Fe}]$ are presented in Table A.1. We note that the calculated uncertainties on $[\mathrm{X} / \mathrm{Fe}]$ are overestimated because of the assumption of the uncorrelated nature of the uncertainties arising from the different stellar parameters in Eq. (1).

## 7. Kinematic analysis

Along with the physical parameters and composition it is also important to know the group of Galactic populations to which the programme stars belong. To determine this we calculated the space velocity for the stars using the method of Johnson \& Soderblom (1987). Using the method given by Bensby et al. (2003) and information such as parallax ( $\pi$ ) and proper motion $\left(\mu_{\alpha}, \mu_{\delta}\right)$ from the Gaia and SIMBAD databases

Table 7. Elemental abundances in HD 145777, CD-27 14351, and HE 0017+0055.

|  | HD 145777 |  |  |  |  |  | CD-27 14351 |  | HE 0017+0055 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Element | Z | solar $\log \epsilon^{(a)}$ | $\log \epsilon$ <br> (dex) | [X/H] | [X/Fe] | $\log \epsilon$ <br> (dex) | [X/H] | [X/Fe] | $\log \epsilon$ <br> (dex) | [ $\mathrm{X} / \mathrm{H}$ ] | [X/Fe] |
| $\mathrm{C}\left(\mathrm{C}_{2}, 5165 \AA\right)$ | 6 | 8.43 | 8.69 (syn) | 0.26 | 2.43 | 8.70 (syn) | 0.27 | 2.98 | 8.70 (syn) | 0.27 | 2.73 |
| $\mathrm{C}\left(\mathrm{C}_{2}, 5635 \AA\right)$ | 6 | 8.43 | 8.69 (syn) | 0.26 | 2.43 | 8.70 (syn) | 0.27 | 2.98 | 8.71 (syn) | 0.28 | 2.74 |
| $\mathrm{C}(\mathrm{CH}, 4310$ A $)$ | 6 | 8.43 | 8.67 (syn) | 0.24 | 2.41 | 8.70 (syn) | 0.27 | 2.98 | 8.73 (syn) | 0.30 | 2.76 |
| N (CN, 4215 A) | 7 | 7.83 | 6.33 (syn) | -1.50 | 0.67 | 7.00 (syn) | -0.83 | 1.88 | 8.20 (syn) | 0.37 | 2.83 |
| Na I | 11 | 6.24 | $4.52 \pm 0.12$ (2) | -1.72 | 0.45 | $4.91 \pm 0.20$ (2) | -1.33 | 1.38 | - | - | - |
| Mg I | 12 | 7.60 | $6.25 \pm 0.23$ (2) | -1.35 | 0.82 | 6.70 (1) | -0.90 | 1.81 | - | - | - |
| Ca I | 20 | 6.34 | $4.66 \pm 0.21$ (9) | -1.68 | 0.49 | $4.54 \pm 0.20$ (5) | -1.80 | 0.91 | - | - | - |
| Sc II | 21 | 3.15 | 1.75 (syn) | -1.40 | 0.77 | - | - | - | - | - | - |
| Ti I | 22 | 4.95 | $3.44 \pm 0.17$ (2) | -1.51 | 0.66 | $3.19 \pm 0.20$ (3) | -1.76 | 0.95 | 3.13 (1) | -1.82 | 0.64 |
| Ti II | 22 | 4.95 | $3.43 \pm 0.08$ (5) | -1.52 | 0.65 | $3.20 \pm 0.13$ (5) | -1.75 | 0.96 | $3.14 \pm 0.05$ (3) | -1.81 | 0.65 |
| V I | 23 | 3.93 | 1.65 (syn) | -2.28 | -0.11 | 2.33 (syn) | -1.60 | 1.11 | - | - | - |
| Cr I | 24 | 5.64 | $3.26 \pm 0.13$ (6) | -2.38 | -0.21 | $3.11 \pm 0.18$ (3) | -2.53 | 0.18 | 2.68 (1) | -2.96 | -0.50 |
| Mn I | 25 | 5.43 | - | - | - | - | - | - | - | - | - |
| Mn II | 25 | 5.43 | 2.45 (syn) | -2.98 | -0.81 | - | - | - | - | - | - |
| Fe I | 26 | 7.50 | $5.33 \pm 0.18$ (33) | -2.17 | - | $4.78 \pm 0.16$ (33) | -2.72 | - | $5.03 \pm 0.12$ (21) | -2.47 | - |
| Fe II | 26 | 7.50 | $5.33 \pm 0.25$ (4) | -2.17 | - | $4.81 \pm 0.07$ (3) | -2.69 | - | $5.05 \pm 0.03$ (3) | -2.45 | - |
| Co I | 27 | 4.99 | 2.85 (1) | -2.14 | 0.03 | - | - | - | - | - | - |
| Ni I | 28 | 6.22 | - | - | - | - | - | - | - | - | - |
| Zn I | 30 | 4.56 | 3.02 (1) | -1.54 | 0.63 | - | - | - | 2.62 (1) | -1.94 | 0.52 |
| Sr I | 38 | 2.87 | 1.37 (syn) | -1.50 | 0.67 | 1.90 (syn) | -0.97 | 1.74 | - | - | - |
| Y II | 39 | 2.21 | $1.26 \pm 0.02$ (2) | -0.95 | 1.22 | $1.47 \pm 0.10$ (3) | -0.74 | 1.97 | $0.33 \pm 0.08$ (3) | -1.88 | 0.58 |
| Zr I | 40 | 2.58 | $1.46 \pm 0.14$ (2) | -1.12 | 1.05 | 2.07 (1) | -0.51 | 2.20 | - | - | - |
| Zr II | 40 | 2.58 | - | - | - | 2.09 (1) | -0.49 | 2.22 | $1.67 \pm 0.20$ (3) | -0.91 | 1.55 |
| Ba II | 56 | 2.18 | 1.28 (syn) $\pm 0.03$ | -0.90 | 1.27 | 1.29 (syn) $\pm 0.09$ | -0.89 | 1.82 | 2.02 (syn) | -0.16 | 2.30 |
| La II | 57 | 1.10 | 0.30 (syn) | -0.80 | 1.37 | -0.05 (syn) | -1.15 | 1.56 | 1.10 (syn) $\pm 0.20$ | 0.0 | 2.46 |
| Ce II | 58 | 1.58 | $1.20 \pm 0.09$ (5) | -0.38 | 1.79 | $0.76 \pm 0.16$ (3) | -0.82 | 1.89 | $1.23 \pm 0.06$ (2) | -0.35 | 2.11 |
| Pr II | 59 | 0.72 | $0.22 \pm 0.00$ (2) | -0.50 | 1.67 | -0.03 (1) | -0.75 | 1.96 | 0.68 (1) | -0.04 | 2.42 |
| Nd II | 60 | 1.42 | $0.73 \pm 0.18$ (5) | -0.69 | 1.48 | $0.08 \pm 0.16$ (6) | -1.34 | 1.37 | $1.21 \pm 0.11$ (4) | -0.21 | 2.25 |
| Sm II | 62 | 0.96 | $0.42 \pm 0.03$ (2) | -0.54 | 1.63 | - | - | - | $0.48 \pm 0.04$ (2) | -0.48 | 1.98 |
| Eu II | 63 | 0.52 | -0.85 (syn) | -1.37 | 0.80 | $<-1.80$ (syn) | $<-2.32$ | $<0.39$ | 0.20 (syn) | -0.32 | 2.14 |

Notes. The numbers in parentheses in Cols. 4, 7, and 10 show the number of lines used for the abundance determination.
References. ${ }^{(a)}$ Asplund et al. (2009).
(Gaia Collaboration 2018) and radial velocity ( $V_{\mathrm{r}}$ ) from our estimates, we calculated the components of space velocity with respect to Local Standard of Rest (LSR) using the relation

$$
\begin{equation*}
(\boldsymbol{U}, \boldsymbol{V}, \boldsymbol{W})_{\mathrm{LSR}}=(\boldsymbol{U}, \boldsymbol{V}, \boldsymbol{W})+(\boldsymbol{U}, \boldsymbol{V}, \boldsymbol{W})_{\odot} \mathrm{km} \mathrm{~s}^{-1} . \tag{3}
\end{equation*}
$$

Here $\boldsymbol{U}, \boldsymbol{V}$, and $\boldsymbol{W}$ are the velocity vectors pointing towards the Galactic centre, the direction of Galactic rotation, and the Galactic north pole, respectively. The solar $\boldsymbol{U}, \boldsymbol{V}, \boldsymbol{W}$ component velocities (11.1, 12.2, 7.3) $\mathrm{km} \mathrm{s}^{-1}$ are taken from Schönrich et al. (2010). The total spatial velocity ( $V_{\text {spa }}$ ) is given by
$V_{\mathrm{spa}}=\sqrt{U_{\mathrm{LSR}}^{2}+V_{\mathrm{LSR}}^{2}+W_{\mathrm{LSR}}^{2}}$.
The detailed description of the calculations can be found in Purandardas et al. (2019). The estimated components of spatial velocity and the total spatial velocity are presented in Table 11. Following the procedures of Reddy et al. (2006), Bensby et al. (2003, 2004), and Mishenina et al. (2004), we calculated the probability that the stars are member of the thin disc, the thick disc, or the halo population. The estimated metallicity and spatial velocities indicate that three stars are members of the thick disc population. The probability estimates for them being members of the thick disc population are $0.83,0.84$, and 0.65 for HD 145777,

HE 2144-1832, and HE 0017-0055, respectively. The probability estimates are 0.9 and 1.0 that the objects HE 2339-0837 and CD-27 14351, respectively, are members of the halo population (Table 11).

## 8. Discussion

We begin with a brief discussion on the formation scenarios of CEMP-s and CEMP-r/s stars from the literature, in the context of the stars in this study.

### 8.1. Formation scenarios of CEMP-(s \& r/s) stars and their likelihoods

As discussed in Sect. 1, the widely accepted scenario to explain the enhancement of heavy elements exhibited by CEMP-s stars is that these objects are in binary systems with a now invisible white dwarf companions (as shown in Fig. 11a). The observed enhancement of heavy elements in CD-27 14351 may be attributed to a binary companion in such a binary system. Various proposed formation scenarios that attempt to explain the unusual elemental abundance pattern of the CEMP-r/s stars are available in the literature. Jonsell et al. (2006) discussed nine scenarios explaining their origin, and concluded that none of the

Table 8. Elemental abundances in HE 2144-1832 and HE 2339-0837.

|  |  | HE 2144-1832 |  |  |  |  | HE 2339-0837 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Element | Z | solar $\log \epsilon^{(a)}$ | $\log \epsilon$ <br> (dex) | [X/H] | [X/Fe] | $\log \epsilon$ <br> (dex) | [ $\mathrm{X} / \mathrm{H}$ ] | [X/Fe] |
| $\mathrm{C}\left(\mathrm{C}_{2}, 5165\right.$ A $)$ | 6 | 8.43 | 8.65 (syn) | 0.22 | 1.85 | 8.73 (syn) | 0.30 | 3.04 |
| $\mathrm{C}\left(\mathrm{C}_{2}, 5635 \AA\right.$ ) | 6 | 8.43 | 8.60 (syn) | 0.17 | 1.80 | 8.50 (syn) | 0.07 | 2.81 |
| C ( $\mathrm{CH}, 4310$ A ) | 6 | 8.43 | 8.55 (syn) | 0.12 | 1.75 | - | - | - |
| $\mathrm{N}(\mathrm{CN}, 4215 \AA)$ | 7 | 7.83 | 6.70 (syn) | -1.13 | 0.50 | - | - | - |
| Na I | 11 | 6.24 | $5.14 \pm 0.08$ (3) | -1.10 | 0.53 | $5.04 \pm 0.03$ (2) | -1.20 | 1.54 |
| Mg I | 12 | 7.60 | $6.64 \pm 0.11$ (2) | -0.96 | 0.67 | 7.03 (1) | -0.57 | 2.17 |
| Ca I | 20 | 6.34 | $5.11 \pm 0.17$ (8) | -1.23 | 0.40 | $4.09 \pm 0.14$ (4) | -2.25 | 0.49 |
| Ti I | 22 | 4.95 | $3.53 \pm 0.13$ (6) | -1.42 | 0.21 | $-\quad$ | - | - |
| Ti II | 22 | 4.95 | $3.51 \pm 0.05$ (3) | -1.44 | 0.19 | $2.62 \pm 0.15$ (4) | -2.33 | 0.41 |
| V I | 23 | 3.93 | 2.36 (syn) | -1.57 | 0.06 | - | - | - |
| Cr I | 24 | 5.64 | $3.89 \pm 0.18$ (4) | -1.75 | -0.12 | 2.56 (1) | -3.08 | -0.34 |
| Mn I | 25 | 5.43 | 3.20 (syn) $\pm 0.0$ | -2.23 | -0.60 | - | - | - |
| $\mathrm{Fe}_{\mathrm{I}}$ | 26 | 7.50 | $5.87 \pm 0.15$ (27) | -1.63 | - | $4.76 \pm 0.08$ (19) | -2.74 | - |
| Fe II | 26 | 7.50 | $5.87 \pm 0.00$ (2) | -1.63 | - | $4.76 \pm 0.08$ (4) | -2.74 | - |
| Co I | 27 | 4.99 | $3.42 \pm 0.03$ (3) | -1.57 | 0.06 | - | - | - |
| Ni I | 28 | 6.22 | $5.00 \pm 0.16$ (5) | -1.22 | 0.41 | - | - | - |
| Zn I | 30 | 4.56 | 2.85 (1) | -1.71 | -0.08 | - | - | - |
| Sr I | 38 | 2.87 | 1.90 (syn) | -0.97 | 0.66 | 1.45 (syn) | -1.42 | 1.32 |
| Y II | 39 | 2.21 | $1.74 \pm 0.08$ (3) | -0.47 | 1.16 | $0.14 \pm 0.10$ (3) | -2.07 | 0.67 |
| Zr I | 40 | 2.58 | $1.92 \pm 0.18$ (3) | -0.66 | 0.97 | - | - | - |
| Zr II | 40 | 2.58 | - | - | - | 1.48 (1) | -1.10 | 1.64 |
| Ba II | 56 | 2.18 | 2.04 (syn) | -0.14 | 1.49 | 1.65 (syn) $\pm 0.15$ | -0.53 | 2.21 |
| La II | 57 | 1.10 | 1.00 (syn) | -0.10 | 1.53 | 0.60 (syn) | -0.50 | 2.24 |
| Ce II | 58 | 1.58 | $1.65 \pm 0.17$ (6) | 0.07 | 1.70 | $1.21 \pm 0.13$ (3) | -0.37 | 2.37 |
| Pr II | 59 | 0.72 | $0.81 \pm 0.17$ (3) | 0.09 | 1.72 | $0.24 \pm 0.22$ (2) | -0.48 | 2.26 |
| Nd II | 60 | 1.42 | $1.40 \pm 0.17$ (7) | -0.02 | 1.61 | $1.23 \pm 0.10$ (5) | -0.19 | 2.55 |
| Sm II | 62 | 0.96 | $1.11 \pm 0.21$ (3) | 0.15 | 1.78 | $0.51 \pm 0.14$ (3) | -0.45 | 2.29 |
| Eu II | 63 | 0.52 | -0.10 (syn) | -0.62 | 1.01 | -0.38 (syn) | -0.90 | 1.84 |

Notes. The numbers in parentheses in Cols. 4 and 7 show the number of lines used for the abundance determination.
References. ${ }^{(a)}$ Asplund et al. (2009).
explanations was satisfactory. Lugaro et al. (2009) also discussed a few formation scenarios of this class of stars. In search of the most plausible formation mechanism, Abate et al. (2016) calculated the frequency of CEMP-r/s stars among CEMP-s stars, considering different formation scenarios discussed by Jonsell et al. (2006) and Lugaro et al. (2009), and compared that with the frequency of an observed sample of CEMP-r/s stars taken from the literature. A pictoral representation of some of these scenarios relevant to the present study is presented in Fig. 11.

### 8.1.1. Radiative levitation

This scenario is based on the fact that due to the large photon absorption cross sections of partially ionised heavy elements, they can be pushed outwards by radiative pressure that causes the abundances of heavy elements in the atmospheres of hot stars (e.g. Przybylski's star) to appear much higher than the solar abundances. The observed abundance peculiarities of CEMP-r/s stars could also be thought of as a consequence of radiative levitation. However, as discussed in Cohen et al. (2003), Jonsell et al. (2006), and Abate et al. (2016), this scenario is rejected as a formation mechanism of CEMP-r/s stars. Richard et al. (2002) and Matrozis \& Stancliffe (2016) have found from their simulations that radiative levitation is most effective in stars on the main sequence, and especially when they approach the turn-off as they have very thin convective envelopes. CEMP (-s \& -r/s) stars
are generally observed to be subgiants or giants and the effect of radiative levitation is found to be negligible in giants and low-temperature objects. All four objects that we have found to be enhanced in both $s$ - and $r$-process elements are lowtemperature ( $4160-4940 \mathrm{~K}$ ) objects with $\log g$ values in the range $0.6-1.40$ cgs units. Radiative levitation thus cannot be a process responsible for the observed overabundance of heavy elements in these stars.

### 8.1.2. Self-pollution of a star formed from r-rich ISM

This scenario (Hill et al. 2000; Cohen et al. 2003; Jonsell et al. 2006) is shown in Fig. 11b. As discussed in Jonsell et al. (2006) and Abate et al. (2016), this hypothesis may be rejected as none of the CEMP-r/s stars observed to date have been found to be in the evolutionary stage of AGB phase. The stars we studied are giants, and the estimated low ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ values and the absence of Tc lines imply the extrinsic nature of the overabundance of carbon and heavy elements. This scenario thus cannot explain the abundance pattern observed in our programme stars.

### 8.1.3. SN and AGB pollution of a star in triple system

Figure 11d shows this scenario (Cohen et al. 2003; Jonsell et al. 2006). Both Cohen et al. (2003) and Jonsell et al. (2006) dismissed this scenario because it seems very unrealistic that the

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Table 9. Comparison of the abundances of our programme stars with the literature values.

| Star name | $[\mathrm{Fe} / \mathrm{H}]$ | $[\mathrm{C} / \mathrm{Fe}]^{(*)}$ | $[\mathrm{N} / \mathrm{Fe}]$ | $[\mathrm{Sr} / \mathrm{Fe}]$ | $[\mathrm{Y} / \mathrm{Fe}]$ | $[\mathrm{Zr} / \mathrm{Fe}]$ | $[\mathrm{Ba} \mathrm{II} / \mathrm{Fe}]$ | Ref. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HD 145777 | -2.17 | 2.42 | 0.67 | 0.67 | 1.22 | 1.05 | 1.27 | 1 |
| CD-27 14351 | -2.71 | 2.98 | 1.88 | 1.74 | 1.97 | 2.21 | 1.82 | 1 |
|  | -2.62 | 2.89 | 1.89 | 1.73 | 1.99 | - | 1.77 | 4 |
| HE 0017+0055 | -2.46 | 2.74 | 2.83 | - | 0.58 | 1.55 | 2.30 | 1 |
|  | -2.40 | 2.17 | 2.47 | - | 0.50 | 1.60 | $>1.90$ | 3 |
|  | -2.72 | 2.31 | 0.52 | - | - | - | - | 5 |
| HE 2144-1832 | -1.63 | 1.80 | 0.50 | 0.66 | 1.16 | 0.97 | 1.49 | 1 |
|  | -1.70 | 0.80 | 0.60 | 1.50 | - | - | 1.30 | 2 |
| HE 2339-0837 | -2.74 | 2.93 | - | 1.32 | 0.67 | 1.64 | 2.21 | 1 |
|  | -2.71 | 2.71 | - | - | - | - | - | 5 |
| Star name | $[\mathrm{La} \mathrm{II} / \mathrm{Fe}]$ | $[\mathrm{Ce} \mathrm{II} / \mathrm{Fe}]$ | $[\mathrm{Pr} \mathrm{II} / \mathrm{Fe}]$ | $[\mathrm{Nd} \mathrm{II/Fe]}$ | $[\mathrm{Sm} \mathrm{II} / \mathrm{Fe}]$ | $[\mathrm{Eu} \mathrm{II} / \mathrm{Fe}]$ |  | Ref. |
| HD 145777 | 1.37 | 1.79 | 1.67 | 1.48 | 1.63 | 0.80 | 1 |  |
| CD-27 14351 | 1.56 | 1.89 | 1.96 | 1.37 | - | $<0.39$ | 1.65 | 1 |
| HE 0017+0055 | 1.57 | 2.46 | 2.11 | - | 1.26 | - | 1.98 | 2.14 |
|  | 2.40 | 2.00 | - | 2.25 | 2.20 | 1.90 | 2.30 | 4 |
| HE 2144-1832 | - | - | - | - | - | - | 1 |  |
|  | - | 1.70 | 1.72 | 1.61 | 1.78 | 1.01 | 3 |  |
| HE 2339-0837 | 2.24 | 2.37 | - | - | - | - | 5 |  |
|  | - | - | - | - | - | 1 |  |  |

Notes. ${ }^{(*)}$ Abundance of carbon is the average abundance derived from different molecular bands.
References. 1. Our work, 2. Hansen et al. (2016a), 3. Jorissen et al. (2016a), 4. Karinkuzhi et al. (2017), 5. Kennedy et al. (2011).
Table 10. Observed abundance ratios.

| Star name | [ $\mathrm{Fe} / \mathrm{H}$ ] | [1s/Fe] | [hs/Fe] | [hs/ls] | ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ <br> (From CN band at $8005 \AA$ ) | $\begin{gathered} { }^{12} \mathrm{C} /{ }^{13} \mathrm{C} \\ \text { (From } \mathrm{C}_{2} \text { band at } 4740 \AA \text { ) } \end{gathered}$ | [ $\mathrm{Ba} / \mathrm{Eu}]$ | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HD 145777 | -2.17 | 0.98 | 1.48 | 0.50 | 5.45 | 5.50 | 0.47 | 1 |
| CD-27 14351 | -2.71 | 1.97 | 1.66 | -0.31 | 5.50 | 2.58 | - | 1 |
|  | -2.62 | 1.82 | 1.77 | -0.05 | 10.1 | - | 0.14 | 4 |
| HE 0017+0055 | -2.46 | 1.07 | 2.28 | 1.21 | 3.64 | 4.00 | 0.16 | 1 |
|  | -2.40 | 1.05 | 2.20 | 1.15 | - | 4.00 | - | 3 |
|  | - | - | - | - | - | 1.30 | - | 2 |
| HE 2144-1832 | -1.63 | 0.93 | 1.58 | 0.65 | 2.50 | 2.50 | 0.48 | 1 |
|  | - | - | - | - | - | 2.10 | - | 2 |
| HE 2339-0837 | -2.74 | 1.21 | 2.34 | 1.13 | - | 7.00 | 0.37 | 1 |

References. 1. Our work, 2. Goswami (2005), 3. Jorissen et al. (2016a), 4. Karinkuzhi et al. (2017).
triple system survives such a nearby SN explosion for further mass transfer. Abate et al. (2016) also rejected this hypothesis, failing to reproduce the observed frequency of CEMP-r/s stars.

### 8.1.4. AGB and 1.5 SN pollution of a star in a binary system

This scenario is shown in Fig. 11e (Jonsell et al. 2006). It was shown by Zijlstra (2004) that at low metallicity, due to low mass-loss efficiency, the degenerate core of high-mass AGB star remains massive enough to reach the Chandrasekhar mass limit and explodes as a type 1.5 supernova (Iben \& Renzini 1983). However, type 1.5 supernova can disrupt the binary system by destroying the primary star (Nomoto et al. 1976; Iben \& Renzini 1983; Lau et al. 2008). As discussed in Abate et al. (2016), this hypothesis is also dismissed as most CEMP-r/s stars are found to be in binary systems (Lucatello et al. 2005).
8.1.5. AGB and accretion-induced collapse (AIC) pollution of a star in a binary system

This scenario (Qian \& Wasserburg 2003; Cohen et al. 2003) is shown in Fig. 11f. The three phases of mass transfer seem problematic since the observed CEMP-r/s stars, in many cases, are found to be at the main-sequence turn-off making the accretion difficult (Lugaro et al. 2009). As discussed in Abate et al. (2016), a narrow orbital separation is required for this scenario, so that even after the first phase of mass transfer the stars stay close enough to fill the Roche-lobe for the next phase of mass transfer. However, taking this situation into account, the observed frequency of CEMP-r/s stars could not be reproduced (Abate et al. 2016). In addition, it is quite uncertain if this kind of collapse can produce $r$-process elements so as to match the observed abundance pattern of the CEMP-r/s stars (Qian \& Woosley 1996; Qian \& Wasserburg 2003).

Table 11. Spatial velocity and probability estimates.

| Star name | $U_{\text {LSR }}\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | $V_{\mathrm{LSR}}\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | $W_{\mathrm{LSR}}\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | $V_{\text {spa }}\left(\mathrm{km} \mathrm{s}^{-1}\right)$ | $P_{\text {thin }}$ | $P_{\text {thick }}$ | $P_{\text {halo }}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HD 145777 | $-4.51 \pm 3.22$ | $-155.01 \pm 17.49$ | $67.18 \pm 5.62$ | $169.00 \pm 13.86$ | 0 | 0.83 | 0.17 |
| CD-27 14351 | $101.95 \pm 4.04$ | $-213.31 \pm 24.66$ | $-57.21 \pm 4.17$ | $243.25 \pm 20.88$ | 0 | 0.10 | 0.90 |
| HE 0017+0055 | $16.21 \pm 2.02$ | $-190.74 \pm 29.87$ | $-10.33 \pm 15.90$ | $191.71 \pm 30.31$ | 0 | 0.65 | 0.35 |
| HE 2144-1832 | $234.33 \pm 16.01$ | $8.57 \pm 6.32$ | $-9.90 \pm 9.09$ | $234.69 \pm 15.82$ | 0.01 | 0.84 | 0.15 |
| HE 2339-0837 | $218.78 \pm 34.88$ | $-126.66 \pm 37.83$ | $-224.20 \pm 14.05$ | $337.90 \pm 4.18$ | 0 | 0 | 1.0 |

### 8.1.6. Intermediate neutron-capture process (i-process)

In their simulations Cowan \& Rose (1977) found that a significantly high neutron flux (higher than that of $s$-process) can be produced by mixing different amounts of hydrogen-rich material into the intershell region of AGB stars (also known as proton ingestion episodes or PIEs), leading to the occurrence of $i$-process nucleosynthesis in AGB stars. This nucleosynthesis process operating at a neutron density ( $n \sim 10^{15} \mathrm{~cm}^{-3}$ ), which is intermediate to that of $s$ - and $r$-process neutron densities can produce both $s$ - and $r$-process elements in a single stellar site (Dardelet et al. 2014; Hampel et al. 2016, 2019; Roederer et al. 2016). Hampel et al. (2016) successfully reproduced the abundance distribution of 20 CEMP-r/s stars with the help of an $i$-process model. Although it is evident that the $i$-process can explain the abundance pattern seen in CEMP-r/s stars, the astrophysical sites of the $i$-process are not clearly understood. A variety of sites have been proposed where PIEs can take place, favouring the conditions for $i$-process nucleosynthesis.

Figure 11a shows the formation scenario of CEMP-r/s stars, which is similar to that suggested for $\mathrm{CH}, \mathrm{Ba}$, and CEMP-s stars. In this scenario these stars are secondary in binary systems, where the primary, which is slightly more massive, evolves to the AGB phase and transfers $s$-process rich elements to the secondary star. The only difference in the scenario for CEMP-r/s stars is that the primary produces both $s$ - and $r$-process elements in the AGB phase with the help of $i$-process nucleosynthesis, and later pollutes the secondary with both $s$ - and $r$-process elements. Recent simulations have shown that higher neutron densities of the order of $10^{12-15} \mathrm{~cm}^{-3}$ necessary for $i$-process are attained in very metal-poor AGB stars (Campbell \& Lattanzio 2008; Cristallo et al. 2009; Campbell et al. 2010; Stancliffe et al. 2011). The reactions ${ }^{13} \mathrm{C}(\alpha, n)^{16} \mathrm{O}$ and ${ }^{22} \mathrm{Ne}(\alpha, n)^{25} \mathrm{Mg}$ are the two neutron sources proposed to operate in AGB stars. The reaction ${ }^{22} \mathrm{Ne}(\alpha, n){ }^{25} \mathrm{Mg}$ that can produce a neutron density of $\sim 10^{11-14} \mathrm{~cm}^{-3}$ needs a temperature of $\sim 3 \times 10^{8} \mathrm{~K}$ for activation, which is achieved only in intermediate-mass stars $\left(M \geq 3 M_{\odot}\right)$ at the thermal pulse (TP) phase (Lugaro et al. 2012). As this phase is very short (a few days), in spite of high neutron density, neutron exposure remains inefficient to produce the heavy- $s$ process peak (Fishlock et al. 2014). Again, the ${ }^{13} \mathrm{C}(\alpha$, $n)^{16} \mathrm{O}$ neutron source gets activated at a lower temperature $\left(\sim 1 \times 10^{8} \mathrm{~K}\right)$, and hence can operate in the interpulse phase of both low- and intermediate-mass AGB stars. Although this reaction can produce a neutron density of $\sim 10^{7} \mathrm{~cm}^{-3}$, the longer timescale ( $\sim 10^{5} \mathrm{yr}$ ) of the interpulse phase enables sufficient neutron exposure to produce the heavy-s peak. However, some authors (Masseron et al. 2010; Jorissen et al. 2016a) argue in favour of the ${ }^{22} \mathrm{Ne}(\alpha, n)^{25} \mathrm{Mg}$ reaction as the primary neutron source responsible for the production of the abundance peculiarity observed in CEMP-r/s stars. The isotopic ratio of Mg could provide sufficient clues about the neutron source. The operation of ${ }^{22} \mathrm{Ne}(\alpha, n)^{25} \mathrm{Mg}$ reaction produces a large amount
of ${ }^{25} \mathrm{Mg}$, which in turn produces ${ }^{26} \mathrm{Mg}$ by neutron-capture. So, we can expect the ${ }^{24} \mathrm{Mg}:{ }^{25} \mathrm{Mg}:{ }^{26} \mathrm{Mg}$ ratio to change from the terrestrial ( $79: 10: 11$ ) value to a ratio with higher abundances of ${ }^{25} \mathrm{Mg}$ and ${ }^{26} \mathrm{Mg}$ (Scalo 1978). However, Zamora et al. (2004) attempted to determine Mg isotopic ratios from MgH bands in cool carbon stars and concluded that at optical wavelengths it is not possible to derive the Mg isotopic ratios as the synthetic spectra are insensitive to variations of Mg isotopic ratios due to the presence of strong $\mathrm{C}_{2}$ and CN molecular bands. Thus, the scope of finding a spectroscopic test to identify the neutron source responsible for the production of heavy elements in CEMP-r/s stars still remains open.

Another site proposed for the $i$-process nucleosynthesis, supporting binary mass-transfer scenario for the formation of CEMP-r/s stars, is the very late thermal pulse (VLTP) in postAGB stars (Herwig et al. 2011). The abundance pattern of Sakurai's object (V4334 Sagittarii), a born-again giant, could not be reproduced by $s$-process yields. This object shows an overabundance of $\mathrm{Rb}, \mathrm{Sr}$, and Y that is two orders of magnitude higher than that of the second $s$-process peak (Asplund et al. 1999). Assuming proton ingestion into the He-shell convection zone, Herwig et al. (2011) carried out a 3D hydrodynamic simulation of a VLTP in a pre-white dwarf. They achieved a significantly high neutron density $\left(10^{15} \mathrm{~cm}^{-3}\right)$ and could successfully reproduce the abundance distribution of Sakurai's object. The post-AGB stars in the Large and Small Magellanic Clouds (LMC and SMC, respectively) are found to exhibit an unusual abundance pattern (van Winckel 2003). Lugaro et al. (2015) illustrated that the $s$-process cannot explain the abundance pattern of these stars and proposed that $i$-process might explain better the abundances of the heavy elements along with the measured low abundance of Pb . Later, Hampel et al. (2019) could satisfactorily fit the abundance patterns observed in seven Pb poor post-AGB stars (including the post-AGB stars of LMC and SMC) with $i$-process models.

Simulations of super-AGB TP stars showed that proton ingestion into the convective He-burning shell is favoured following the production of $i$-process neutron density (Doherty et al. 2015; Jones et al. 2016). Metal-poor massive stars (20$30 M_{\odot}$ ) are also considered as $i$-process sites (Banerjee et al. 2018; Clarkson et al. 2018). A single CEMP-r/s star can form from the ISM contaminated by the $i$-process material ejected by metal-poor massive stars (Banerjee et al. 2018).

One more proposed site for $i$-process nucleosynthesis is rapidly accreting white dwarf (RAWDs) (Denissenkov et al. 2017; Côté et al. 2018; Denissenkov et al. 2019). Denissenkov et al. (2019) proposed that single CEMP-r/s stars could be the tertiary (with a wider orbit) in a triple star system, where it orbits a close binary with a RAWD. Later the tertiary escapes from the triple star system being polluted by $i$-process material from the RAWD when the RAWD explodes as a SNIa. Due to the requirement of a particular sequence of events, population synthesis
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Fig. 11. Representation of different proposed formation scenarios of CEMP-s and CEMP-r/s stars. $M_{1}, M_{2}$, and $M_{3}$ represent the masses of the stars, where $M_{1}>M_{2}>M_{3}$. Here evolutions of single, binary, and triple star systems with different conditions are shown. The figures are discussed individually in Sect. 8.1.
calculations can only decide the probability of the formation of CEMP-r/s stars from RAWDs (Hampel et al. 2019).

Roederer et al. (2016) reported a metal-poor star HD 94028 with underabundance of carbon $([\mathrm{C} / \mathrm{Fe}]=-0.06)$, and low Ba and Eu abundances. With the help of high-quality NUV spectra, they could estimate the abundances or upper limits of 64 species of 56 elements including the species whose features are seen mostly in the NUV. Roederer et al. (2016) found that the star exhibits a supersolar [As/Ge] ratio, a solar [Se/As] ratio, and enhanced abundances of Mo and Ru. They could not reproduce this elemental pattern with any combination of s and $r$-process, but an additional contribution from the $i$-process could fit the peculiar pattern. The contribution of $i$-process has also been observed in pre-solar grains in pristine meteorites (Fujiya et al.

2013; Liu et al. 2014). These observations indicate more than one astrophysical sites for the $i$-process.

### 8.1.7. AGB pollution of a star in binary system formed from r-rich ISM

This scenario (Hill et al. 2000; Cohen et al. 2003; Jonsell et al. 2006; Ivans et al. 2005; Bisterzo et al. 2011) is illustrated in Fig. 11c. Although Bisterzo et al. $(2011,2012)$ claim to reproduce, within the error bars, the observed [hs/ls] (which is higher in CEMP-r/s stars than CEMP-s stars) considering the binary system formed from the r-rich molecular cloud, there are several arguments that stand against this scenario. It was noted that in the case of independent $s$ - and $r$-process enrichment, the
correlation of the abundances of Ba and Eu cannot be reproduced by the AGB models (Abate et al. 2016), and also that this scenario cannot explain the large fraction of CEMP-r/s stars among the CEMP-s stars (Jonsell et al. 2006; Lugaro et al. 2009).

As the abundance patterns of most of the CEMP-r/s stars found in the literature can be explained with $i$-process models, some authors prefer the nomenclature 'CEMP-i' to 'CEMP-r/s' (Hampel et al. 2016; Frebel 2018; Hampel et al. 2019) and calling the stars formed by AGB pollution in the binary system formed from r-rich ISM ‘CEMP-r+s stars’ (Gull et al. 2018; Frebel 2018).

Gull et al. (2018) reported a red giant CEMP star RAVE $\mathrm{J} 094921.8-161722([\mathrm{Fe} / \mathrm{H}]=-2.2,[\mathrm{C} / \mathrm{Fe}]=1.35)$ with a surprising elemental abundance pattern. The star exhibits an enhanced abundance of Pb , indicating $s$-process contribution and Th , which is produced in $r$-process nucleosynthesis. Gull et al. (2018) claimed that this object was the first bona fide CEMP$\mathrm{r}+\mathrm{s}$ star as its abundance pattern could be satisfactorily fitted only with AGB mass-transfer model taking into account initial $r$-process enhancement. Sbordone et al. (2020) reported the abundance analysis of object GIU J190734.24-315102.1 located in the Sagittarius (Sgr) dwarf spheroidal (dSph) galaxy, and claimed that the abundance pattern could be best fit only with a model considering AGB-pollution in a binary system preenriched with a neutron star-neutron star merger event. Sbordone et al. (2020) classify this object as the first CEMP-r/s star found in the Sgr dSph, but due to its formation scenario this object may be referred to as a bona fide CEMP-r+s star.

The expected rate of occurrence of CEMP-r+s stars among metal-poor stars is $2-3 \%$ (Gull et al. 2018). With an occurrence rate of $3 \%$, about two dozen r-II stars have been found to date (Gull et al. 2018), although why no other bona fide CEMP-r+s stars have yet been detected remains a puzzle (Frebel 2018).

### 8.2. Comparison of the observed abundances of the programme stars with i-process model predictions

Hampel et al. (2016) calculated yields of heavy elements considering different constant neutron densities ranging from $10^{7}-10^{15} \mathrm{~cm}^{-3}$ using single-zone nuclear network calculations. The nucleosynthesis is assumed to occur in the intershell region of AGB stars. The physical input parameters, such as temperature and density for the intershell region of a low-mass ( $1 M_{\odot}$ ) low-metallicity $\left(z=10^{-4}\right)$ AGB star, are adapted from Stancliffe et al. (2011). The constituents of the intershell region have been adapted from that of Abate et al. (2015). The temperature and density of the intershell region are considered to be $1.5 \times 10^{8} \mathrm{~K}$ and $\rho=1600 \mathrm{~g} \mathrm{~cm}^{-3}$, respectively. However, no significant changes in the results were found when tested with a range of temperatures $\left(1 \times 10^{8}\right.$ to $\left.2.2 \times 10^{8} \mathrm{~K}\right)$ and densities $\left(\rho=800-3200 \mathrm{gcm}^{-3}\right)$. The run times of the models are adjusted in such a way that a high neutron exposure ( $\tau \sim 495 \mathrm{mb}^{-1}$ ) is ensured. Equilibrium abundance pattern between heavy elements and the seed nuclei is established based on such a high neutron exposure, and the element-to-element ratio becomes a function of constant neutron density. After the exposure the neutron flux is kept switched off for $t=10 \mathrm{Myr}$.

During the time when neutron flux is switched on, it should be noted that for lower neutron densities the elemental abundance pattern of typical $s$-process is produced with stable ls $(\mathrm{Sr}$, $\mathrm{Y}, \mathrm{Zr})$ and $\mathrm{hs}(\mathrm{Ba}, \mathrm{La}, \mathrm{Ce})$ peaks. However, with $i$-process neutron densities $\left(n=10^{12}-10^{15} \mathrm{~cm}^{-3}\right)$, the neutron-capture path goes further away from the valley of stability, making both is and hs peak shift to lighter elements; in particular, they form a peak at ${ }^{135} \mathrm{I}$. Then, after the neutron exposure is switched off, it is


Fig. 12. Best-fitting $i$-process model (solid blue curve) for the stars. The points with error bars indicate the observed abundances.
found that the decay of unstable isotopes produce stable 1s and hs peak elements, for example ${ }^{135} \mathrm{I}$ decays to produce ${ }^{135} \mathrm{Ba}$. Abundances of Ba and Eu are found to increase with neutron density. This is how the $i$-process can modify the abundance pattern of neutron-capture elements.

We used the model yields ([X/Fe]) of Hampel et al. (2016), with neutron densities ranging from $10^{9}-10^{15} \mathrm{~cm}^{-3}$, and compared them with the observed abundances of our programme stars. In order to find the neutron density responsible for the observed abundance distribution of the programme stars, we followed the procedure given in Hampel et al. (2016). We used the equation
$X=X_{i}(1-d)+X_{\odot} d$,
where $X_{i}$ is the model yield, $X_{\odot}$ is the solar-scaled abundance, and $d$ is a dilution factor.

Figure 12 shows the best-fit models with appropriate neutron densities and corresponding dilution factors. It is seen that the $i$-process model with neutron densities of $n \sim 10^{13}, 10^{15}$, and $10^{14} \mathrm{~cm}^{-3}$ closely fit the observed abundances of HE 2144-1832, HE 0017+0055, and HE 2339-0837, respectively. The best model fit for HD 145777 is found at a neutron density of $n \sim$ $10^{10} \mathrm{~cm}^{-3}$.

### 8.3. Classification of the programme stars

As discussed in Sect. 1, different authors (Beers \& Christlieb 2005; Jonsell et al. 2006; Masseron et al. 2010; Abate et al. 2016; Frebel 2018; Hansen et al. 2019) have used different criteria to classify the CEMP stars into various subclasses. Four objects in our sample, HD 145777, HE 0017+0055, HE 2144-1832, and HE 2339-0837, show overabundances of Ba and Eu along with other light-s and heavy-s elements. With $0<[\mathrm{Ba} / \mathrm{Eu}]<0.5$, all four objects fall in the category of CEMP-r/s stars if the classification criteria of Beers \& Christlieb (2005) for CEMP-r/s stars is followed. But, according to the classification scheme of Abate et al. (2016), CEMP-r/s stars are those that have $[\mathrm{Ba} / \mathrm{Fe}]$
and $[\mathrm{Eu} / \mathrm{Fe}]$ values that are greater than unity. This criterion classifies HE 2144-1832 $([\mathrm{Ba} / \mathrm{Fe}]=1.49$ and $[\mathrm{Eu} / \mathrm{Fe}]=1.01)$, HE $0017+0055([\mathrm{Ba} / \mathrm{Fe}]=2.30$ and $[\mathrm{Eu} / \mathrm{Fe}]=2.14)$, and HE 2339-0837 $([\mathrm{Ba} / \mathrm{Fe}]=2.21$ and $[\mathrm{Eu} / \mathrm{Fe}]=1.84)$ as CEMP-r/s stars, and HD 145777 ( with $[\mathrm{Ba} / \mathrm{Fe}]=1.27$ and $[\mathrm{Eu} / \mathrm{Fe}]=0.80$ ) as a CEMP-s star. All four of these objects fall in the category of CEMP-r/s stars if we use the criteria $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$ given by Frebel (2018) for the CEMP-i subclass (we use the 'CEMP$\mathrm{r} / \mathrm{s}^{\prime}$ nomenclature). We could not estimate the abundances of Hf, Ir , and Pb , hence the other criteria, namely $[\mathrm{Hf} / \mathrm{Ir}] \sim 1.0$ for the CEMP-i subclass and $[\mathrm{Ba} / \mathrm{Pb}]>-1.5$ for the CEMP-s subclass put forward by Frebel (2018), could not be used. However, the lower limit given on $[\mathrm{Ba} / \mathrm{Eu}](>0.5)$ by Frebel (2018) for the CEMP-s subclass clearly indicates that these four stars cannot be classified as CEMP-s stars. If we use [ $\mathrm{Sr} / \mathrm{Ba}$ ] as a classifier, as discussed in Hansen et al. (2019) with values [ $\mathrm{Sr} / \mathrm{Ba}$ ] $\sim-0.60$, -0.83 , and -0.89 respectively for HD 145777, HE 2144-1832, and HE 2339-0837, they fall in the category of CEMP-r/s stars. As the abundance of Sr could not be estimated for the object HE $0017+0055$, [Sr/Ba] could not be used to classify this object.

The object CD-27 14351 is found to satisfy the criteria for the CEMP-s stars of all four classification schemes, hence this object with $[\mathrm{Ba} / \mathrm{Fe}]=1.82,[\mathrm{Eu} / \mathrm{Fe}]<0.39,[\mathrm{Ba} / \mathrm{Eu}]>1.43$, $[\mathrm{La} / \mathrm{Eu}]>1.17$, and $[\mathrm{Sr} / \mathrm{Ba}]=-0.08$ is classified as a CEMP-s star.

### 8.3.1. Probing [hs/ls] as a classifier

It has been noted from various studies in the past (Bisterzo et al. 2011, 2012; Abate et al. 2015, 2016; Hampel et al. 2016) that [hs/ls] exhibit higher values for CEMP-r/s stars than that of CEMP-s stars. In this section we explore whether [hs/ls] can be used to distinguish CEMP-r/s and CEMP-s stars, and hence if this ratio can be used as a classifier.

To accomplish this we carried out a literature survey and compiled data for 40 CEMP-s and 32 CEMP-r/s stars, and calculated $[\mathrm{hs} / \mathrm{ls}],[\mathrm{Sr} / \mathrm{Ba}]$, and $[\mathrm{Ba} / \mathrm{Eu}]$ for these stars on a homogeneous scale. We adopt the CEMP classifications of the literature objects given by the original studies and without any ambiguity. However, for some objects different groups have provided different atmospheric parameters and elemental abundances, and have assigned different classes to them. For instance, Allen et al. (2012) considered HE 0336+0113 to be a CEMP-s star, but Masseron et al. (2010) considered it a CEMP-r/s star. HE 0336+0113 exhibits $[\mathrm{Eu} / \mathrm{Fe}]>1.0$ and shows the highest value of $[\mathrm{Ba} / \mathrm{Eu}](=1.45)$ among the CEMP stars (Cohen et al. 2006). Hampel et al. (2019), after comparing the object's observed abundances with $i$-process models, reported that the characteristic properties of HE 0336+0113 are more of $s$-process than $i$-process. This analysis prompted us to classify HE $0336+0113$ as a CEMP-s star. Bisterzo et al. $(2011,2012)$ studied most of the CEMP-s stars in Table A. 2 and explained their abundance peculiarities with the help of AGB models with initial masses of 1.3-2.0 $M_{\odot}$. Except for SDSS J1349-0229, which is classified as a CEMP-r/s star (Behara et al. 2010), all other CEMP-r/s stars in Table A. 2 have been examined with $i$-process model predictions and their abundance patterns are well reproduced with $i$-process model yields (Hampel et al. 2016, 2019; Goswami \& Goswami 2020).

The elemental abundances of the objects reported by different authors differ from each other. As different authors use different codes, model atmospheres, and line lists for their abundance analyses, it is not surprising to see the differences in their results; however, it is not an easy task to select one analysis over
the others. Thus, for the objects for which the elemental abundance results from several different groups are available, we take the mean value of $[\mathrm{Fe} / \mathrm{H}]$, and similarly the mean abundance for each element. For these cases, we use the mean $[\mathrm{X} / \mathrm{Fe}]$ to calculate $[\mathrm{hs} / \mathrm{ls}],[\mathrm{Sr} / \mathrm{Ba}]$, and $[\mathrm{Ba} / \mathrm{Eu}]$. To calculate $[\mathrm{l} / \mathrm{Fe}]$, we take the mean of the abundances of light-s elements ( $\mathrm{Sr}, \mathrm{Y}, \mathrm{Zr}$ ); similarly, the abundances of heavy-s elements ( $\mathrm{Ba}, \mathrm{La}, \mathrm{Ce}, \mathrm{Nd}$ ) are averaged out to calculate $[\mathrm{hs} / \mathrm{Fe}]$. We do not consider the two second peak $s$-process elements Pr and Sm , as $r$-process contributes more than $s$-process to the isotopic abundances of these elements (Arlandini et al. 1999). Bisterzo et al. (2012) noted that lights elements when plotted against each other show large scatter. Heavy-s elements also show scatter for some objects, although not as large. In order to reduce the systematic error, we calculated $[\mathrm{ls} / \mathrm{Fe}]$ and $[\mathrm{hs} / \mathrm{Fe}]$ only for those stars for which abundance estimates are available at least for two light $s$-process and two heavy $s$-process elements. To calculate [ls/Fe] and $[\mathrm{hs} / \mathrm{Fe}]$, we also excluded those elements for which only the upper limit of abundance is mentioned in the literature. Table A. 2 presents the list of objects and their elemental abundance ratios of $\mathrm{C}, \mathrm{N}$, and heavy elements used for this analysis. Our estimates of [hs/ls] are also presented in this table. Estimates of [ $\mathrm{hs} / \mathrm{ls}$ ], when plotted with respect to $[\mathrm{Fe} / \mathrm{H}]$, show a large scatter (Fig. 13b). The use of different sets of elemental abundances instead of using a consistent set of elements for hs and 1 l abundances may also contribute to this observed scatter. Nevertheless, it is not always possible to have the same set of hs and is elements for all stars, and using a consistent set of elements will tremendously affect the number of stars used to carry out the test. As metallicity decreases, the neutron-to-iron seed ratio increases and hence heavier elements are synthesised to a greater extent (i.e. [hs/ls] increases as metallicity decreases; Gallino et al. 1998). In Fig. 13b we can clearly see this trend for both CEMP-s (black filled squares) and CEMP-r/s (red filled circles) stars. However, even though they have the same metallicity range, we note that the CEMP$\mathrm{r} / \mathrm{s}$ stars exhibit higher values of [hs/ls] than the CEMP-s stars (Bisterzo et al. 2011, 2012). This implies that neutron density has to be higher for the formation of CEMP-r/s stars than of CEMP-s stars. Similarly, in Fig. 13d, we can see that the mean abundances of 1s elements have the same range in the cases of CEMP-s and CEMP-r/s stars, but in CEMP-r/s stars the hs elements are more enhanced than in CEMP-s stars. This indicates that the heavy elements observed in CEMP-r/s stars are synthesised with a higher neutron density than those in CEMP-s stars. This is because the higher neutron density can easily overcome the barrier ( $\tau \sim 0.05 \mathrm{mb}^{-1}$ ) at the magic neutron number 50 (the ls peak), and effectively produces the hs peak at the magic neutron number 82. As seen from Fig. 13c, $[\mathrm{Eu} / \mathrm{Fe}]$ increases with $[\mathrm{hs} / \mathrm{Fe}]$, showing a tight correlation between $[\mathrm{Eu} / \mathrm{Fe}]$ and $[\mathrm{hs} / \mathrm{Fe}]$. This correlation between heavy-s elements and Eu observed in the CEMP-r/s stars can only be explained with the help of a formation mechanism where both the $s$-process and $r$-process elements are produced in a single stellar site, which provides much support for $i$-process as a possible formation mechanism for CEMP-r/s stars. As [hs/ls] does not depend upon the dilution of the AGB processed material on the companion star, using a sample of CEMP-s and CEMP-r/s stars from the literature, we examined whether this ratio could be used to distinguish between CEMP-s and CEMP-r/s stars. We find that CEMP-s stars peak at around $[\mathrm{hs} / \mathrm{ls}] \sim 0.65$ with a standard deviation of 0.35 , and CEMP-r/s stars peak at [hs/ls] $~ 1.06$ with a standard deviation of 0.32 . However, even though they peak at different values of [hs/ls], we see an overlap of CEMP-s and CEMP-r/s stars in the range $0.0<[\mathrm{hs} / \mathrm{ls}]<1.5$ (Figs. 13a,b). Hence, [hs/ls] cannot be


Fig. 13. Probing [hs/ls] as a classifier of CEMP-s and CEMP-r/s stars. The filled red circles represent CEMP-r/s stars, filled black squares represent CEMP-s stars, and filled blue triangles and filled green pentagons respectively represent CEMP-s and CEMP-r/s stars in this work. Panel $a$ : $\mu$ and $\sigma$ represent the mean and standard deviation of [hs/ls] respectively for CEMP-s and CEMP-r/s stars. Panel c: short-dashed black line represents the correlation between $[\mathrm{hs} / \mathrm{Fe}]$ and $[\mathrm{Eu} / \mathrm{Fe}]$ for CEMP-s and CEMP-r/s stars. Panel $d$ : short-dashed black line and long-dashed red line represent the correlation between $[\mathrm{hs} / \mathrm{Fe}]$ and $[1 \mathrm{~s} / \mathrm{Fe}]$ for CEMP-s and CEMP-r/s stars, respectively.
used as a useful classifier for CEMP-s and CEMP-r/s stars. In Fig. 13d all the CEMP-r/s stars lie above the solid black line at [hs/Fe] ~ 1.4; however, a limiting value of $[\mathrm{hs} / \mathrm{Fe}] \geq 1.4$ also cannot be used as a classifier as many CEMP-s stars also exhibit $[\mathrm{hs} / \mathrm{Fe}] \geq 1.4$.

### 8.3.2. Identification of classifier based on available data

In order to explain the nature of the emerging CEMP stars, Beers \& Christlieb (2005) introduced for the first time four subclasses of CEMP stars using only two neutron-capture elements, Ba and Eu (due to the observational limitations). This scheme of classification is a guide to the community to use the unifying nomenclature and to facilitate further advances. However, since the classification of Beers \& Christlieb (2005), various authors (Jonsell et al. 2006; Masseron et al. 2010; Norris et al. 2010; Bisterzo et al. 2011; Bonifacio et al. 2015; Maeder \& Meynet 2015; Yoon et al. 2016; Abate et al. 2016; Hansen et al. 2016b; Frebel 2018; Hansen et al. 2019; Skúladóttir et al. 2020) put forward different criteria for identification and classification of the CEMP stars. The community has not had much time to understand the physics behind the observed abundance patterns. The ever-growing data sets and the advancement of theoretical predictions require further revisions of the classification schemes,
and thus revisiting these classification schemes is extremely important and unavoidable.

We have seen that one of our programme stars, HD 145777, is classified as a CEMP-r/s star by three classification schemes (Beers \& Christlieb 2005; Frebel 2018; Hansen et al. 2019) and as a CEMP-s star by the criteria discussed by Abate et al. (2016). So, we tried to figure out which of the classification scheme discussed above fits the literature data. As the programme stars are CEMP-s and CEMP-r/s types, we focus on the classification schemes that discuss the criteria to distinguish these two subclasses.
[Sr/Ba] as a classifier. We first discuss the most recent classifier, $[\mathrm{Sr} / \mathrm{Ba}]$. When we plot $[\mathrm{Sr} / \mathrm{Ba}]$ versus $[\mathrm{Fe} / \mathrm{H}]$ (Fig. 14a), we can see that there is a clear overlap of CEMP-s and CEMP-r/s stars with respect to $[\mathrm{Sr} / \mathrm{Ba}]$ (as seen in the case of [hs/ls]) in the range $-1.6<[\mathrm{Sr} / \mathrm{Ba}]<-0.5$. In Figs. $14 \mathrm{a}, \mathrm{b}$ the grid formed by the dashed black lines and the grid formed by the dotted red lines represent the region of CEMP-s and CEMPr/s stars, respectively, put forward by the classification scheme of Hansen et al. (2019). In Fig. 14b, it is seen that a few CEMP stars (Table A.2) with an underabundance of $\mathrm{Eu}([\mathrm{Eu} / \mathrm{Fe}]<1.0)$ also fall in the region defined for CEMP-r/s stars. The number


Fig. 14. [Sr/Ba] as a classifier of CEMP-s and CEMP-r/s stars. The filled red circles represent CEMP-r/s stars, filled black squares represent CEMPs stars, and filled blue triangles and filled green pentagons respectively represent CEMP-s and CEMP-r/s stars in this work. The grid formed by the dashed black lines represents the region of CEMP-s stars, and the grid formed by the dotted red lines represents the region of CEMP-r/s stars put forward by Hansen et al. (2019). In panel (b) the solid black line at $[\mathrm{Eu} / \mathrm{Fe}]=1.0$ separates the CEMP-s and CEMP-r/s stars according to the classification criteria adopted by Abate et al. (2016).


Fig. 15. Same as Fig. 14, but for $[\mathrm{Ba} / \mathrm{Eu}]$. The filled red circles represent CEMP-r/s stars, filled black squares represent CEMP-s stars, and filled blue triangles and filled green pentagons respectively represent CEMP-s and CEMP-r/s stars in this work. The grid formed by the dotted red lines represents the region of CEMP-r/s stars put forward by Beers \& Christlieb (2005). The grid formed by the dashed magenta lines represents the region of CEMP-r/s stars put forward by Abate et al. (2016).
difference of CEMP-s stars in Figs. 14a,b falling in the CEMPr/s region indicates that many CEMP stars with the absence of Eu also fall in the category of CEMP-r/s stars by this classification criterion. We cannot separate CEMP-s and CEMP-r/s stars with the help of the [ $\mathrm{Sr} / \mathrm{Ba}$ ] criterion (Hansen et al. 2019), and hence it cannot be used effectively. Moreover, it is worth mentioning that the abundances of Sr and Ba are highly uncertain due to NLTE effects (Bisterzo et al. 2012). However, as mentioned by Hansen et al. (2019), this criterion may be useful to roughly distinguish between the different CEMP subclasses in low-resolution, low S/N large surveys as absorption lines of Eu are much weaker than Sr .
[Ba/Eu] as a classifier. In Figs. 15a,b the grid formed by the dotted red lines bound the region $(0.0<[\mathrm{Ba} / \mathrm{Eu}]<0.5)$ allowed by Beers \& Christlieb (2005) for CEMP-r/s stars. Although most of the CEMP-r/s stars (filled red circles), including our programme stars (filled green pentagons), reside inside the region, some fall outside the boundary. Abate et al. (2016) did not put an upper limit to $[\mathrm{Ba} / \mathrm{Eu}]$ for CEMP-s and

CEMP-r/s stars, so this criterion could be used more effectively (HE 0336+0113 is the only outlier). According to this criterion, CEMP-r/s stars are a subclass of CEMP-s stars and the criterion $[\mathrm{Eu} / \mathrm{Fe}]>1.0$ separates the CEMP-r/s stars from the CEMP-s stars (Abate et al. 2016). Jonsell et al. (2006) and Masseron et al. (2010) also adopted the same classification scheme as Abate et al. (2016) to distinguish between CEMP-s and CEMP-r/s stars; however, their criteria to classify the other two subclasses (CEMP-r \& CEMP-no) differ. Abundances of many of the CEMP-r/s stars, (e.g. CS 22881-036, CS 29497-030, HE 0143-0441, HE 2258-6358, and LP 625-44) having $[\mathrm{Ba} / \mathrm{Eu}]>0.5$ are found to fit well with the $i$-process model (Hampel et al. 2016) of higher neutron density ( $n \sim 10^{14} \mathrm{~cm}^{-3}$ ) (Hampel et al. 2019). This is in contrast to $0.0<[\mathrm{Ba} / \mathrm{Eu}]<0.5$ of Beers \& Christlieb (2005) for CEMP-r/s stars and also $[\mathrm{Ba} / \mathrm{Eu}]>0.5$ of Frebel (2018) for CEMP-s stars.
[La/Eu] as a classifier. Unlike other classification schemes, Frebel (2018) used different sets of elements to classify CEMP-s and CEMP-r/s stars. While $\mathrm{Ba}, \mathrm{Eu}$, and Pb


Fig. 16. Same as Fig. 14, but for [La/Eu]. The filled red circles represent CEMP-r/s stars, filled black squares represent CEMP-s stars, and filled blue triangles and filled green pentagons respectively represent CEMP-s and CEMP-r/s stars in this work. Panel a: grid formed by the dotted red lines represents the region of CEMP-r/s stars put forward by Frebel (2018). Panel $b$ : we can see that all the CEMP-r/s stars but two fall inside the grid formed by the dotted red lines bound by $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$ and $0.0<[\mathrm{Ba} / \mathrm{Eu}]<1.0$. The grid formed by the black dashed lines bound by $0.5<[\mathrm{La} / \mathrm{Eu}]<0.7$ represents the uncertain region in the upper boundary of the classification put forward by Frebel (2018) for CEMP-r/s stars.
are used in the case of CEMP-s stars, La, Eu, Hf, and Ir are used to classify CEMP-r/s stars. The abundances of Hf and Ir are usually derived from the absorption lines of Hf and Ir that are normally found in the NUV spectra. As we could not get the abundances for these two elements in the literature, the criterion [ $\mathrm{Hf} / \mathrm{Ir}] \sim 1.0$ could not be tested with our compiled data. Theoretical validation of this criterion can be found in Table 4 of Hampel et al. (2016). In Fig. 16a, two CEMP-r/s stars are found to lie outside the region (the grid formed by dotted red lines) defined by $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$, and two CEMP-s stars are located near the upper boundary ( $[\mathrm{La} / \mathrm{Eu}] \sim 0.6$ ) of the region.

Modifications to the classifiers [Ba/Eu] and [La/Eu]. Frebel (2018) kept provisions for future adjustments to the classifying criteria. In Fig. 16b, except for two stars (CD-28 1082 and HD 209621), all the CEMP-r/s stars fall inside the region (the grid formed by the dotted red lines) bound by $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$ and $0.0<[\mathrm{Ba} / \mathrm{Eu}]<1.0$. As a few CEMP-(s \& r/s) stars also fall very close to the upper boundary, we can put uncertainty on the upper limit of $[\mathrm{La} / \mathrm{Eu}]$ (i.e. $[\mathrm{La} / \mathrm{Eu}]<0.6 \pm 0.1$ ). We suggest that an object satisfying the criteria $0.0<[\mathrm{Ba} / \mathrm{Eu}]<1.0$ and $0.0<[\mathrm{La} / \mathrm{Eu}]<0.5$ can be classified as a CEMP-r/s star; however, if $[\mathrm{La} / \mathrm{Eu}]=0.6 \pm 0.1$ the condition $[\mathrm{Eu} / \mathrm{Fe}]>1.0$ also needs to be satisfied for the star to be a CEMP-r/s star. The two outliers exhibit differences in the range $0.5-0.7$ dex between the abundances of La and the other hs elements. In Fig. 15b we can see that a CEMP-s star HE 0336+0113, which is Eu (> 1.0) enhanced with very high value for $[\mathrm{Ba} / \mathrm{Eu}](=1.45)$, falls in the region allowed for CEMP-r/s stars. The upper limit of $[\mathrm{Ba} / \mathrm{Eu}](<1.0)$ is chosen so as to avoid misclassifying such stars as CEMP-r/s stars.
[La/Ce] as a classifier. As models with higher neutron densities are required to reproduce the observed overabundance of heavy elements in the CEMP-r/s stars, the possibility of ${ }^{22} \mathrm{Ne}(\alpha, n)^{25} \mathrm{Mg}$ being the primary neutron source cannot be discarded as it can produce a higher neutron density than the ${ }^{13} \mathrm{C}(\alpha$, $n)^{16} \mathrm{O}$ reaction. Masseron et al. (2010) discussed the requirement of the ${ }^{22} \mathrm{Ne}(\alpha, n)^{25} \mathrm{Mg}$ neutron source for the production of heavy elements in CEMP-r/s stars on the basis of [La/Ce]. In general, $[\mathrm{La} / \mathrm{Ce}]$ gives higher values in CEMP-r/s stars, which is possible only when ${ }^{22} \mathrm{Ne}(\alpha, \mathrm{n})^{25} \mathrm{Mg}$ operates. We have found
[La/Ce] > 0.0 only in HE 0017+0055 among our programme stars. Jorissen et al. (2016a) also recorded a positive value for [ $\mathrm{La} / \mathrm{Ce}$ ] for this object. In the case of the other two CEMP-r/s stars (HE 2144-1832 and HE 2339-0837), [ $\mathrm{La} / \mathrm{Ce}$ ] is found to be negative. In the literature, such negative values are seen in a few other CEMP-r/s stars as well (Table A.2). Furthermore, from the simulations of Hampel et al. (2016) at higher neutron densities ( $n \sim 10^{12-15} \mathrm{~cm}^{-3}$ ), it can be seen that [ $\mathrm{La} / \mathrm{Ce}$ ] does not yield a positive value for all the neutron densities (see Table 4 of Hampel et al. 2016). For $n \sim 10^{12}$ and $10^{13} \mathrm{~cm}^{-3}[\mathrm{La} / \mathrm{Ce}]$ gives positive values, but for $n \sim 10^{14}$ and $10^{15} \mathrm{~cm}^{-3}[\mathrm{La} / \mathrm{Ce}]<0$. So we propose that $[\mathrm{La} / \mathrm{Ce}]$ needs to be reconsidered as an indicator of neutron source.
[As/Ge] and [Se/Ge] as classifiers. Roederer et al. (2016) suggested that supersolar [As/Ge] and solar or subsolar [Se/Ge] could indicate the operation of $i$-process. Although, due to the lack of high-quality NUV spectra, the abundances of these elements ( $\mathrm{As}, \mathrm{Se}, \mathrm{Ge}$ ) are currently limited, in the future the neutron-capture elements found in the NUV region are likely to play important roles in characterising the $i$-process. This will also help to validate the claim that $[\mathrm{As} / \mathrm{Ge}]$ and $[\mathrm{Se} / \mathrm{Ge}]$ could be used as classifiers of $i$-process.

The difficulty in drawing sharp boundaries to distinguish CEMP-s and CEMP-r/s stars is clearly visible in all the classifiers. Moreover, the smooth transition of CEMP-s and CEMP-r/s stars, as seen in Fig. 13c, may indicate that $s$ - and $i$-process neutron densities are not distinctly different and have a continuous range from $n \sim 10^{7}$ to $10^{15} \mathrm{~cm}^{-3}$.

## 9. Conclusions

We have estimated the atmospheric parameters and abundances of twenty-four elements including $\mathrm{C}, \mathrm{N}, \alpha$-elements, Fe-peak elements, and neutron-capture elements for HD 145777, CD-27 14351, HE 0017+0055, HE 2144-1832, and HE 2339-0837. The object HE 2144-1832 is found to be a metal-poor star with $[\mathrm{Fe} / \mathrm{H}] \sim-1.63$, and the other four belong to the very metal-poor class with $[\mathrm{Fe} / \mathrm{H}]<-2$. The kinematic analysis shows that HD 145777, HE 2144-1832, and HE 0017-0055 belong to the thick disc population, and the
objects HE 2339-0837 and CD-27 14351 are members of the halo population.

All the programme stars are found to be bright giants with surface gravity $0.60 \leq \log g \leq 1.40$ and enhanced in carbon with a maximum of $[\mathrm{C} / \mathrm{Fe}] \sim 2.98$ for $\mathrm{CD}-27$ 14351, and a minimum of $\sim 1.80$ for HE 2144-1832. While nitrogen is mildly enhanced in HD 145777 and HE 2144-1832, it shows overabundance with [ $\mathrm{N} / \mathrm{Fe}$ ] $\sim 2.83$ and 1.88 in HE 0017+0055 and CD-27 14351, respectively. In the stars HD 145777 and HE 2144-1832, the $\alpha$ elements Mg and Ca show mild overabundance ( $[\mathrm{X} / \mathrm{Fe}] \sim 0.5$ ). Neutron-capture elements $\mathrm{Sr}, \mathrm{Y}, \mathrm{Zr}, \mathrm{Ba}, \mathrm{La}, \mathrm{Ce}, \mathrm{Nd}, \mathrm{Sm}, \mathrm{Pr}$, and Eu show mild to high enhancements in all the programme stars.

Adopting the classification of Abate et al. (2016), we have found that HE 2144-1832, HE 0017+0055, and HE 2339-0837 with $[\mathrm{Ba} / \mathrm{Fe}]>1,[\mathrm{Eu} / \mathrm{Fe}]>1$, and $[\mathrm{Ba} / \mathrm{Eu}]>0$ are CEMPr/s stars and HD 145777 and CD-27 14351 with $[\mathrm{Ba} / \mathrm{Fe}]>1$, $[\mathrm{Eu} / \mathrm{Fe}]<1$, and $[\mathrm{Ba} / \mathrm{Eu}]>0$ are CEMP-s stars. We do not confirm the high abundance of Eu reported in a previous study (Karinkuzhi et al. 2017) for the object CD-27 14351.

In the context of the double enhancement (enhanced in both $s$ - and $r$-process elements) seen in four of the programme stars, we have discussed different formation scenarios of CEMP-r/s and CEMP-s stars. The absence of Tc lines and the low values of ${ }^{12} \mathrm{C} /{ }^{13} \mathrm{C}$ indicate the extrinsic nature of the programme stars. We have seen that $i$-process models of Hampel et al. (2016) can satisfactorily reproduce the observed overabundance of heavy elements in the CEMP-r/s stars. The $i$-process model (Hampel et al. 2016) with neutron density, $n \sim 10^{13} \mathrm{~cm}^{-3}, n \sim 10^{15} \mathrm{~cm}^{-3}$, and $n \sim 10^{14} \mathrm{~cm}^{-3}$ give the best fit to the observed overabundance of heavy elements in the stars HE 2144-1832, HE 0017+0055, and HE 2339-0837, respectively. Such a high neutron density explains the enhancement of both $s$ - and $r$-process elements in these stars. For HD 145777, in order to fit the observed abundances, an $i$-process model with neutron density of $10^{10} \mathrm{~cm}^{-3}$ is needed. This is towards the higher limit of the neutron density required for $s$-process nucleosynthesis. Although the Eu abundance in HD 145777 is not high enough to make it a CEMP-r/s star, Eu is still enhanced, and this enhancement can be attributed to this high neutron density.

With the help of a sample of 72 CEMP-s and CEMP-r/s stars from the literature, we have critically analysed the different criteria used by various authors for CEMP-s and CEMP-r/s stars. We have found that the set of criteria adopted by Abate et al. (2016) is suitable and fits well with the literature data. The criterion $0.0<[\mathrm{La} / \mathrm{Eu}]<0.6$ put forward by Frebel (2018) to classify CEMP-r/s stars is also found to be suitable with a slight modification to the upper limit. As [hs/ls] gives higher values for CEMP-r/s stars than CEMP-s stars, we have examined whether [hs/ls] can be used as a classifier. Even though they peak at different values of [hs/ls], CEMP-s and CEMP-r/s stars show an overlap in the range $0.0<[\mathrm{hs} / \mathrm{ls}]<1.5$. Thus, this ratio alone cannot be used as a definitive classifier of CEMP-s and CEMP-r/s stars. The best criteria to distinguish the CEMP-s and CEMP-r/s stars are found to be the following:

- CEMP: $[\mathrm{C} / \mathrm{Fe}] \geq 0.7$
- CEMP-r/s: $[\mathrm{Ba} / \mathrm{Fe}] \geq 1.0,[\mathrm{Eu} / \mathrm{Fe}] \geq 1.0$
i) $0.0 \leq[\mathrm{Ba} / \mathrm{Eu}] \leq 1.0$ and $/$ or $0.0 \leq[\mathrm{La} / \mathrm{Eu}] \leq 0.7$;
- CEMP-s: $[\mathrm{Ba} / \mathrm{Fe}] \geq 1.0$
i.) $[\mathrm{Eu} / \mathrm{Fe}]<1.0,[\mathrm{Ba} / \mathrm{Eu}]>0.0$ and $/$ or $[\mathrm{La} / \mathrm{Eu}]>0.5$;
ii.) $[\mathrm{Eu} / \mathrm{Fe}] \geq 1.0,[\mathrm{Ba} / \mathrm{Eu}]>1.0$ and $/$ or $[\mathrm{La} / \mathrm{Eu}]>0.7$.

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## Appendix A: Additional tables

Table A.1. Differential abundance $(\Delta \log \epsilon)$ of different species due to the variations in stellar atmospheric parameters for HE $2144-1832$.
$\left.\begin{array}{lccccccccccc}\hline \hline \text { Element } & \begin{array}{c}\Delta T_{\text {eff }} \\ (+100 \mathrm{~K})\end{array} & \begin{array}{c}\Delta T_{\text {eff }} \\ (-100 \mathrm{~K})\end{array} & \begin{array}{c}\Delta \log g \\ (+0.2 \mathrm{dex})\end{array} & \begin{array}{c}\Delta \log g \\ (-0.2 \mathrm{dex})\end{array} & \begin{array}{c}\Delta \zeta \\ \left(+0.2 \mathrm{~km} \mathrm{~s}^{-1}\right)\end{array} & \begin{array}{c}\Delta \zeta \\ \left(-0.2 \mathrm{~km} \mathrm{~s}^{-1}\right)\end{array} & \begin{array}{c}\Delta[\mathrm{Fe} / \mathrm{H}] \\ (+0.2 \mathrm{dex})\end{array} & \begin{array}{c}\Delta[\mathrm{Fe} / \mathrm{H}] \\ (-0.2 \mathrm{dex})\end{array} & \begin{array}{c}\left(\Sigma \sigma_{i}^{2}\right)^{1 / 2} \\ (+\Delta)\end{array} & \begin{array}{c}\left(\Sigma \sigma_{i}^{2}\right)^{1 / 2} \\ (-\Delta)\end{array} & \begin{array}{c}\sigma[\mathrm{X} / \mathrm{Fe}] \\ (+\Delta)\end{array} \\ \hline \mathrm{C}\left(\mathrm{C}_{2}, 5165 \AA \mathrm{X} / \mathrm{Fe}\right] \\ (-\Delta)\end{array}\right]$

Table A.2. CEMP-s and CEMP-r/s stars from the literature.

| CEMP-s stars |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Star Name | [ $\mathrm{Fe} / \mathrm{H}$ ] | [C/Fe] | [ $\mathrm{N} / \mathrm{Fe}$ ] | [C/N] | [St/Fe] | [Y/Fe] | [ $\mathrm{Zr} / \mathrm{Fe}$ ] | $[\mathrm{Ba} / \mathrm{Fe}]$ | [ $\mathrm{La} / \mathrm{Fe}$ ] | [ $\mathrm{Ce} / \mathrm{Fe}$ ] | [ $\mathrm{Nd} / \mathrm{Fe}$ ] | [Sm/Fe] | [ $\mathrm{Eu} / \mathrm{Fe}$ ] | $[\mathrm{Pb} / \mathrm{Fe}]$ | [1s/Fe] | [hs/Fe] | [hs/ls] | [Ba/Eu] | [Sr/Ba] | Ref. |
| BD+04 2466 | -1.99 | 1.17 | 1.10 | 0.07 | - | 0.52 | 0.79 | 1.49 | 1.20 | 1.07 | 1.35 | - | - | 1.92 | 0.66 | 1.28 | 0.62 | - | - | 32 |
|  | -1.92 | 1.17 | 1.10 | 0.07 | - | 0.47 | 0.79 | 1.70 | 1.20 | 1.07 | 1.35 | - | - | 1.92 | - | - | - | - | - | 21 |
|  | -2.10 | - | - | - | - | 0.54 | - | 1.36 | - | - | - | - | - | - | - | - | - | - | - | 12 |
|  | -1.92 | - | - | - | - | 0.55 | - | 1.31 | - | - | - | - | - | - | - | - | - | - | - | 25 |
|  | -2.00 | - | - | - | - | - | - | 1.60 | - | - | - | - | - | - | - | - | - | - | - | 33 |
| BD-01 2582 | -2.25 | - | - | - | - | - | - | 1.50 | - | - | - | - | - | - | - | - | - | - | - | 33 |
| BS 16077-0077 ${ }^{(a),(b)}$ | $-2.05{ }^{\text {c }}$ ( | 2.25 | - | - | -0.06 | -0.12 | -0.02 | 0.75 | 0.58 | 0.60 | 0.60 | - | -0.01 | - | -0.07 | 0.63 | 0.70 | 0.76 | -0.81 | 30 |
| CD-38 2151 | -1.72 | 1.50 | 1.40 | 0.10 | 1.16 | 0.44 | 1.50 | 0.97 | 1.09 | 1.30 | 1.17 | 1.07 | - | - | 1.03 | 1.13 | 0.10 | - | 0.19 | 32 |
|  | -2.03 | 1.50 | 1.40 | 0.10 | 1.16 | 0.57 | 2.00 | 0.97 | 0.88 | 1.24 | 1.34 | 1.53 | - | - | - | - | - | - | - | 19 |
|  | -1.40 | - | - | - | - | 0.30 | 1.00 | - | 1.30 | 1.35 | 1.00 | 0.61 | - | - |  |  |  |  | - | 34 |
| CS 22880-074 ${ }^{(a)}$ | -1.85 | 1.41 | 0.05 | 1.36 | 0.27 | 0.38 | 0.73 | 1.33 | 1.16 | 1.22 | 1.20 | - | 0.53 | 1.90 | 0.46 | 1.23 | 0.77 | 0.80 | -1.06 | 32 |
|  | -1.76 | 1.51 | 0.20 | 1.31 | 0.14 | 0.60 | 0.73 | 1.34 | 1.24 | - | - | - | 0.55 | , | - | - | - |  | - | 20 |
|  | -1.93 | 1.30 | -0.10 | 1.40 | 0.39 | 0.16 | - | 1.31 | 1.07 | 1.22 | 1.20 | - | 0.50 | 1.90 | - | - | - | - | - | 2 |
| CS 22942-019 | -2.66 | 2.10 | 0.50 | 1.60 | 1.55 | 1.58 | 1.69 | 1.71 | 1.53 | 1.54 | 1.26 | 1.64 | 0.80 | $\leq 1.60$ | 1.61 | 1.51 | -0.10 | 0.91 | -0.16 | 32 |
|  | -2.67 | 2.20 | 0.70 | 1.50 | 1.40 | - | - | 1.50 | 1.85 | - | - | - | 0.80 | - | - | - | - | - | - | 20 |
|  | -2.64 | 2.00 | 0.30 | 1.70 | 1.70 | 1.58 | 1.69 | 1.92 | 1.20 | 1.54 | 1.26 | 1.64 | 0.79 | $\leq 1.60$ | - | - | - | - | - | 2 |
| CS 22949-008 ${ }^{(a)}$ | $-2.45{ }^{\text {(c) }}$ | 2.00 | - | - | -0.17 | 1.25 | 1.61 | 0.98 | - | 1.49 | 1.98 | 0.61 | - | , | 0.90 | 1.48 | 0.58 | - | -1.15 | 30 |
| CS 29512-073 ${ }^{(a)}$ | $-2.06{ }^{\text {(c) }}$ | 1.40 | - | - | $0.75{ }^{(d)}$ | 0.60 | 0.59 | 1.42 | 1.42 | 1.63 | 1.57 | 1.88 | 0.37 | - | 0.65 | 1.51 | 0.86 | 1.05 | -0.67 | 30 |
| CS 30301-015 ${ }^{(a)}$ | -2.64 | 1.60 | 0.60 | 1.00 | 0.30 | 0.29 | - | 1.45 | 0.84 | 1.16 | 1.25 | 0.85 | 0.20 | 1.70 | 0.30 | 1.18 | 0.88 | 1.25 | -1.15 | 2 |
| G 18-24 | -1.62 | - | - | - | - | 0.58 | - | 1.17 | - | - | - | - | - | - | - | - | - | - | - | 12 |
| G 24-25 ${ }^{(a)}$ | -1.40 | 1.03 | - | - | $0.36{ }^{(d)}$ | 0.70 | $0.95{ }^{(d)}$ | 1.35 | 1.55 | 1.59 | 1.47 | 1.40 | 0.61 | 1.68 | 0.67 | 1.49 | 0.82 | 0.74 | -0.99 | 29 |
| HD 5223 | -2.05 | 1.57 | - | - | 1.39 | 0.63 | 1.57 | 1.82 | 1.76 | 1.87 | 1.54 | 1.68 | - | <2.21 | 1.19 | 1.75 | 0.56 | - | -0.43 | 10 |
| HD $30443{ }^{(a)}$ | -1.69 | 1.68 | 0.40 | 1.28 | 0.74 | 1.37 | 1.60 | 1.70 | - | 1.62 | 2.47 | 2.24 | - | - | 1.24 | 1.93 | 0.69 | - | -0.96 | 19 |
| HD 196944 | -2.33 | 1.31 | 1.30 | 0.01 | 0.84 | 0.57 | 0.63 | 1.27 | 0.96 | 1.20 | 0.83 | 0.69 | 0.17 | 2.00 | 0.68 | 1.07 | 0.39 | 1.10 | -0.43 | 32 |
|  | -2.45 | 1.42 | - | - | - | 0.58 | - | 1.56 | - | 1.49 | 0.94 | - | - | - |  | - | - | - | - | 24 |
|  | -2.25 | 1.20 | 1.30 | -0.10 | 0.84 | 0.56 | 0.66 | 1.10 | 0.91 | 1.01 | 0.86 | 0.78 | 0.17 | 1.90 | - | - | - | - | - | 2 |
|  | -2.23 | - | - | - | - | - | - | 1.14 | - | - | - | - | - | - | - | - | - | - | - | 16 |
|  | -2.40 | - | - | - | - | - | 0.60 | - | 1.00 | 1.10 | 0.70 | 0.60 | - | 2.10 | - |  | - | - | - | 23 |
| HD 198269 | -1.40 | - | - | - | - | 0.50 | 1.20 | - | 1.40 | 1.60 | 1.00 | 0.90 | 0.80 | - | 0.85 | 1.33 | 0.48 | - | - | 34 |
| HD 201626 | -1.35 | - | - | - | - | 1.00 | 1.30 | 2.12 | 1.68 | 1.90 | 1.97 | 1.57 | - | - | 1.15 | 1.92 | 0.77 | - | - | 32 |
|  | -1.39 | - | - | - | - | - | - | 2.12 | 1.76 | 1.89 | 2.24 | 1.63 | - | - | - | - | - | - | - | 9 |
|  | -1.30 | - | - | - | - | 1.00 | 1.30 | - | 1.60 | 1.90 | 1.70 | 1.50 | - | - | - | - | - | - | - | 34 |

Notes. ${ }^{(a)}$ Outliers of the classifier of Hansen et al. (2019). ${ }^{(b)}$ Outliers of the classifier of Frebel (2018). ${ }^{(c)}[\mathrm{Fe} / \mathrm{H}]$ is from Fe I lines. ${ }^{(d)}$ Average abundance from neutral and ionised species. ${ }^{(e)}$ Outlier of the classifier of Abate et al. (2016). ${ }^{(f)}$ Outliers of the classifier of Beers \& Christlieb (2005).

References. 1. Aoki et al. (2001), 2. Aoki et al. (2002), 3. Aoki et al. (2008), 4. Barbuy et al. (2005), 5. Barklem et al. (2005), 6. Behara et al. (2010), 7. Cohen et al. (2003), 8. Cohen et al. (2006), 9. Karinkuzhi \& Goswami (2014), 10. Goswami et al. (2006), 11. Hill et al. (2000), 12. Ishigaki et al. (2010), 13. Ivans et al. (2005), 14. Johnson \& Bolte (2002), 15. Johnson \& Bolte (2004), 16. Jonsell et al. (2005), 17. Jonsell et al. (2006), 18. Lucatello et al. (2003), 19. Purandardas et al. (2019), 20. Preston \& Sneden (2001), 21. Pereira \& Drake (2009), 22. Sivarani et al. (2004), 23. Van Eck et al. (2003), 24. Zacs et al. (1998), 25. Zhang et al. (2009), 26. Jorissen et al. (2016a), 27. this work, 28. Goswami \& Aoki (2010), 29. Liu et al. (2012), 30. Allen et al. (2012), 31. Hansen et al. (2019), 32. mean of the presented data, 33. Burris et al. (2000) 34. Vanture (1992), 35. Masseron et al. (2010), 36. Placco et al. (2013).

Table A.2. continued.

| Star Name |  | [C/Fe] | [N/Fe] |  |  |  |  | CEMP-s stars <br> [ $\mathrm{Ba} / \mathrm{Fe}$ ] |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| HE 0012-1441 | $-2.52^{(c)}$ | 1.59 | 0.64 | 0.95 | - | - | - | 1.15 | - | - | - | - | - | $<1.92$ | - | - | - | - | - | 8 |
| HE 0024-2523 ${ }^{(a)}$ | $-2.72{ }^{(c)}$ | 2.60 | 2.10 | 0.50 | 0.34 | <0.91 | <1.22 | 1.46 | 1.80 | - | - | - | <1.10 | 3.30 | - | 1.63 | - | - | -1.12 | 18 |
| HE 0202-2204 ${ }^{(a)}$ | -1.98 | 1.16 | - | - | 0.57 | 0.41 | 0.47 | 1.41 | 1.36 | 1.30 | 1.02 | 1.03 | 0.49 | - | 0.48 | 1.27 | 0.79 | 0.92 | -0.84 | 5 |
| HE 0231-4016 ${ }^{(a)}$ | -2.08 | 1.36 | - | - | 0.67 | 0.72 | - | 1.47 | 1.22 | 1.53 | 1.35 | - | - | - | 0.70 | 1.39 | 0.69 | - | -0.80 | 5 |
| HE 0253-6024 | -2.10 | 1.30 | 0.20 | 1.10 | 1.50 | 0.80 | - | 1.70 | 1.50 | 1.20 | 2.00 | - | <1.00 | - | 1.15 | 1.60 | 0.45 | - | -0.20 | 31 |
| HE 0317-4705 | -2.30 | 1.40 | 0.40 | 1.00 | 1.70 | 0.60 | - | 1.00 | 1.40 | 1.50 | 1.30 | - | <1.00 | - | 1.15 | 1.30 | 0.15 | - | 0.70 | 31 |
| HE 0336+0113 ${ }^{(e)}$ | $-2.68{ }^{\text {c }}$ c | 2.25 | 1.60 | 0.65 | 1.68 | 1.40 | - | 2.63 | 1.93 | 2.30 | 2.12 | - | 1.18 | <2.28 | 1.54 | 2.25 | 0.71 | 1.45 | -0.95 | 8 |
| HE 0430-4404 ${ }^{(a)}$ | -2.07 | 1.44 | - | - | 0.56 | 0.60 | - | 1.62 | 1.41 | - | - | - | - | - | 0.58 | 1.52 | 0.94 | - | -1.06 | 5 |
| HE 1031-0020 ${ }^{(a)}$ | $-2.86{ }^{\text {c }}$ c | 1.63 | 2.48 | -0.85 | 0.31 | 0.25 | - | 1.21 | 1.16 | 1.40 | 1.72 | - | <0.87 | 2.66 | 0.28 | 1.37 | 1.09 | - | -0.90 | 8 |
| HE 1135+0139 | -2.33 | 1.19 | - | - | 0.66 | 0.36 | 0.46 | 1.13 | 0.93 | 1.17 | 0.77 | - | 0.33 | - | 0.49 | 1.00 | 0.51 | 0.80 | -0.47 | 5 |
| HE 1152-0355 | -1.29 | 0.58 | - | - | - | 0.14 | 0.00 | 1.58 | 1.57 | - | 0.43 | 0.87 | - | - | 0.07 | 1.19 | 1.12 | - | - | 10 |
| HE 1430-1123 ${ }^{(a)}$ | -2.71 | 1.84 | - | - | 0.24 | 0.50 | - | 1.82 | - | - | 1.72 | - | - | - | 0.37 | 1.77 | 1.40 | - | -1.58 | 5 |
| HE 1434-1442 | $-2.39{ }^{\text {c }}$ c | 1.95 | 1.40 | 0.55 | - | 0.37 | - | 1.23 | - | - | 1.70 | - | - | 2.18 | - | 1.47 | - | - | - | 8 |
| HE 1443+0113 | $-2.07{ }^{\text {c }}$ c | 1.84 | - | - | - | - | - | 1.40 | - | - | - | - | - | - | - | - | - | - | - | 8 |
| HE 1509-0806 ${ }^{(a)}$ | $-2.91{ }^{(c)}$ | 1.98 | 2.23 | -0.25 | 1.12 | 0.95 | - | 1.93 | 1.67 | 1.89 | 2.18 | - | $<0.93$ | 2.61 | 1.04 | 1.92 | 0.88 | - | -0.81 | 8 |
| HE 2138-3336 ${ }^{(a)}$ | -2.79 | 2.43 | 1.66 | 0.77 | 0.27 | 0.48 | 0.81 | 1.91 | 1.60 | 1.81 | 1.57 | 1.53 | <1.09 | 3.84 | 0.52 | 1.72 | 1.20 | - | -1.64 | 36 |
| HE 2150-0825 ${ }^{(a)}$ | -1.98 | 1.35 | - | - | 0.66 | 0.85 | 0.97 | 1.70 | 1.41 | 1.48 | 1.42 | - | - | - | 0.83 | 1.50 | 0.67 | - | -1.04 | 5 |
| HE 2158-0348 ${ }^{(a)}$ | $-2.70{ }^{\text {c }}$ c | 1.87 | 1.52 | 0.35 | 0.52 | 0.87 | 1.74 | 1.59 | 1.55 | 1.89 | 1.51 | <2.40 | 0.80 | 2.60 | 1.04 | 1.64 | 0.60 | 0.79 | -1.07 | 8 |
| HE 2158-5134 | -3.00 | 2.60 | 0.80 | 1.80 | 2.60 | 1.80 | - | 2.30 | <2.00 | <2.20 | 1.80 | - | - | - | 2.20 | 2.05 | -0.15 | - | 0.30 | 31 |
| HE 2227-4044 ${ }^{(a)}$ | -2.32 | 1.67 | - | - | 0.41 | - | - | 1.38 | 1.28 | - | - | - | - | - | - | 1.33 | - | - | -0.97 | 5 |
| HE 2232-0603 ${ }^{(a)}$ | $-1.85{ }^{(c)}$ | 1.22 | 0.47 | 0.75 | 0.55 | 0.60 | - | 1.41 | 1.23 | 1.45 | - | - | - | 1.55 | 0.58 | 1.36 | 0.78 | - | -0.86 | 8 |
| HE 2240-0412 ${ }^{(a)}$ | -2.20 | 1.35 | - | - | 0.24 | - | - | 1.37 | - | - | - | - | - | - | - | - | - | - | -1.13 | 5 |
| HE 2258-4427 | -2.10 | 1.40 | -0.10 | 1.50 | 1.70 | 1.00 | - | 1.30 | 1.40 | 1.60 | 1.50 | - | 0.80 | - | 1.35 | 1.45 | 0.10 | 0.50 | 0.40 | 31 |
| HE 2339-4240 | -2.30 | 1.70 | 0.60 | 1.10 | 1.60 | 0.80 | - | 2.00 | 2.00 | 1.70 | 2.00 | - | - | - | 1.20 | 1.93 | 0.73 | - | -0.40 | 31 |
| Star Name | [Fe/H] | [ $\mathrm{C} / \mathrm{Fe}$ ] | [ $\mathrm{N} / \mathrm{Fe}$ ] | [C/N] | [Sr/Fe] | [Y/Fe] | [Zr/Fe] | CEMP-r/s stars [ $\mathrm{Ba} / \mathrm{Fe}$ ] | [ $\mathrm{La} / \mathrm{Fe}$ ] | [ $\mathrm{Ce} / \mathrm{Fe}$ ] | [ $\mathrm{Nd} / \mathrm{Fe}$ ] | [Sm/Fe] | [ $\mathrm{Eu} / \mathrm{Fe}$ ] | [ $\mathrm{Pb} / \mathrm{Fe}$ ] | [1s/Fe] | [hs/Fe] | [hs/ls] | [Ba/Eu] | [Sr/Ba] | Ref. |
| BS 16080-175 ${ }^{(b)}$ | -1.86 | 1.75 | <0.80 | - | 1.04 | 1.07 | 1.29 | 1.55 | 1.65 | - | - | - | 1.05 | 2.60 | 1.13 | 1.60 | 0.47 | 0.50 | -0.51 | 30 |
| BS 17436-058 | -1.90 | 1.50 | 1.25 | 0.25 | 0.95 | 0.73 | 0.93 | 1.61 | 1.49 | - | - | - | 1.17 | 2.26 | 0.87 | 1.55 | 0.68 | 0.44 | -0.66 | 30 |
| CD-28 $1082{ }^{(b)}$ | -2.45 | 2.19 | 2.73 | -0.54 | 1.44 | 1.61 | - | 2.09 | 1.55 | 1.97 | 1.99 | 2.29 | 2.07 | - | 1.53 | 1.90 | 0.37 | 0.02 | -0.65 | 19 |
| CS 22183-015 ${ }^{(f),(a)}$ | -2.91 | 2.13 | 1.78 | 0.35 | 0.44 | 0.50 | 0.68 | 2.01 | 1.61 | 1.72 | 1.78 | - | 1.49 | 2.99 | 0.54 | 1.78 | 1.24 | 0.52 | -1.57 | 32 |
|  | $-2.75{ }^{\text {c }}$ c | 1.92 | 1.77 | 0.15 | 0.34 | 0.52 | - | 2.04 | 1.70 | 1.88 | 1.91 | - | 1.70 | 2.79 | - | - | - | - | - | 8 |
|  | -3.12 | - | - | - | - | 0.45 | 0.62 | 2.09 | 1.59 | 1.55 | 1.65 | - | 1.39 | 3.17 | - | - | - | - | - | 14 |
|  | -2.85 | 2.34 | 1.79 | 0.55 | 0.54 | 0.54 | 0.74 | 1.89 | 1.53 | - | - | - | 1.37 | 3.00 | - | - | - | - | - | 30 |
| CS 22881-036 ${ }^{(f)}$ | -2.06 | 1.96 | 1.00 | 0.96 | 0.59 | 1.01 | 0.95 | 1.93 | 1.59 | - | 2.04 | - | 1.00 | - | 0.85 | 1.85 | 1.00 | 0.93 | -1.34 | 20 |
| CS 22887-048 (f) | -1.70 | 1.84 | <1.29 | - | 1.00 | 0.99 | 1.23 | 2.00 | 1.73 | - | - | - | 1.49 | 3.40 | 1.07 | 1.87 | 0.80 | 0.51 | -1.00 | 30 |
| CS 22898-027 ${ }^{(a)}$ | -2.23 | 2.16 | 1.11 | 1.05 | 0.70 | 0.76 | 1.23 | 2.25 | 2.20 | 2.13 | 2.12 | 2.08 | 1.91 | 2.87 | 0.90 | 2.18 | 1.28 | 0.34 | -1.55 | 32 |
|  | -2.15 | 1.95 | 1.20 | 0.75 | 0.60 | 0.95 | 1.39 | 2.27 | 2.28 | - | 2.00 | - | 1.94 | - | - | - | - | - | - | 20 |
|  | -2.30 | 2.34 | 1.24 | 1.10 | 0.59 | 0.60 | 1.28 | 2.26 | 2.19 | - | - | - | 1.91 | 2.89 | - | - | - | - | - | 30 |
|  | -2.25 | 2.20 | 0.90 | 1.30 | 0.92 | 0.73 | 1.01 | 2.23 | 2.13 | 2.13 | 2.23 | 2.08 | 1.88 | 2.84 | - | - | - | - | - | 2 |
| CS 22948-027 | -2.50 | 2.19 | 1.55 | 0.64 | 0.90 | 1.00 | - | 2.06 | 2.32 | 2.20 | 2.22 | - | 1.99 | 2.72 | 0.95 | 2.20 | 1.25 | 0.07 | -1.16 | 32 |
|  | -2.47 | 2.43 | 1.75 | 0.68 | 0.90 | 1.00 | - | 2.26 | 2.32 | 2.20 | 2.22 | - | 1.88 | 2.72 | - | - | - | - | - | 4 |
|  | -2.57 | 2.10 | 1.10 | 1.00 | - | - | - | 1.67 | - | - | - | - | - | - | - | - | - | - | - | 20 |
|  | $-2.47{ }^{\text {c }}$ c | 2.05 | 1.80 | 0.25 | 0.90 | 1.00 | - | 2.26 | 2.32 | 2.20 | 2.22 | - | 2.10 | - | - | - | - | - | - | 11 |
| CS 29497-034 | -3.00 | 2.61 | 2.16 | 0.45 | 1.20 | 0.97 | - | 2.05 | 2.25 | 2.00 | 2.16 | - | 2.03 | 2.95 | 1.09 | 2.12 | 1.03 | 0.02 | -0.85 | 32 |
|  | -2.90 | 2.63 | 2.38 | 0.25 | 1.00 | 1.10 | - | 2.03 | 2.12 | 1.95 | 2.09 | - | 1.80 | 2.95 | - | - | - | - | - | 4 |
|  | $-2.90{ }^{\text {cc }}$ | 2.50 | 2.30 | 0.20 | 1.00 | 1.10 | - | 2.03 | 2.12 | 1.95 | 2.09 | - | 2.25 | - | - | - | - | - | - | 11 |
|  | -3.20 | 2.70 | 1.80 | 0.90 | 1.60 | 0.70 | - | 2.10 | 2.50 | 2.10 | 2.30 | - | - | - | - | - | - | - | - | 31 |
| CS 29497-030 ${ }^{(f)}$ | -2.64 | 2.43 | 2.00 | 0.43 | 1.09 | 0.84 | 1.42 | 2.25 | 2.16 | 2.12 | 2.00 | - | 1.72 | 3.60 | 1.12 | 2.13 | 1.01 | 0.53 | -1.16 | 32 |
|  | -2.57 | 2.47 | 2.12 | 0.35 | 1.34 | 0.97 | 1.40 | 2.32 | 2.22 | 2.10 | 2.14 | - | 1.99 | 3.65 | - | - | - | - | - | 13 |
|  | -2.70 | 2.38 | 1.88 | 0.50 | 0.84 | 0.71 | 1.43 | 2.17 | 2.10 | 2.14 | 1.85 | - | 1.44 | 3.55 | - | - | - | - | - | 22 |
| CS 29503-010 | $-1.69{ }^{\text {c }}$ c | 1.65 | - | - | $1.13{ }^{(d)}$ | 1.09 | 1.26 | 1.81 | 2.16 | 2.05 | 2.31 | 2.34 | 1.69 | - | 1.16 | 2.08 | 0.92 | 0.12 | -0.68 | 30 |
| CS 29526-110 ${ }^{(a)}$ | -2.21 | 2.22 | 1.40 | 0.82 | 0.65 | 1.32 | 1.39 | 2.26 | 2.12 | 2.15 | 2.10 | - | 2.01 | 3.23 | 1.12 | 2.16 | 1.04 | 0.25 | -1.61 | 32 |
|  | -2.07 | 2.07 | - | - | 0.77 | 1.34 | 1.26 | 2.39 | 2.09 | - | - | - | - | 3.16 | - | - | - | - | - |  |
|  | -2.38 | 2.20 | 1.40 | 0.80 | 0.88 | - | 1.11 | 2.11 | 1.69 | 2.01 | 2.01 | - | 1.73 | 3.30 | - | - | - | - | - | 2 |
|  | $-2.19{ }^{\text {c }}$ c | 2.38 | - | - | 0.29 | 1.29 | 1.79 | 2.29 | 2.57 | 2.29 | 2.19 | - | 2.28 | - | - | - | - | - | - | 30 |
| CS 29528-028 | -2.12 ${ }^{\text {c }}$ c | 2.76 | - | - | $1.72{ }^{(d)}$ | 1.99 | 2.17 | 2.49 | 2.21 | 2.47 | 2.54 | - | 2.16 | - | 1.96 | 2.43 | 0.47 | 0.33 | -0.77 | 30 |
| CS 31062-050 ${ }^{(a),(f)}$ | -2.37 | 1.91 | 1.20 | 0.71 | 0.91 | 0.48 | 0.94 | 2.55 | 2.28 | 2.06 | 2.12 | 2.06 | 1.82 | 2.86 | 0.78 | 2.25 | 1.47 | 0.73 | -1.64 | 32 |
|  | -2.41 | 1.82 | - | - | - | 0.48 | 0.85 | 2.80 | 2.12 | 2.02 | 1.99 | 1.96 | 1.79 | 2.81 | - | - | - | - | - | 15 |
|  | -2.32 | 2.00 | 1.20 | 0.80 | 0.91 | - | 1.02 | 2.30 | 2.44 | 2.10 | 2.24 | 2.15 | 1.84 | 2.90 | - | - | - | - | - | 2 |
| HD 187861 | -2.01 | 2.02 | 2.18 | -0.16 | - | 0.00 | - | 1.39 | 1.89 | 1.69 | 1.80 | 0.70 | 1.34 | 2.86 | - | 1.70 | - | 0.05 | - | 32 |
|  | -1.65 | - | - | - | - | 0.00 | - | - | 2.05 | 2.00 | 1.80 | 0.70 | - | - | - | - | - | - | - | 34 |
|  | -2.36 | 2.02 | 2.18 | -0.16 | - | - | - | 1.39 | 1.73 | 1.37 | - | - | 1.34 | 2.86 | - | - | - | - | - | 35 |
| HD $209621^{(b)}$ | -1.42 | 1.25 | - | - | 1.02 | 0.73 | 1.80 | 1.70 | 2.41 | 2.42 | 2.14 | 1.46 | 1.35 | 1.88 | 1.18 | 2.17 | 0.99 | 0.35 | -0.68 | 32 |
|  | -1.93 | 1.25 | - | - | 1.02 | 0.36 | 1.80 | 1.70 | 2.41 | 2.04 | 1.87 | 1.46 | 1.35 | 1.88 | - | - | - | - | - | 28 |
|  | -0.90 | - | - | - | - | 1.10 | - | - | - | 2.80 | 2.40 | - | - | - | - | - | - | - | - | 34 |
| HD 224959 | -1.83 | 1.77 | 1.88 | -0.11 | - | 0.80 | - | 2.19 | 2.02 | 2.01 | 1.80 | 1.40 | 1.74 | 3.06 | - | 2.01 | - | 0.45 | - | 32 |
|  | -1.60 | - | - | - | - | 0.80 | - | - | 2.00 | 2.10 | 1.80 | 1.40 | - | - | - | - | - | - | - | 34 |
|  | -2.06 | 1.77 | 1.88 | -0.11 | - | - | - | 2.19 | 2.03 | 1.91 | - | - | 1.74 | 3.06 | - | - | - | - | - | 35 |
| HE 0002-1037 | -2.40 | 1.90 | 1.00 | 0.90 | <1.00 | 0.40 | - | 2.00 | 2.00 | 1.70 | 2.10 | - | 1.70 | - | - | 1.95 | - | 0.30 | - | 31 |
| HE 0017+0055 | -2.40 | 2.17 | 2.47 | -0.30 | , | 0.50 | 1.60 | >1.90 | 2.40 | 2.00 | 2.20 | 1.90 | 2.30 | - | 1.05 | 2.20 | 1.15 | - | - | 26 |
| HE 0059-6540 | -2.20 | 1.30 | 1.20 | 0.10 | 1.20 | 0.40 | - | 1.70 | 1.60 | 1.40 | 1.70 | - | 1.50 | - | 0.80 | 1.60 | 0.80 | 0.20 | -0.50 | 31 |
| HE 0131-3953 ${ }^{(a),(f)}$ | -2.71 | 2.45 | - | - | 0.46 | - | - | 2.20 | 1.94 | 1.93 | 1.76 | - | 1.62 | - | - | 1.96 | - | 0.58 | -1.74 | 5 |
| HE 0143-0441 ${ }^{(f)}$ | $-2.31{ }^{\text {(c) }}$ | 1.98 | 1.73 | 0.25 | 0.86 | 0.59 | 1.05 | 2.32 | 1.78 | 1.93 | 2.17 | - | 1.46 | 3.11 | 0.83 | 2.05 | 1.22 | 0.86 | -1.46 | 8 |
| HE 0151-6007 | -2.70 | 1.40 | 0.20 | 1.20 | 1.10 | 0.80 | - | 2.30 | 2.50 | 2.40 | 2.60 | - | 2.30 | - | 0.95 | 2.45 | 1.50 | 0.00 | -1.20 | 31 |
| HE 0338-3945 ${ }^{(a)}$ | -2.42 | 2.10 | 1.55 | 0.55 | 0.74 | 0.78 | 1.20 | 2.41 | 2.27 | 2.19 | 2.20 | 2.25 | 1.92 | 3.10 | 0.91 | 2.27 | 1.36 | 0.49 | -1.67 | 32 |
|  | -2.41 | 2.07 |  | - | 0.73 | 0.73 | - | 2.41 | 2.26 | 2.21 | 2.09 | , | 1.89 | 10 | - | - | - | - | - | 5 |
|  | -2.42 | 2.13 | 1.55 | 0.58 | 0.74 | 0.83 | 1.20 | 2.41 | 2.28 | 2.16 | 2.30 | 2.25 | 1.94 | 3.10 | - | - | - | - | - | 17 |
| HE 1105+0027 ${ }^{(a)(f)}$ | -2.42 | 2.00 | - | - | 0.73 | 0.75 | - | 2.45 | 2.10 | - | 2.06 | - | 1.81 | - | 0.74 | 2.20 | 1.46 | 0.64 | -1.72 | 5 |
| HE 1305+0007 | -2.01 | 1.84 | - | - | 0.86 | 0.73 | 2.09 | 2.32 | 2.56 | 2.53 | 2.59 | 2.60 | 1.97 | 2.37 | 1.23 | 2.50 | 1.27 | 0.35 | -1.46 | 10 |
| HE 2148-1247 ${ }^{(a)}$ | -2.26 | 1.91 | 1.65 | 0.26 | 0.76 | 0.83 | 1.47 | 2.36 | 2.38 | 2.28 | 2.27 | 1.99 | 1.98 | 3.12 | 1.02 | 2.32 | 1.30 | 0.38 | -1.60 | 7 |
| HE 2258-6358 ${ }^{(f)}$ | -2.67 | 2.42 | 1.44 | 0.98 | 0.80 | 0.70 | 0.69 | 2.23 | 1.91 | 1.66 | 1.76 | 1.81 | 1.68 | 3.32 | 0.73 | 1.89 | 1.16 | 0.55 | -1.43 | 36 |
| LP 625-44 ${ }^{(a)(f)}$ | -2.71 | 2.10 | 1.00 | 1.10 | 1.15 | 0.99 | 1.34 | 2.74 | 2.46 | 2.27 | 2.30 | 2.21 | 1.97 | 2.55 | 1.16 | 2.44 | 1.28 | 0.77 | -1.59 | 1 |
| LP 706-7 ${ }^{(a),(f)}$ | -2.61 | 2.13 | 1.50 | 0.63 | 0.18 | 0.42 | <1.16 | 2.02 | 1.92 | 1.99 | 1.90 | <2.21 | 1.51 | 2.40 | 0.30 | 1.96 | 1.66 | 0.51 | -1.84 | 32 |
|  | -2.53 | 2.14 | - | - | 0.08 | - | - | 2.08 | 1.92 | - | - | - | - | 2.53 | - | - | - | - | - | 3 |
|  | -2.55 | 2.10 | 1.20 | 0.90 | 0.30 | 0.59 | - | 1.98 | 2.02 | 2.12 | 1.79 | - | 1.62 | 2.40 | - | - | - | - | - | 2 |
|  | -2.74 | 2.15 | 1.80 | 0.35 | 0.15 | 0.25 | <1.16 | 2.01 | 1.81 | 1.86 | 2.01 | <2.21 | 1.40 | 2.28 | - | - | - | - | - | 1 |
| SDSS J0912+0216 | -2.50 | 2.17 | 1.75 | 0.42 | 0.57 | 0.61 | 1.08 | 1.49 | 1.35 | 2.17 | 1.12 | 2.60 | 1.20 | 2.33 | 0.75 | 1.53 | 0.78 | 0.29 | -0.92 | 6 |
| SDSS J1349-0229 (f) | -3.00 | 2.82 | 1.60 | 1.22 | 1.30 | 1.29 | 1.56 | 2.17 | 1.74 | 2.63 | 1.91 | 2.35 | 1.6 | 3.09 | 1.3 | 2.11 | 0.7 | 0.5 | -0.87 | 6 |
| Star Name | [ $\mathrm{Fe} / \mathrm{H}$ ] | [ $\mathrm{C} / \mathrm{Fe}$ ] | [ $\mathrm{N} / \mathrm{Fe}$ ] | [C/N] | [Sr/Fe] | [Y/Fe] | [ $\mathrm{Zr} / \mathrm{Fe}$ ] | Our Work $[\mathrm{Ba} / \mathrm{Fe}]$ | [ $\mathrm{La} / \mathrm{Fe}$ ] | [ $\mathrm{Ce} / \mathrm{Fe}$ ] | [ $\mathrm{Nd} / \mathrm{Fe}$ ] | [Sm/Fe] | [ $\mathrm{Eu} / \mathrm{Fe}$ ] | [Pb/Fe] | [1s/Fe] | [hs/Fe] | [hs/ls] | [Ba/Eu] | [Sr/Ba] | Ref |
| HD $145777{ }^{(a),(b),(f)}$ | -2.17 | 2.43 | 0.67 | 1.76 | 0.67 | 1.22 | 1.05 | 1.27 | 1.37 | 1.79 | 1.48 | 1.63 | 0.80 | - | 0.98 | 1.48 | 0.50 | 0.47 | -0.60 | 27 |
| CD-27 14351 | -2.71 | 2.98 | 1.88 | 1.10 | 1.74 | 1.97 | 2.21 | 1.82 | 1.56 | 1.89 | 1.37 | - | $<0.39$ | - | 1.97 | 1.66 | -0.31 | >1.43 | -0.08 | 27 |
| HE 0017+0055 | -2.46 | 2.73 | 2.83 | -0.10 | - | 0.58 | 1.55 | 2.30 | 2.46 | 2.11 | 2.25 | 1.98 | 2.14 | - | 1.07 | 2.28 | 1.21 | 0.16 | - | 27 |
| HE 2144-1832 | -1.63 | 1.85 | 0.50 | 1.35 | 0.66 | 1.16 | 0.97 | 1.49 | 1.53 | 1.70 | 1.61 | 1.78 | 1.01 | - | 0.93 | 1.58 | 0.65 | 0.48 | -0.83 | 27 |
| HE 2339-0837 | -2.74 | 3.04 | - | - | 1.32 | 0.67 | 1.64 | 2.21 | 2.24 | 2.37 | 2.55 | 2.29 | 1.84 | - | 1.21 | 2.34 | 1.13 | 0.37 | -0.89 | 27 |


[^0]:    * Full Tables 4 and 6 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via http://cdsarc. u-strasbg.fr/viz-bin/cat/J/A+A/649/A49
    *» Based [in part] on data collected at Subaru Telescope, which is operated by the National Astronomical Observatory of Japan.
    **ᄎ [Part of] the data are retrieved from the JVO portal (http: //jvo. nao.ac.jp/portal) operated by the NAOJ.

[^1]:    ${ }^{1}$ Notation: $[\mathrm{A} / \mathrm{B}]=\log \left(N_{\mathrm{A}} / N_{\mathrm{B}}\right)_{*}-\log \left(N_{\mathrm{A}} / N_{\mathrm{B}}\right)_{\odot}$, where $N_{\mathrm{A}}$ and $N_{\mathrm{B}}$ are number densities.

[^2]:    2 http://jvo.nao.ac.jp/portal

[^3]:    3 http://kurucz.harvard.edu/grids.html

[^4]:    4 http://www.as.utexas.edu/~chris/moog.html
    5 http://kurucz.harvard.edu/grids.html

[^5]:    6 linemake contains laboratory atomic data (transition probabilities, hyperfine and isotopic substructures) published by the Wisconsin Atomic Physics and the Old Dominion Molecular Physics groups. These lists and accompanying line list assembly software have been developed by C. Sneden and are curated by V. Placco at https://github. com/ vmplacco/linemake.

