

Physical Properties of the Very Young PN Hen3-1357 (Stingray Nebula) Based on Multiwavelength Observations

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Abstract

We carried out a detailed analysis of the interesting and important very young planetary nebula (PN) Hen3-1357 (Stingray Nebula) based on a unique data set of optical to far-IR spectra and photometric images. We calculated the abundances of nine elements using collisionally excited lines (CELs) and recombination lines (RLs). The RL C/O ratio indicates that this PN is O-rich, which is also supported by the detection of the broad $9/18~\mu m$ bands from amorphous silicate grains. The observed elemental abundances can be explained by asymptotic giant branch (AGB) nucleosynthesis models for initially $1-1.5~M_{\odot}$ stars with Z=0.008. The Ne overabundance might be due to the enhancement of 22 Ne isotope in the He-rich intershell. Using the spectrum of the central star synthesized by Tlusty as the ionization/heating source of the PN, we constructed the self-consistent photoionization model with Cloudy to the observed quantities and derived the gas and dust masses, dust-to-gas mass ratio, and core mass of the central star. About 80% of the total dust mass is from warm–cold dust component beyond ionization front. Comparison with other Galactic PNe indicates that Hen3-1357 is an ordinary amorphous silicate-rich and O-rich gas PN. Among other studied PNe, IC4846 shows many similarities in properties of the PN to Hen3-1357, although their post-AGB evolution is quite different from each other. Further monitoring of observations and comparisons with other PNe such as IC4846 are necessary to understand the evolution of Hen3-1357.

Key words: dust, extinction – ISM: abundances – planetary nebulae: individual (Hen3-1357)

1. Introduction

Planetary nebula (PN) is the next evolutionary stage of asymptotic branch (AGB) stars. PNe consist of a dusty nebula and a hot central star that is evolving toward a white dwarf. So far, over 1000 PNe in the Galaxy have been identified (e.g., Frew 2008). Among PNe, Hen3-1357 (SAO244567, V839 Ara, PN G331.3-12.1, Stingray Nebula; Bobrowsky et al. 1998) has recently attracted much attention and has been studied actively since its first classification as a post-AGB star by Parthasarathy & Pottasch (1989).

Parthasarathy et al. (1993, 1995) discovered that Hen3-1357 has a young nebula and is going on post-AGB evolution; the UV spectrum of the 1988 study shows the P-Cygni profiles of the N v 1239/43 Å and C IV 1548/50 Å lines detected in the spectra, taken by the *International Ultraviolet Explore (IUE)*, and the optical spectra from 1990 and 1992 show many nebular emission lines. Hen3-1357 is the first object evolving from a B1 type post-AGB supergiant into a PN within an extremely short timescale.

Using a distance of 5.6 kpc based on an extinction estimate from UBV photometry by Kozok (1985), Parthasarathy et al. (1993) estimated the luminosity of the central star to be $3000\,L_{\odot}$. Parthasarathy et al. (1995) found that the effective temperature $(T_{\rm eff})$ of the central star has increased from 37,500 K to 47,500 K during the same period. Later, Parthasarathy et al. (1997) estimated that $T_{\rm eff}=50\,000\,{\rm K}$ in 1995. A core mass versus luminosity relation suggests the core mass is $0.55\,M_{\odot}$, while the luminosity had faded by a factor of three in UV wavelength from 1988 to 1996 (Parthasarathy 2006). Increasing $T_{\rm eff}$ as the UV flux fades indicates a dropping luminosity, resulting that Hen3-1357 is rapidly evolving toward a white dwarf.

However, it is difficult to explain its evolution and evolutionary timescale. Parthasarathy et al. (1993) estimated a kinematical age to be ~2700 years by adopting the distance of 5.6 kpc, the (bright rim) radius of 0."8 measured using the *Hubble Space Telescope (HST)* image (Bobrowsky 1994), and an expansion velocity of 8 km s⁻¹ (Parthasarathy et al. 1993). According to the H-burning post-AGB evolution for initially 1.5 M_{\odot} stars with metallicity Z=0.016 (Vassiliadis & Wood 1994), such stars would take over 10^4 years to evolve into the white dwarf cooling track. The discrepancy between the observationally estimated and the model-predicted timescale suggests that Hen3-1357 might have experienced an extraordinary post-AGB evolution.

Reindl et al. (2014) demonstrated that Hen3-1357 has steadily increased its $T_{\rm eff}$ from 38,000 K in 1988 to a peak value of 60,000 K in 2002 and cooled again to 55,000 K in 2006 based on the stellar UV spectra. They proposed late He-flash evolution to explain this rapid $T_{\rm eff}$ increment. Reindl et al. (2017) found that $T_{\rm eff}$ further cooled down 50,000 K in 2015 using the newly obtained the HST UV spectra of the central star. Such a $T_{\rm eff}$ variation is found by Arkhipova et al. (2013), who estimated that $T_{\text{eff}} = 57,000 \text{ K}$ in 1990, 55,000 K in 1992, and 41,000 K in 2011 using the [O III] 5007 A line intensities relative to $H\beta$. Through a comparison with a theoretically calculated late thermal pulse (LTP) evolutionary path, Reindl et al. (2017) concluded that Hen3-1357 might have experienced an LTP. As Reindl et al. (2017) noted, however, any theoretical LTP model cannot yet fully reproduce the observed parameters of the central star of Hen3-1357.

Despite many efforts, the puzzling evolution of Hen3-1357 remains a fatal and challenging problem. For understanding Hen3-1357, properties of the nebula are crucial because the

Table 1Observation log for Hen3-1357

Telescope/Instrument	Obs-Date
Spitzer/IRS	2005 Mar 20
MPG ESO 2.2 m/FEROS	2006 Apr 16
AKARI/IRC and FIS	2006 Dec 31
Spitzer/IRAC	2009 Apr 22

evolutionary history of the progenitor star has been imprinted in the nebula, as well. Utilizing nebular emission lines, one can easily derive elemental abundances such as C/N/O/Ne, which are essential key elements to prove AGB nucleosynthesis. The C/O ratio and the dust features seen in mid-IR spectra would suggest how much mass of the progenitor has gone into the formation of the nebula. It is of interest to investigate the conditions of the gas and dust and derive their masses in terms of material recycling in the Galaxy. Thus, nebula analysis is complementary for stellar analysis, and properties of the nebula can be the basis for understanding both the PN and its central star.

From these reasons, we investigated properties of the nebula based on a unique data set from UV to far-IR wavelengths $(0.35-140 \,\mu\text{m})$. This paper is organized as follows. In Section 2, we describe our optical high-dispersion spectroscopy using the Fiber-fed Extended Range Optical Spectrograph (FEROS: Kaufer et al. 1999) attached to the MPG ESO 2.2 m telescope and the archival mid-IR and far-IR data taken by the AKARI and *Spitzer* infrared space telescopes. In Section 3, we describe nebular abundance analysis. We first report the C/O and N/O ratios using the recombination lines of these elements in this PN. We compare the observed abundances with the AGB nucleosynthesis models to investigate the initial mass of the progenitor star. In Section 4, we construct the spectral energy distribution (SED) model using photoionization code Cloudy (Ferland et al. 2013, version C13.03) to investigate physical conditions of the nebula and the central star of PN (CSPN). We measure broadband magnitudes of the CSPN from the FEROS spectrum. We have a brief discussion on the CSPN's SED. In Section 5, we compare the observed elemental abundances and dust features with those of other PNe in order to verify Hen3-1357 as a PN. In Section 6, we summarize our work.

2. Observations and Data Reduction

We describe the photometric and spectroscopic data set taken by *Spitzer*, *AKARI*, and our FEROS observations. The observation log is summarized in Table 1. The *AKARI* data were obtained in 2006 May 6–2007 August 28, the middle date is around 2006 December 31.

2.1. Spitzer and AKARI Photometry

We measured the mid-IR flux densities for Bands 1-4 of the Spitzer/Infrared Array Camera (IRAC; Fazio et al. 2004), where the central wavelengths (λ_c) are 3.6, 4.5, 5.8, and 8.0 μ m, respectively. We reduced the basic calibrated data (BCD, program ID: 50116, obs AORKEY: 25445376, PI: G. Fazio) using mosaicking and point-source extraction software (MOPEX)⁵ provided by the Spitzer Science Center (SSC)

to create a mosaic image for each band. We subtracted artificial features seen in the images as best as possible. After we subtracted out surrounding stars by point-spread function fittings using the DIGIPHOT photometry package in IRAF v.2.16, 6 we performed aperture photometry. The results are summarized in Table 2.

To trace the amorphous silicate feature seen in the *Spitzer/IRS* spectrum, we used the *AKARI* Infrared Camera (IRC; Onaka et al. 2007) S9W ($\lambda_c = 9~\mu \text{m}$) and L18W ($\lambda_c = 18~\mu \text{m}$). We used the *AKARI* Far-Infrared Surveyor (FIS; Kawada et al. 2007) data as vital constraints to the warm-cold dust continuum in the SED modeling. For this end, we utilized the photometry measurements by Yamamura et al. (2010) for the IRC two bands and FIS Bright Source Catalog Ver.2 for the FIS-N60, WIDE-S, and WIDE-L bands at $\lambda_c = 65$, 90, and 140 μm , respectively. These data were taken by the *AKARI* all-sky survey. We list these flux densities in Table 2, where A(-B) means $A \times 10^{-B}$ hereafter.

2.2. MPG ESO 2.2 m FEROS Spectroscopy

We secured the optical high-dispersion spectrum (3500–9200 Å) using the FEROS attached to the MPG ESO 2.2 m Telescope, La Silla, Chile (Prop.ID: 77.D-0478A, PI: M. Parthasarathy).

The weather condition was stable and clear throughout the night, and the seeing was 0".8–1".17 (average: 0".97) measured from the differential image motion monitor. FEROS's fibers use 2"0 apertures and provide simultaneously the object and sky spectra. The detector is the EEV CCD chip with 2048×4096 pixels of $15 \times 15 \,\mu\mathrm{m}$ square. We selected a 1×1 on-chip binning and low gain mode. The atmospheric dispersion corrector (ADC) was not used during the observation. The exposure time was a single 2100 sec at an airmass of 1.297–1.380. For the flux calibration and blaze function correction, we observed the standard star HR 3454 (Hamuy et al. 1992, 1994) at airmass \sim 1.2. Since we did not use the ADC, a color-dependent displacement of the source from differential atmospheric refraction (DAR) might be present. However, we took the data of the Stingray nebula and HR 3454 to be at a similar airmass. Therefore, we believe that the DAR effect on the inferred extinction coefficients, the derived electron temperatures, and therefore on the derived ionic and elemental abundances would be largely reduced. We reduced the data with the echelle spectra reduction package ECHELLE in IRAF using a standard reduction manner including bias subtraction, removing scattered light, detector sensitivity correction, removing cosmic-ray hits, airmass extinction correction, flux-density calibration, and an all echelle order connection. Using the sky spectrum, we subtracted the sky lines from the Hen3-1357 spectrum. The average resolving power $(\lambda/\Delta\lambda)$ is 44,950, which was measured from the average full width at half maximum (FWHM) of over 300 Th-Ar comparison lines obtained for the wavelength calibrations. The signal-to-noise ratios per pixel were \sim 2–12 for the continuum.

 $^{^{5} \ \, \}text{http://irsa.ipac.caltech.edu/data/SPITZER/docs/dataanalysistools/tools/mopex/}$

⁶ IRAF is distributed by the National Optical Astronomy Observatories, operated by the Association of Universities for Research in Astronomy (AURA), Inc., under a cooperative agreement with the National Science Foundation. http://iraf.noao.edu.

 $^{^{7}}$ We measured the gain = $4.99 e^{-}$ ADU $^{-1}$ and readout-noise = $8.31 e^{-}$ using the IRAF task FINDGAIN.

Table 2Near- to Far-IR-Band Flux Densities of Hen3-1357

$\lambda_{\rm c}$ (μ m)	Tele/Instr/Band	$F_{ u}$ (mJy)	$(\operatorname{erg} \operatorname{s}^{-1} \overset{F_{\lambda}}{\operatorname{cm}^{-2}} \mu \operatorname{m}^{-1})$
3.6	Spitzer/IRAC/Band1	$1.09(+1) \pm 5.22(-1)$	$2.58(-12) \pm 1.24(-13)$
4.5	Spitzer/IRAC/Band2	$1.61(+1) \pm 5.02(-2)$	$2.38(-12) \pm 7.42(-15)$
5.8	Spitzer/IRAC/Band3	$1.08(+1) \pm 1.68(-1)$	$9.87(-13) \pm 1.53(-14)$
8.0	Spitzer/IRAC/Band4	$3.97(+1) \pm 8.20(-1)$	$1.89(-12) \pm 3.91(-14)$
9.0	AKARI/IRC/S9W	$8.87(+1) \pm 8.62(0)$	$3.13(-12) \pm 3.04(-13)$
65.0	AKARI/FIS/N60	$2.25(+3) \pm 3.52(+2)$	$1.60(-12) \pm 2.50(-13)$
90.0	AKARI/FIS/WIDE-S	$1.88(+3) \pm 5.06(+1)$	$6.98(-13) \pm 1.87(-14)$
140.0	AKARI/FIS/WIDE-L	$3.77(+2) \pm 2.75(+2)$	$5.77(-14) \pm 4.21(-14)$

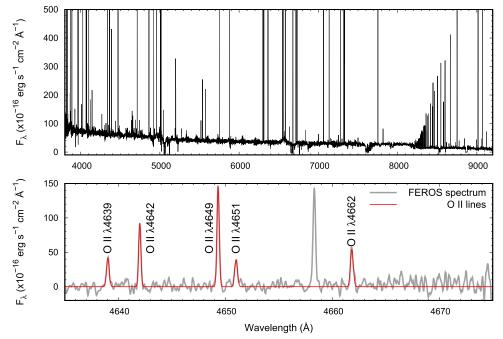


Figure 1. (Upper panel) FEROS spectrum of Hen3-1357 in the range between 3800 Å and 9200 Å. (Lower panel) FEROS spectrum in 4635-4675 Å (gray line) and the Gaussian fitting results for the O II lines in this wavelength range (red line). The local continuum was subtracted out.

The resultant FEROS spectrum is presented in Figure 1; the detected recombination lines (RLs) of O II are shown in the lower panel. As far as we know, the N and O RLs such as N II and O II are detected in this PN for the first time.

2.3. Spitzer/IRS Spectrum

To investigate dust features and perform plasma diagnostics using fine-structure lines, we analyzed the mid-IR spectra taken by the *Spitzer/*Infrared Spectrograph (IRS; Houck et al. 2004) with the Short-Low (SL, 5.2–14.5 μm , the slit dimension: $\sim\!3\rlap.{''}6\times57\rlap.{''})$, Short-High (SH, 9.9–19.6 μm , $4\rlap.{''}7\times11\rlap.{''}3)$, and Long-High modules (LH, 18.7–37.2 μm , $11\rlap.{''}1\times22\rlap.{''}3)$.

We processed the BCD (program ID: 3633, obs AORKEY: 11312640, PI: B. Matthew) using the data reduction packages SMART v.8.2.9 (Higdon et al. 2004) and IRSCLEAN v.2.1.18 provided by the SSC. We scaled the flux density of the reduced LH spectrum to match with that of the reduced SH spectrum in the overlapping wavelength and we obtained the single $9.9-37.2~\mu m$ spectrum. Then, using a similar method, we

combined this high-dispersion spectrum and the SL 5.2–14.5 μ m spectrum into the single 5.2–37.2 μ m spectrum.

We present the resultant spectrum in Figure 2. The intensity peak positions of the identified atomic lines are marked by the vertical lines. We detected Ne, S, and Ar fine-structure lines. The spectrum clearly shows two broad features (indicated by the horizontal red lines) attributed to amorphous silicate grains; the features centered at 9 μ m and 18 μ m are due to the Si-O stretching mode and the O-Si-O bending mode, respectively. Perea-Calderón et al. (2009) reported that this PN is an O-rich dust object. We did not identify any carbon-based dust grains and molecules in the *Spitzer/IRS* spectrum. Thus, we can conclude that Hen3-1357 has an O-rich dust nebula.

3. Results

3.1. Scaling the Flux Density of the Spitzer/IRS Spectrum

We performed a correction to recover the loss of light from Hen3-1357 by the slit.

First, using the AKARI/IRC 9.0 μm band photometry listed in Table 2, we scaled the flux density of the spectrum by considering the AKARI/IRC 9.0 μm filter transmission curve by a constant scaling factor of 0.951. Next, using this scaled

http://irsa.ipac.caltech.edu/data/SPITZER/docs/dataanalysistools/tools/irsclean/

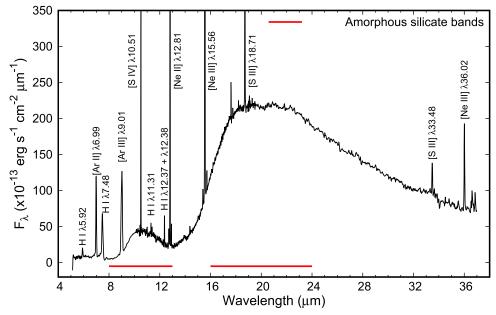


Figure 2. Spitzer/IRS spectrum of Hen3-1357. The identified atomic lines and amorphous silicate features are denoted.

spectrum and the *Spitzer/IRAC* 8.0 μ m filter transmission curve, we measured the *Spitzer/IRAC* 8.0 μ m band flux density. The measured value 1.90(-12) erg s⁻¹ cm⁻² μ m⁻¹ is consistent with the IRAC 8.0 μ m photometry result.

AKARI/IRC 9.0 μ m and Spitzer/IRAC 8.0 μ m bands include atomic lines of H, Ne, S, and Ar certainly contributing to these two bands. As noted in Section 3.4, we did not find a significant difference between optical nebular line intensities relative to the H β measured in 2006 and in 2011. This means that the ionization and elemental abundances of the nebula might not have changed between 2006 and 2011.

Our adopted scaling factor (0.951) indicates that the IR-band flux decreased by $\sim 5\%$ between 2005 and 2009. Therefore, we assume that the mid-IR wavelength evolution had not dramatically changed between 2005 and 2009.

Taking into account these analyses, we scaled the flux density of the spectrum to match the $AKARI/IRC~9.0~\mu m$ band flux density.

3.2. The $H\beta$ Flux of the Entire Nebula

The H β flux of the entire nebula is necessary for setting the nebula's hydrogen density structure in our SED modeling as well as for calculating the Ne^{+,2+}, S^{2+,3+}, and Ar^{+,2+} to H⁺ number density ratios and electron density $n_{\rm e}$ and temperature $T_{\rm e}$ using mid-IR fine-structure lines of these ions.

Since the H I 7.46 μ m line is in the longer wavelength edge of the SL2 spectrum (5.13–7.60 μ m) and also in the shorter edge of the SL1 spectrum (7.46–14.29 μ m), we did not employ this line for estimating the H β line flux of the entire nebula. Therefore, we obtained the H β line flux by utilizing the theoretical H I I(n=7-6 and 11–8)/I(n=4-2) intensity ratio calculated by Storey & Hummer (1995), where n is the principal quantum number. Note that a detected line at 12.37 μ m (see Figure 2) indeed is composed of H I n=7-6 at 12.37 μ m and n=11-8 at 12.38 μ m. From the $I(12.37 \,\mu$ m + 12.38 μ m)/ $I(H\beta) = 1.04(-2)$ in the case of an $n_e = 10^4$ cm⁻³ and a $T_e = 10^4$ K (Storey & Hummer 1995), we estimated the H β flux of the entire nebula to be 9.83 $(-12) \pm 7.33(-13)$ erg s⁻¹ cm⁻².

Table 3 Derived $c(H\beta)$ Ratios

$\lambda_{\text{lab.}}$ (Å)	Line	$c(H\beta)$
3797.9	B10	$8.25(-2) \pm 6.43(-3)$
3835.4	В9	$3.25(-2) \pm 5.17(-3)$
3970.1	B7	$7.39(-2) \pm 2.95(-3)$
4101.7	В6	$4.38(-1) \pm 3.56(-3)$
4340.5	B5	$1.34(-1) \pm 5.16(-3)$
8545.4	P15	$2.03(-2) \pm 1.04(-2)$
8598.4	P14	$3.84(-2) \pm 2.54(-3)$
8665.0	P13	$7.49(-2) \pm 2.48(-3)$
8750.5	P12	$6.64(-2) \pm 1.98(-3)$
9014.9	P10	$1.18(-2) \pm 2.25(-3)$

Note. For the interstellar reddening correction to the FEROS spectrum, we adopted the average $c(H\beta) = 8.27(-2) \pm 3.47(-2)$.

3.3. Flux Measurements

We measured the fluxes of the emission lines by Gaussian fittings and then corrected these fluxes using the formula

$$I(\lambda) = F(\lambda) \cdot 10^{c(H\beta)(1+f(\lambda))}, \tag{1}$$

where $I(\lambda)$ is the de-reddened line flux, $F(\lambda)$ is the observed line flux, $f(\lambda)$ is the interstellar extinction function at λ computed by the reddening law of Cardelli et al. (1989) with $R_V = 3.1$, and $c(H\beta)$ is the reddening coefficient at $H\beta$.

We measured $c(H\beta)$ values by comparing the observed 10 Balmer and Paschen line ratios to $H\beta$ with the theoretical ratios of Storey & Hummer (1995) for a $T_e = 10^4$ K and an $n_e = 10^4$ cm⁻³ under the Case B assumption. To reduce the $c(H\beta)$ estimation errors originated from the H I absorptions in the flux standard star HR 3454, we estimated $c(H\beta)$ using different line ratios. The derived $c(H\beta)$ values are listed in Table 3. Since the $H\alpha$ line was saturated, we did not calculate $c(H\beta)$ using the $F(H\alpha)/F(H\beta)$ ratio. Finally, we adopted the average $c(H\beta) = 8.27(-2) \pm 3.47(-2)$. The scatter between the estimated $c(H\beta)$ could be due to the H I absorptions' depth of HR 3454 measured by Hamuy et al. (1992, 1994). We did not correct interstellar extinction for the

Spitzer/IRS spectrum because the extinction is negligibly small in the mid-IR wavelength.

For the year 2006, Reindl et al. (2014) reported E(B-V)=0.11, corresponding to $c(H\beta)=0.16$. Although they did not give the uncertainty of E(B-V), we assume $\delta E(B-V)=0.02$ from the fact that they measured $E(B-V)=0.14\pm0.02$ in the year 1997. Thus, their $c(H\beta)$ for the year 2006 is estimated to be 0.16 ± 0.03 , which is consistent with ours.

In Table 13, we list 180 nebular lines detected in the FEROS spectrum. Since the [O III] 5007 Å and H α lines were saturated, we do not list their fluxes. We calculated the average heliocentric radial velocity 12.30 km s⁻¹ and local standard of rest (LSR) radial velocity 12.29 km s⁻¹ using all the identified lines in the FEROS spectrum (1 σ uncertainty is 0.25 km s⁻¹). Our heliocentric radial velocity is in good agreement with Arkhipova et al. (2013, 12.6 \pm 1.7 km s⁻¹).

In Table 14, we listed the fluxes of the identified 14 atomic gas emission lines detected in the flux-density scaled Spitzer/IRS spectrum, where the fluxes are normalized with respect to the H β flux of the entire nebula.

3.4. Comparison of Line Fluxes Between 2006 and 2011

We investigated the possibility of temporal variations of the emission-line intensities by comparing our measurements with those of Arkhipova et al. (2013), who obtained the 3500–7200 Å low-resolution spectrum (FWHM = 4.5 Å) on 2011 June at the South African Astronomical Observatory (SAAO). In Table 15, we list their measured line intensities that overlapped with ours. In 2006–2011, the nebular line fluxes did not significantly change. Indeed, the $I(\lambda)$ in 2006 are very similar to those in 2011 ($I(2011)/I(2006) = 1.11 \pm 0.02$, correlation factor of 0.995). Thus, the ionization and elemental abundances of the nebula might not be largely changed in 2006–2011. Variation in the $T_{\rm eff}$ of the central star by 5000 K to 10,000 K in a 5- to 10-year interval might not immediately change the nebular morphology, parameters, and abundances in the same time period.

3.5. Plasma Diagnostics

In forbidden line analysis, we employed the NEBULAR package by Shaw & Dufour (1995) and in recombination line analysis, we used private software. In both emission-line analyses, we adopted effective recombination coefficients, transition probabilities, and effective collision strengths listed in Otsuka et al. (2010, their Table 7).

We performed plasma diagnostics using collisionally excited lines (CELs) and RLs. We greatly increased the results compared to Parthasarathy et al. (1993), who obtained one $n_{\rm e}$ and two $T_{\rm e}$ using the optical spectrum taken in 1992, and Arkhipova et al. (2013), who deduced one $n_{\rm e}$ and four $T_{\rm e}$ based on the 3500–7200 Å spectrum taken in 2011. In Table 4, we list the diagnostic line ratios to derive $n_{\rm e}$ and $T_{\rm e}$ and the resultant values. In Figure 3, we present the $n_{\rm e}$ – $T_{\rm e}$ diagram using the diagnostic CEL ratios. "opt" indicates the result from the optical forbidden line ratio; e.g., [S III] I(9069 Å)/I(6312 Å) ratio. "ir/opt" means the result from the mid-IR fine-structure lines and optical forbidden line; e.g., [S III] $I(18.7/33.5 \,\mu\text{m})/I(9067 \,\text{Å})$ ratio. We note that CEL emissivities are in general sensitive to $n_{\rm e}$ and $T_{\rm e}$, accordingly, CEL ionic abundances depend on a selection of $n_{\rm e}$ and $T_{\rm e}$.

First, we calculated n_e using CELs. The n_e - T_e diagram indicates that the average n_e is in the range from $\sim 2000 \text{ cm}^{-3}$

in neutral gas regions (by the $n_{\rm e}([{\rm N\,I}])$ curve, ID(1)) and $\sim 20,000\,{\rm cm^{-3}}$ in highly ionized gas regions (by the $n_{\rm e}([{\rm Ar\,IV}])$ curve, ID(7)) and the average $T_{\rm e}$ is $\sim 8000-10,000\,{\rm K}$. We derived all $n_{\rm e}$ by adopting a constant $T_{\rm e} = 9000\,{\rm K}$.

derived all n_e by adopting a constant $T_e = 9000 \text{ K}$. Next, we calculated $T_e([\text{O I}])$ by adopting $n_e([\text{N I}])$, $T_e([\text{Ar III}])$ by the average $n_e = 22,980 \text{ cm}^{-3}$ between $n_e([\text{S III}])$ and $n_e([\text{Cl III}])$, $T_e([\text{S III}])$ by $n_e([\text{S III}])$, $T_e([\text{Cl III}])$ by $n_e([\text{Cl III}])$, and both $T_e([\text{O III}])$ and $T_e([\text{Ne III}])$ by adopting $n_e([\text{Ne III}])$, respectively.

To obtain $T_e([O II])$, $n_e([O II])$, and $T_e([N II])$, which are representative n_e and T_e in lower ionization regions, we subtracted respective contributions from O^{2+} and O^{2+} recombination to the O^{2+} and O^{2+} recombination to the O^{2+} and O^{2+} recombination to the contributions to these lines, O^{2+} and O^{2+} recombination to the contributions to these lines, O^{2+} and O^{2+} are contributions to these lines, O^{2+} and O^{2+} are contributions to these lines, O^{2+} and O^{2+} are contributions to these lines, O^{2+} and O^{2+} are contributions to the con

$$\frac{I_{\rm R}({\rm [O~II]~7320/30~\mathring{A}})}{I({\rm H}\beta)} = 9.36 \left(\frac{T_{\rm e}}{10^4}\right)^{0.44} \frac{n({\rm O}^{2+})}{n({\rm H}^+)}, \qquad (2)$$

$$\frac{I_{\rm R}([{\rm N~II}]~5755~{\rm \AA})}{I({\rm H}\beta)} = 3.19 \left(\frac{T_{\rm e}}{10^4}\right)^{0.33} \frac{n({\rm N}^{2+})}{n({\rm H}^+)}.$$
 (3)

Here, $n(O^{2+})/n(H^+)$ and $n(N^{2+})/n(H^+)$ are the number density ratios of the O^2 and N^+ with respect to the H^+ , respectively.

We adopted the CEL $O^{2+} = 1.87(-4) \pm 1.39(-6)$ (see Section 3.6) in order to obtain the $I_R([O II] 7320/30 \text{ Å}) = 0.16 \pm 0.01$, where $I(H\beta) = 100$. Based on the result that the CEL O^{2+} is consistent with the RL O^{2+} , we assumed that the CEL O^{2+} could be very close to the RL O^{2+} . Here, we adopted the RL O^{2+} could be very close to the RL O^{2+} (see Section 3.6) to calculate the $I_R([N II] 5755 \text{ Å})$ of $O.33 \pm O.05$.

The [O II] I(3726 Å)/I(3729 Å) ratio is an n_e indicator and the I(3726/29 Å)/I(7320/30 Å) ratio is sensitive to both T_e and n_e . In Hen3-1357, n_e exceeds the critical density of the [O II] 3726/29 Å lines, so the I(3726 Å)/I(3729 Å) ratio could not give reliable n_e . Therefore, we used the I(3726/29 Å)/I(7320/30 Å) ratio to derive an n_e required for the N⁺, O⁺, Cl⁺, Ar⁺, and Fe²⁺ calculations. We obtained $n_e([O \text{ II}])$ by adopting a constant $T_e = 9000 \text{ K}$ and then obtained $T_e([N \text{ II}])$ using $n_e([O \text{ II}]) = 17,520 \text{ cm}^{-3}$.

We found the discrepancy between two $T_{\rm e}({\rm [S\,III]})$ values (IDs 10 and 11). This might be due to the underestimated [S III] 9069 Å that appeared in the red wavelength edge of the FEROS spectrum because the ionic S²⁺ abundance from this line is ~14% smaller than that from the fine-structure [S III] lines, which are insensitive to $T_{\rm e}$ (see Table 5). As we explained in Section, 2.2, the differential atmospheric refraction (DAR) effect might have affected [S III] 9069 Å, although we cannot exactly estimate how much light was lost from the [S III] 9069 Å line. The DAR effect might affect widely separated diagnostic line intensity ratios. However, for the S²⁺ abundance estimate, we adopted the average $T_{\rm e}$ between two $T_{\rm e}({\rm [S\,III]})$, thus, reducing the effects by inconsistency between these two $T_{\rm e}({\rm [S\,III]})$.

Similarly, if we underestimate the [O II] 7320/30 Å intensity by \sim 14%, which is an expected value from the above analysis for the S²⁺ abundance, we obtain $n_{\rm e}({\rm [O II]})=20\,300~{\rm cm}^{-3}$. Then, using $n_{\rm e}({\rm [O II]})$, we obtain $T_{\rm e}({\rm [N II]})=9010~{\rm K}$. Under $n_{\rm e}({\rm [O II]})$ and $T_{\rm e}({\rm [N II]})$, the N⁺, O⁺, Cl⁺, and Fe²⁺ abundances would increase by \sim 12%. Even if the DAR effect is

 $[\]overline{^9}$ We calculated these ionic abundances under $n_{\rm e}({\rm [O~II]})$ and $T_{\rm e}({\rm [N~II]})$ (see Table 16).

Table 4Summary of Plasma Diagnostics

		dominations (this moult for th	2006)		
ID	Ion	$n_{\rm e}$ -derivations (this work for the Diagnostic line ratio	Ratio	Result (cm ⁻³)	Arkhipova et al. (2013) (cm^{-3})
(1)	[N I]	I(5197 Å)/I(5200 Å)	$1.59(0) \pm 3.16(-2)$	1390 ± 90	
(2)	[S II]	I(6716 Å)/I(6731 Å)	$3.23(-1) \pm 7.30(-2)$, , , , , , , , , , , , , , , , , , , ,	
(3)	[O II]	I(3726/29 Å)/I(7320/30 Å)	$4.37(0) \pm 1.17(-1)$	$17,520 \pm 530$	8740 ± 7701
(4)	[S III]	$I(18.7 \ \mu m)/I(33.5 \ \mu m)$	$3.94(0) \pm 3.32(-1)$	$21,990 \pm 4840$	•••
(5)	[Cl III]	I(5517 Å)/I(5537 Å)	$4.86(-1) \pm 1.69(-2)$	$23,970 \pm 3120$	
(6)	[Ne III]	$I(15.6 \ \mu \text{m})/I(36.0 \ \mu \text{m})$	$1.56(+1) \pm 9.67(-1)$	$22,750 \pm 5850$	
(7)	[Ar IV]	I(4711 Å)/I(4740 Å)	$4.88(-1) \pm 4.55(-2)$	$22,720 \pm 4360$	
	Ηı	Paschen decrement		10,000 - 20,000	
		$T_{\rm e}$ -derivations (this work for th	e year 2006)		Arkhipova et al. (2013)
ID	Ion	Diagnostic line ratio	Ratio	Result (K)	(K)
(8)	[O I]	I(6300/63 Å)/I(5577 Å)	$9.69(+1) \pm 2.57(0)$	8470 ± 70	
(9)	[N II]	I(6548/83 Å)/I(5755 Å)	$6.38(+1) \pm 1.55(0)$	9280 ± 100	$11,066 \pm 1752$
(10)	[S III]	I(9069 Å)/I(6312 Å)	$1.22(+1) \pm 6.34(-1)$	8880 ± 180	$11,831 \pm 2286$
(11)	[S III]	$I(18.7/33.5 \ \mu \text{m})/I(9069 \ \text{Å})$	$1.38(0) \pm 7.82(-2)$	7430 ± 280	
(12)	[Cl III]	I(5517/37 Å)/I(8434/8501 Å)	$2.03(+1) \pm 4.54(0)$	7490 ± 850	
(13)	[Ar III]	I(7135/7751 Å)/I(5191 Å)	$2.09(+2) \pm 1.14(+1)$	8670 ± 150	
(14)	[Ar III]	$I(9.01 \ \mu \text{m})/I(7135/7751 \ \text{Å})$	$9.70(-1) \pm 4.27(-2)$	8400 ± 310	
(15)	[O III]	I(4959 Å)/I(4363 Å)	$5.91(+1) \pm 7.27(-1)$	9420 ± 40	$11,553 \pm 1579$
(16)	[Ne III]	$I(15.6 \ \mu \text{m})/I(3869/3968 \ \text{Å})$	$1.92(0) \pm 7.34(-2)$	8560 ± 70	
$T_{\rm e}({\rm PJ})$		$(I_{\lambda}(8194 \text{ Å})-I_{\lambda}(8169 \text{ Å}))/I(P11)$	$2.16(-2) \pm 2.53(-3)$	8090 ± 1680	
$T_{\rm e}({\rm He~I})$	Не і	I(7281 Å)/I(6678 Å)	$1.83(-1) \pm 7.38(-3)$	8340 ± 330	
$T_{\rm e}({\rm He~I})$	Не і	I(7281 Å)/I(5876 Å)	$4.95(-2) \pm 1.80(-3)$	7980 ± 360	

Note. For a comparison, the results from Arkhipova et al. (2013, for the year 2011) are listed in the last column.

present in our FEROS spectrum, the potential error of $c({\rm H}\beta)$, $T_{\rm e}$ and $n_{\rm e}$, and ionic/elemental abundances caused by the DAR effect would be $\sim\!15\%$ or less. Hence, our conclusion on these physical parameters derived from the CELs and the RLs does not change.

Finally, we calculated $T_{\rm e}$ and $n_{\rm e}$ using He I lines and H I Paschen series. We calculated $T_{\rm e}({\rm He~I})$ using He I $I(7281~{\rm Å})/I$ (6678 Å) and $I(7281~{\rm Å})/I(5876~{\rm Å})$ ratios using the recombination coefficients in a constant $n_{\rm e}=10^4~{\rm cm}^{-3}$ provided by Benjamin et al. (1999). We calculated the Paschen jump $T_{\rm e}({\rm PJ})$ using Equation (7) of Fang & Liu (2011). The H I P11 line is in an echelle order gap. Therefore, we obtained the *expected I* (P11) using the observed H I P12 line and the theoretical I (P11)/ $I({\rm P12})$ ratio of 1.30 in $n_{\rm e}\sim 10^2-10^5~{\rm cm}^{-3}$ and $T_{\rm e}\sim 5000-15{,}000~{\rm K}$ (Storey & Hummer 1995). Thus, we obtained $n_{\rm e}\sim 10{,}000-20{,}000~{\rm cm}^{-3}$ by comparing the observed $I({\rm P}n)/I({\rm P10})$ ratios (n is from 12 to 42) and the theoretical calculations under the Case B assumption and $T_{\rm e}({\rm PJ})=8090~{\rm K}$ by Storey & Hummer (1995).

As a comparison, the results from Arkhipova et al. (2013, for the year 2011) are listed in the last column. Arkhipova et al. (2013) reported $T_e([O III]) = 11,553 \pm 1579 \text{ K}$, $T_e([O II]) = 11,983 \pm 770 \text{ K}$, $T_e([O III]) = 11,066 \pm 1752 \text{ K}$, $T_e([S III]) = 11,831 \pm 2286 \text{ K}$, and $n_e([S II]) = 8740 \pm 7701 \text{ cm}^{-3}$. The difference between their $T_e([O III])$ and ours is due to the [O III] 4363 Å intensity (see Table 15). Under a constant n_e , the $T_e([O III])$ becomes higher as the [O III] I(4959/5007 Å)/I(4363 Å) ratio becomes lower. The $[N II] n_e-T_e$ curve

in Figure 3 suggests that the discrepancy in $T_e([N II])$ could be due to the difference in adopted n_e .

3.6. Ionic Abundance Derivations

In Table 16, we list $n_{\rm e}$ and $T_{\rm e}$ adopted for calculating each ionic abundance. We determined these values by referring to the $n_{\rm e}$ – $T_{\rm e}$ diagram and taking the ionization potential (IP) of the targeting ion into account. We calculated the CEL ionic abundances by solving an equation of population at multiple energy levels (from two energy levels for Ne⁺ and Ar⁺ and 33 levels for Fe²⁺) under the listed $n_{\rm e}$ and $T_{\rm e}$. We adopted a constant $n_{\rm e}=10^4\,{\rm cm}^{-3}$ and the average $T_{\rm e}({\rm He\,I})=8160\,{\rm K}$ to calculate He⁺. For the RL C²⁺, N²⁺, and O²⁺, we adopted $n_{\rm e}=10^4\,{\rm cm}^{-3}$ and $T_{\rm e}({\rm PJ})$.

We summarize the resultant CEL and RL ionic abundances in Tables 5 and 6, respectively. When we detected two or more lines of a target ion, we derived each ionic abundance using each line intensity. Then, we adopted the weight-average value as the representative ionic abundance as listed in the last line of each ion by boldface. We give the 1σ uncertainty of each ionic abundance, which accounts for the uncertainties of line fluxes (including $c(H\beta)$ uncertainty), T_e , and n_e .

The CEL abundances calculated using the optical lines are well consistent with ones using mid-IR fine-structure lines, indicating that the calculated CEL ionic abundances are the result of the proper selection of $T_{\rm e}$, in particular, and of accurate scaling flux of the Spitzer/IRS spectrum.

We obtained the RL N^{2+} and O^{2+} in this PN for the first time. The higher multiplet lines are in general insensitive to Case A or Case B assumptions and reliable because these lines are less affected by both resonance fluorescence by starlight

However, the auroral [O II] lines are out of their spectrum taken in 2011.

¹¹ The nebular [S III] lines are out of their spectrum, too.

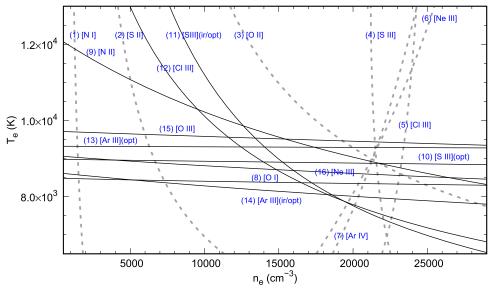


Figure 3. n_e - T_e diagram based on CEL diagnostic line ratios. The dashed and thick lines with "(ID)" indicate the n_e - and T_e -diagnostic curves generated by the line ratios listed in Table 4, respectively.

and recombination from higher terms. The consistency between the RL C^{2+} abundance by the multiple V6 4267.18 Å line and by the V2 6578.05 Å line indicates that the RL C^{2+} from both lines can be reliable. We can have the similar conclusion for the RL O^{2+} and N^{2+} abundances. The RL O^{2+} abundances are well consistent among the O II V1 4638/42/49/51/62/76 Å, V2 4349/67 Å, V10 4069.6/69.9/72/76 Å, V19 4153 Å, and V20 4105 Å lines. The RL N^{2+} abundances are derived using the V3 5679 Å and 4631 Å lines.

As is compared in Table 7, our ionic abundances agree with Arkhipova et al. (2013). However, we found obvious discrepancies in Ne^{2+} and S^{2+} . Their S^{2+} seems to be derived using the auroral line [SIII] 6312 Å. Although they did not report the detection of any [Ne III] lines in their spectrum taken in 2011, we assume that they derived the Ne²⁺ using nebular [Ne III] lines. The Ne^{2+} and \tilde{S}^{2+} differences between Arkhipova et al. (2013) and us are due to the adopted T_e . We stress that our adopted T_e for the Ne²⁺ and S²⁺ is determined using the [Ne III] and [S III] finestructure, nebular, and auroral lines. For instance, if we adopt their $T_{\rm e}({\rm [O\,III]}) = 11,553\,{\rm K}$ to calculate the Ne²⁺ using the nebular [Ne III] lines, the volume emissivities of these [Ne III] lines become 2.66 times higher than those in our adopted $T_e = 8560 \,\mathrm{K}$. Accordingly, the Ne^{2+} is down to 3.18(-5), which is consistent with Arkhipova et al. (2013). However, since the emissivities of the fine-structure [Ne III] lines do not largely change, even in both 8560 K by ours and 11,553 K by Arkhipova et al. (2013), the Ne²⁺ abundances using the fine-structure [Ne III] lines keep 8.38 (-5) (from the [Ne III] 15.56 μ m line) and 8.57(-5) (from the [Ne III] 36.02 μ m line). That is, we find out the spurious Ne²⁺ derivation discrepancy between the nebular and the fine-structure lines. We confirmed that a similar conclusion can apply for S^{2+} . Thus, if the nebula condition is in a steady state and had not dramatically changed between 2006 and 2011, we can conclude that our Ne^{2+} and S^{2+} are more reliable.

3.7. Elemental Abundance Derivations Using the ICFs

By introducing the ionization correction factor (ICF), we inferred the nebular abundances from their ionic abundances.

We calculated these ICF(X) derived based on the fraction of the observed ionic abundances with similar ionization potentials to the target element. The ICF(X) of element X is listed in the last line of each element of Tables 5 and 6. The abundance of the element X n(X)/n(H) corresponds to the value derived from the ICF(X) $\cdot \Sigma_{m=1} n(X^{m+})/n(H^+)$. We will compare these ICF(X) based on IPs with those calculated by Cloudy photoionization model later.

As shown in Section 3.6, we obtained the O(CEL), Ne, S, and Ar ionic abundances in various ionization stages. Thus, for these elements, we can adopt ICF(X) = 1.0. We adopted ICF (He) = 1.0 because we did not detect the nebular He II lines. Assuming that N corresponds to the sum of the N⁺ and N²⁺, we recovered the unobserved N²⁺(CEL) using the ICF(N) proposed by Delgado-Inglada et al. (2014). Then, using ICF(N) for N (CEL), we determined ICF(N(RL)). Since the IPs in both C and N ions are similar, we assumed that ICF(C(RL)) is as same as ICF(N (RL)). ICF(O(RL)) corresponds to O(CEL)/O²⁺(CEL). ICF(CI) corresponds to the Ar/(Ar⁺ + Ar²⁺) ratio. For ICF(Fe), we adopted Equation (3) of Delgado-Inglada & Rodríguez (2014).

In Table 8, we summarize the resultant elemental abundances derived by introducing the ICFs. The value $\epsilon(X)$ in the third column is $12 + \log_{10} n(X)/n(H)$. The value in the last column is the relative abundance to the Sun. We referred to the solar abundance by Asplund et al. (2009). Our work improved nebular elemental abundances calculated by the pioneering work of Parthasarathy et al. (1993) and a recent comprehensive study of Arkhipova et al. (2013).

Using the RL C, N, and O, we derived the C/O and the N/O ratios using the same type of emission lines, i.e., RLs. These ratios are important proofs of the initial mass of the central star. In Table 8, we list an *expected* C(CEL) based on the assumption that the RL C/O ratio (0.21 \pm 0.09) is consistent with the CEL C/O ratio.

The RL C/O ratio indicates that Hen3-1357 is an O-rich PN, which is also supported by the detection of the amorphous silicate features. The average of the logarithmic difference between the nebular and solar abundances of S, Cl, and Ar \langle [S, Cl, Ar/H] \rangle = -0.21 ± 0.10 indicates that this PN is about a half of a solar

Table 5
The Ionic Abundances Derived Using CELs $n(X^{m+})/n(H^{+})$ Elem. Ion

Elem.	Ion	$\lambda_{ m lab.}$	$I(\lambda)$	$n(X^{m+})/n(H^+)$	Elem.	Ion (Vm+)	$\lambda_{\mathrm{lab.}}$	$I(\lambda)$	$n(X^{m+})/n(H^+)$
(X) (1)	(X^{m+}) (2)	(3)	$(I(H\beta) = 100)$ (4)	(5)	(X) (6)	(X^{m+}) (7)	(8)	$(I(H\beta) = 100)$ (9)	(10)
N(CEL)	N^0	5197.90 Å	$3.63(-1) \pm 4.38(-3)$	$1.11(-6) \pm 3.46(-8)$	S	S ⁺	4068.60 Å	$4.47(0) \pm 8.61(-2)$	$1.13(-6) \pm 1.37(-7)$
		5200.26 Å	$2.28(-1) \pm 3.59(-3)$	$1.07(-6) \pm 1.82(-8)$			4076.35 Å	$1.51(0) \pm 2.90(-2)$	$1.17(-6) \pm 1.43(-7)$
		^	Average	$1.09(-6) \pm 2.83(-8)$			6716.44 Å	$6.07(0) \pm 1.54(-1)$	$9.55(-7) \pm 1.57(-7)$
	N^+	5754.64 Å	$2.55(0) \pm 3.87(-2)$	$3.61(-5) \pm 2.41(-6)$			6730.81 Å	$1.25(+1) \pm 3.19(-1)$	$1.07(-6) \pm 1.13(-7)$
		6548.04 Å	$4.10(+1) \pm 9.67(-1)$	$3.60(-5) \pm 1.24(-6)$				Average	$1.06(-6) \pm 1.30(-7)$
		6583.46 Å	$1.21(+2) \pm 2.91(0)$	$3.60(-5) \pm 1.25(-6)$		S^{2+}	6312.10 Å	$1.03(0) \pm 2.19(-2)$	$6.19(-6) \pm 9.21(-7)$
			Average	$3.60(-5) \pm 1.27(-6)$			9068.60 Å	$1.26(+1) \pm 5.96(-1)$	$4.90(-6) \pm 3.88(-7)$
			ICF(N(CEL))	3.09 ± 0.17			$18.71~\mu\mathrm{m}$	$1.39(+1) \pm 4.65(-1)$	$5.60(-6) \pm 8.07(-7)$
				$1.11(-4) \pm 7.39(-6)$			$33.48~\mu\mathrm{m}$	$3.52(0) \pm 2.72(-1)$	$5.63(-6) \pm 1.31(-6)$
O(CEL)	O_0	5577.34 Å	$2.19(-1) \pm 4.49(-3)$	$6.06(-5) \pm 3.96(-6)$				Average	$5.34(-6) \pm 6.98(-7)$
		6300.30 Å	$1.61(+1) \pm 3.39(-1)$	$6.06(-5) \pm 2.48(-6)$		S^{3+}	$10.51~\mu\mathrm{m}$	$7.76(0) \pm 2.66(-1)$	$4.18(-7) \pm 6.52(-8)$
		6363.78 Å	$5.10(0) \pm 1.11(-1)$	$6.00(-5) \pm 2.46(-6)$				ICF(S)	1.00
			Average	$6.05(-5) \pm 2.49(-6)$					$6.82(-6) \pm 7.13(-7)$
	O_{+}	3726.03 Å	$1.01(+2) \pm 2.62(0)$	$2.67(-4) \pm 1.08(-5)$	Ar	Ar^+	$6.99~\mu\mathrm{m}$	$7.43(0) \pm 2.53(-1)$	$7.15(-7) \pm 2.48(-8)$
		3728.81 Å	$3.76(+1) \pm 9.79(-1)$	$2.56(-4) \pm 9.88(-6)$		Ar^{2+}	5191.82 Å	$6.41(-2) \pm 3.11(-3)$	$1.94(-6) \pm 3.27(-7)$
		7320/7330 Å	$3.18(+1) \pm 5.56(-1)$	$2.98(-4) \pm 2.32(-5)$			7135.80 Å	$1.08(+1) \pm 3.22(-1)$	$1.47(-6) \pm 1.16(-7)$
			Average	$2.70(-4) \pm 1.29(-5)$			7751.10 Å	$2.63(0) \pm 9.57(-2)$	$1.50(-6) \pm 1.23(-7)$
	O^{2+}	4363.21 Å	$2.46(0) \pm 2.96(-2)$	$1.88(-4) \pm 9.02(-6)$			$9.01~\mu\mathrm{m}$	$1.30(+1) \pm 4.71(-1)$	$1.70(-6) \pm 6.56(-8)$
		4931.23 Å	$5.46(-2) \pm 2.92(-3)$	$1.80(-4) \pm 9.67(-6)$				Average	$1.59(-6) \pm 9.25(-8)$
		4958.91 Å	$1.46(+2) \pm 3.80(-1)$	$1.87(-4) \pm 1.26(-6)$		Ar^{3+}	4711.37 Å	$3.39(-2) \pm 3.05(-3)$	$2.12(-8) \pm 2.29(-9)$
			Average	$1.87(-4) \pm 1.39(-6)$			4740.16 Å	$6.95(-2) \pm 1.72(-3)$	$2.09(-8) \pm 8.27(-10)$
			ICF(O(CEL))	1.00				Average	$2.10(-8) \pm 1.31(-9)$
				$4.57(-4) \pm 1.30(-5)$				ICF(Ar)	1.00
Ne	Ne ⁺	12.81 μm	$4.67(+1) \pm 1.55(0)$	$7.23(-5) \pm 2.45(-6)$					$2.32(-6) \pm 9.57(-8)$
	Ne ²⁺	3869.06 Å	$4.03(+1) \pm 9.46(-1)$	$8.77(-5) \pm 4.07(-6)$	Fe	Fe ²⁺	4658.05 Å	$1.11(-1) \pm 2.50(-3)$	$6.71(-8) \pm 2.80(-9)$
		3967.79 Å	$1.00(+1) \pm 2.16(-1)$	$7.22(-5) \pm 3.29(-6)$			4701.53 Å	$4.65(-2) \pm 3.17(-3)$	$7.17(-8) \pm 5.65(-9)$
		$15.56~\mu\mathrm{m}$	$9.67(+1) \pm 3.19(0)$	$8.38(-5) \pm 4.54(-6)$			4733.91 Å	$2.58(-2) \pm 2.74(-3)$	$8.82(-8) \pm 1.01(-8)$
		$36.02 \ \mu m$	$6.18(0) \pm 3.23(-1)$	$8.57(-5) \pm 1.01(-5)$			4754.69 Å	$2.86(-2) \pm 3.64(-3)$	$9.18(-8) \pm 1.21(-8)$
			Average	$8.41(-5) \pm 4.56(-6)$			5270.40 Å	$5.89(-2) \pm 2.40(-3)$	$6.76(-8) \pm 3.48(-9)$
			ICF(Ne)	1.00				Average	$7.26(-8) \pm 5.11(-9)$
				$1.56(-4) \pm 4.77(-6)$				ICF(Fe)	2.30 ± 0.14
Cl	Cl^+	8578.69 Å	$3.04(-1) \pm 1.35(-2)$	$1.64(-8) \pm 8.17(-10)$					$1.67(-7) \pm 1.57(-8)$
		9123.60 Å	$1.03(-1) \pm 5.46(-3)$	$2.12(-8) \pm 1.23(-9)$					
			Average	$1.76(-8) \pm 9.22(-10)$					
	Cl^{2+}	5517.72 Å	$1.17(-1) \pm 3.39(-3)$	$1.02(-7) \pm 3.71(-8)$					
		5537.89 Å	$2.40(-1) \pm 4.59(-3)$	$1.02(-7) \pm 3.93(-8)$					
		8434.00 Å	$7.76(-3) \pm 1.23(-3)$	$1.18(-7) \pm 7.51(-8)$					
		8500.20 Å	$9.76(-3) \pm 3.70(-3)$	$1.18(-7) \pm 8.55(-8)$					
			Average	$1.03(-7) \pm 4.06(-8)$					
			ICF(Cl)	1.01 ± 0.06					
				$1.21(-7) \pm 4.16(-8)$					

Table 6
The Ionic Abundances Derived Using RLs

Elem.	Ion (Vm+)	$\lambda_{ m lab}$	$I(\lambda)$	$n(X^{m+})/n(H^+)$
(X)	(X^{m+})	(A)	$(I(H\beta) = 100)$	
Не	He^+	4120.81	$1.77(-1) \pm 4.80(-3)$	$9.95(-2) \pm 5.32(-3)$
		4387.93	$4.39(-1) \pm 6.42(-3)$	$7.18(-2) \pm 4.73(-3)$
		4437.55	$6.64(-2) \pm 4.31(-3)$	$8.53(-2) \pm 6.61(-3)$
		4471.47	$4.63(0) \pm 4.85(-2)$	$9.34(-2) \pm 5.22(-3)$
		4713.22	$6.68(-1) \pm 6.70(-3)$	$1.14(-1) \pm 9.20(-3)$
		4921.93	$1.21(0) \pm 4.45(-3)$	$9.05(-2) \pm 4.65(-3)$
		5015.68	$2.16(0) \pm 1.19(-2)$	$7.69(-2) \pm 3.63(-3)$
		5047.74	$1.68(-1) \pm 3.09(-3)$	$8.24(-2) \pm 4.52(-3)$
		5875.60	$1.47(+1) \pm 2.62(-1)$	$1.02(-1) \pm 6.54(-3)$
		6678.15	$3.97(0) \pm 9.94(-2)$	$9.79(-2) \pm 5.74(-3)$
		7281.35	$7.26(-1) \pm 2.30(-2)$	$8.37(-2) \pm 4.43(-3)$
			Average	$9.69(-2) \pm 5.88(-3)$
			ICF(He)	1.00
				$9.69(-2) \pm 5.88(-3)$
C(RL)	C^{2+}	4267.18	$1.03(-1) \pm 4.54(-3)$	$9.66(-5) \pm 3.06(-5)$
		6578.05	$5.05(-2) \pm 3.71(-3)$	$9.84(-5) \pm 3.88(-5)$
			Average	$9.72(-5) \pm 3.33(-5)$
			ICF(C(RL))	1.48 ± 0.22
				$1.44(-4) \pm 5.38(-5)$
N(RL)	N^{2+}	4630.54	$2.02(-2) \pm 2.59(-3)$	$9.27(-5) \pm 4.21(-5)$
		5679.56	$1.69(-2) \pm 2.30(-3)$	$4.23(-5) \pm 1.93(-5)$
			Average	$6.97(-5) \pm 3.17(-5)$
			ICF(N(RL))	1.48 ± 0.22
				$1.03(-4) \pm 4.94(-5)$
O(RL)	O^{2+}	4069.62	$2.65(-2) \pm 3.24(-3)$	$2.78(-4) \pm 7.04(-5)$
		4069.88	$3.84(-2) \pm 4.55(-3)$	$2.52(-4) \pm 6.61(-5)$
		4072.15	$5.68(-2) \pm 2.51(-3)$	$2.34(-4) \pm 5.45(-5)$
		4075.86	$7.55(-2) \pm 5.04(-3)$	$2.26(-4) \pm 5.34(-5)$
		4104.99	$4.05(-2) \pm 4.28(-3)$	$3.64(-4) \pm 9.07(-5)$
		4153.30	$3.10(-2) \pm 1.60(-3)$	$4.04(-4) \pm 9.69(-5)$
		4349.43	$3.34(-2) \pm 2.39(-3)$	$1.70(-4) \pm 3.92(-5)$
		4366.90	$3.41(-2) \pm 2.60(-3)$	$4.48(-4) \pm 1.07(-4)$
		4638.86	$3.44(-2) \pm 3.53(-3)$	$3.06(-4) \pm 7.73(-5)$
		4641.81	$6.37(-2) \pm 2.21(-3)$	$2.38(-4) \pm 5.35(-5)$
		4649.13	$1.03(-1) \pm 2.72(-3)$	$2.13(-4) \pm 4.79(-5)$
		4650.84	$3.42(-2) \pm 1.93(-3)$	$3.28(-4) \pm 7.57(-5)$
		4661.63	$4.79(-2) \pm 2.17(-3)$	$3.83(-4) \pm 8.68(-5)$
		4676.23	$3.19(-2) \pm 5.12(-3)$	$3.34(-4) \pm 9.09(-5)$
			Average	$\pmb{2.82(-4)\pm6.73(-5)}$
			ICF(O(RL))	2.45 ± 0.07
				$6.89(-4) \pm 1.66(-4)$

Table 7
Comparison of the Ionic Abundances in 2006 by Us and in 2011 by Arkhipova et al. (2013)

Ion (X ^{m+})	$n(X^{m+})/n(H^+)$ in 2006	$n(X^{m+})/n(H^+)$ in 2011
He ⁺	$9.69(-2) \pm 5.88(-3)$	$9.70(-2) \pm 8.00(-3)$
N^+	$3.60(-5) \pm 1.27(-6)$	$5.81(-5) \pm 2.31(-5)$
O_{+}	$2.70(-4) \pm 1.29(-5)$	$9.10(-5) \pm 7.16(-5)$
O ²⁺ (CEL)	$1.87(-4) \pm 1.39(-6)$	$1.01(-4) \pm 4.26(-5)$
Ne ²⁺	$8.41(-5) \pm 4.56(-6)$	$3.46(-5) \pm 1.76(-5)$
S^+	$1.06(-6) \pm 1.30(-7)$	$9.34(-7) \pm 5.70(-7)$
S^{2+}	$5.34(-6) \pm 6.98(-7)$	$1.43(-6) \pm 1.13(-6)$
Ar ²⁺	$1.59(-6) \pm 9.25(-8)$	$1.00(-6) \pm 4.26(-7)$

metallicity (0.6 Z_{\odot}). In the Milky Way chemical evolution of such a metallicity, [Fe/H] should be comparable to [α /H]. The expected [Fe/H] is –0.23 from the average [S,Ar/H] \sim –0.23 if

Table 8 Elemental Abundances

Elem. (X)	n(X)/n(H)	$\epsilon(X)$	[X/H]
Не	$9.69(-2) \pm 5.88(-3)$	10.99 ± 0.03	$+0.06 \pm 0.03$
C(RL)	$1.44(-4) \pm 5.38(-5)$	8.16 ± 0.16	-0.23 ± 0.17
C(CEL)	$9.54(-5) \pm 4.26(-5)$	7.98 ± 0.19	-0.40 ± 0.20
N(RL)	$1.03(-4) \pm 7.39(-6)$	8.01 ± 0.03	$+0.15 \pm 0.12$
N(CEL)	$1.11(-4) \pm 7.39(-6)$	8.05 ± 0.03	$+0.19 \pm 0.12$
O(RL)	$6.89(-4) \pm 1.66(-4)$	8.84 ± 0.10	$+0.11 \pm 0.13$
O(CEL)	$4.57(-4) \pm 1.30(-5)$	8.66 ± 0.01	-0.07 ± 0.07
Ne	$1.56(-4) \pm 4.77(-6)$	8.19 ± 0.01	$+0.14 \pm 0.10$
S	$6.82(-6) \pm 7.13(-7)$	6.83 ± 0.05	-0.33 ± 0.05
Cl	$1.21(-7) \pm 4.16(-8)$	5.08 ± 0.15	-0.17 ± 0.16
Ar	$2.32(-6) \pm 9.57(-8)$	6.37 ± 0.02	-0.13 ± 0.10
Fe	$1.67(-7) \pm 1.57(-8)$	5.22 ± 0.04	-2.24 ± 0.09

Note. C(CEL) is an expected value estimated by adopting the RL C/O ratio.

all of the Fe atoms are in the gas phase and are not captured by any dust grains. However, the observed [Fe/H] is much smaller than the expected [Fe/H] value. Thus, the largely depleted [Fe/H] suggests that over 99% of the Fe atoms in the nebula would be locked within silicate grains.

3.8. Abundance Discrepancy of C²⁺, N²⁺, and O²⁺

One of the long-standing problems in PN abundances is that the RL C, N, O, and Ne ionic abundances are in general larger than the CEL ones. Several explanations for the abundance discrepancy have been proposed, e.g., temperature fluctuation, high-density clumps, and cold hydrogen-deficient components (see, e.g., a review by Liu 2006). There might be a possible link between the binary central star and the abundance discrepancy, as was recently proposed by Jones et al. (2016). In Hen3-1357, the abundance discrepancy factor (ADF) defined as the ratio of the RL to the CEL ionic abundance is 1.51 ± 0.36 in O^{2+} , which is lower than a typical value \sim 2.0 (Liu 2006). Such a degree of the O^{2+} discrepancy can be explained by introducing the temperature fluctuation model proposed by Peimbert (1967).

Parthasarathy et al. (1993) and Feibelman (1995) showed the IUE UV spectrum taken on 1992 April 23 (IUE Program ID: NA108, PI: S.R. Pottasch, Data-ID: 44459). From there, we can see the CEL C III] 1906/09 Å and N III] 1744-54 Å lines. Although Parthasarathy et al. (1995) gave these line fluxes, the CEL C²⁺ and N²⁺ have never been calculated so far. It would be of interest to estimate the $ADF(C^{2+})$ because the RL C^{2+} of $6.91(-5) \pm 1.48(-6)$ using the C II 4267 Å line detected in the spectrum taken in 1992 was calculated by Arkhipova et al. (2013). We download the processed SWP44459 data set from the Multimission Archive at STScI (MAST), we measured the fluxes of the C III] 1906/09 Å and N III] 1744-54 Å lines, and calculated the CEL $C^{2+} = 9.53$ $(-5) \pm 1.19(-6)$ and the CEL $N^{2+} = 5.49(-5) \pm 5.32(-6)$ using the $F(H\beta)$, E(B-V), $T_{\rm e}$, and $n_{\rm e}$ reported by Parthasarathy et al. (1993). The ADF(C²⁺) of 1.24 \pm 0.27 in 1992 is similar to our ADF(O) measured in 2006. This might be applied even for ADF(N); the ratio of the RL N²⁺ in 2006 to the CEL N² in 1992 is 1.27 ± 0.59 .

Based on our analysis, we conclude that the ADF(C/N/O) would be < 2.

3.9. Comparison with AGB Nucleosynthesis Models

The He/C/N/O/Ne/S abundances are close to the AGB star nucleosynthesis model predictions by Karakas (2010) for initially 1.0, 1.25, and 1.5 M_{\odot} stars with Z=0.008 (0.4 Z_{\odot}). The 1.0 M_{\odot} model predicts ϵ (He):10.99, ϵ (C):8.09, ϵ (N):7.81, ϵ (O):8.53, ϵ (Ne):7.69, and ϵ (S):7.00. The differences among these models are ϵ (C) and ϵ (N); ϵ (C):8.04 and ϵ (N):7.90 in the 1.25 M_{\odot} model, and ϵ (C):8.12 and ϵ (N):7.95 in the 1.5 M_{\odot} model. The predicted final core mass is 0.58 M_{\odot} in an initially 1.0 M_{\odot} star to 0.63 M_{\odot} in a 1.5 M_{\odot} star.

According to current stellar models for low-mass AGB stars, partial mixing of the bottom of the H-rich convective envelope into the outermost region of the ^{12}C -rich intershell layer leads to the synthesis of extra ^{13}C and ^{14}N at the end of each third dredge-up (TDU). During He-burning, ^{14}N captures two α particles and ^{22}Ne are produced. ^{20}Ne is the most abundant and it is not altered significantly by H or He burning. The $\epsilon(\text{Ne})$ discrepancy between the observation (8.19) and the model prediction (7.69) might be due to an increase of ^{22}Ne . The models for the 1.0, 1.25, and

 $1.5\,M_{\odot}$ stars with Z=0.008 by Karakas (2010) do not predict TDUs and do not include such partial mixing zone (PMZ). Note that the PMZ is not well justified yet. The Ne abundance in Hen3-1357 suggests that the progenitor might have formed a PMZ and extra ²²Ne and Ne might be conveyed to the stellar surface by unexpected mechanisms, e.g., very few TDUs or LTPs. Otherwise, we might interpret that the $\epsilon(Ne)$ discrepancy between the observation and the model prediction is due to the errors in the atomic data of $Ne^{+,2+}$.

From chemical abundance analysis, we can conclude that the progenitor mass could be $1.0-1.5\,M_\odot$ if Hen3-1357 had evolved from a star with the initial $Z\sim0.008$.

4. Photoionization Model with Cloudy

We construct the self-consistent photoionization model using Cloudy to reproduce all of the observed quantities.

The characteristics of the CSPN are critical in the photoionization models because the X-ray to UV wavelength radiation from CSPN determines the ionization structure of the nebula and surrounding ISM and is the ionizing and heating source of gas and dust grains. The distance is necessary for the comparison between the model and the observed fluxes/flux densities/nebula size. In Sections 4.1 and 4.2, therefore, we try to determine parameters of the CSPN and the distance.

The empirically derived quantities of the nebula and the mid-IR SED provide the input parameters of the nebula and dust grain: $\epsilon(X)$, geometry, the H β flux of the entire nebula, hydrogen density radial profile ($n_{\rm H}$) of the nebula, filling factor (f), and type of dust grain. The band flux densities/fluxes, gas emission-line fluxes, and the SED from the UV to far-IR provide constraints in the iterative fitting of the model parameters. In Section 4.3, we explain the input parameters. Finally, we show the modeling result in Section 4.4.

4.1. Flux Density of the CSPN's SED

First, we investigated the SED of the CSPN using the FEROS spectrum, which is the sum of the nebular emission lines and continuum and the CSPN spectrum. For this end, we need to subtract the nebular continuum from the FEROS spectrum. We used the NEBCONT code in the DISPO package of STARLINK v.2015A¹² to generate the nebular continuum. For the calculation, we adopted the H β flux of the entire nebula 9.83 (-12) erg s⁻¹ cm⁻², $n(\text{He}^+/\text{H}^+) = 9.69(-2)$, $T_e = 8090$ K, and $n_e = 22,860$ cm⁻³, which is the average among $n_e([\text{S III}])$, $n_e([\text{Cl III}])$, $n_e([\text{Ne III}])$, and $n_e([\text{Ar IV}])$.

In the upper panel of Figure 4, we show the synthesized nebular continuum. The discontinuity around 8200 Å indicates the Paschen jump. After we scaled the de-reddened FEROS spectrum up to match with the H β line flux of the entire nebula, we manually removed gas emission lines to the extent possible. This gas emission-line-free FEROS spectrum is presented in the same panel. In the lower panel, we show the resultant spectrum generated by subtracting the synthesis nebular continuum spectrum from the gas emission-line-free and flux-density-scaled FEROS spectrum. Note that the residual spectrum coincides with the spectrum of the CSPN. A spike feature around 8200 Å is from the residuals of Paschen and Bracket continuum between the observed and the model. If we can subtract this continuum around the Paschen jump from the

¹² http://starlink.eao.hawaii.edu/starlink

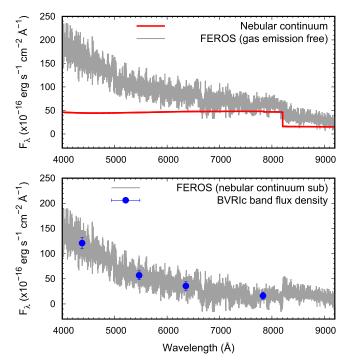


Figure 4. (Upper panel) Gas emission-line-free FEROS spectrum of Hen3-1357 (de-reddened, gray line) and the synthesized nebular continuum by NEBCONT (red line) in the range from 4000 to 9200 Å. (Lower panel) Nebular continuum subtracted FEROS spectrum (gray line) and the de-reddened *BVRIc* band flux densities (blue circles) based on this residual FEROS spectrum.

observed spectrum, the spike feature will be gone. This spike feature does not affect the *Ic*-band magnitude measurement. Using this residual spectrum, we measured flux densities for *BVRIc* bands by taking filter transmission curves of each band, as summarized in Table 9.

4.2. Synthesis of the CSPN's SED, Core Mass, and Distance

Reindl et al. (2014) performed spectral synthesis fitting of the spectrum of the CSPN taken using Far Ultraviolet Spectroscopic Explorer (*FUSE*) in 2006 and obtained $T_{\rm eff} = 55{,}000~{\rm K}$ and log $g = 6.0 \pm 0.5~{\rm cm~s}^{-2}$. However, in our Cloudy model with this $T_{\rm eff}$ and the measured de-reddened m_V of the CSPN (14.51, see Section 4.1) determining the luminosity, we overproduced the fluxes of higher IP ions such as [Ne III] and [O III] lines. ¹³

It might be because the nebula ionization structure is not yet fully changed by the recent very fast post-AGB evolution of the CSPN. Although we firmly believe the results of Reindl et al. (2014), we needed to adopt a SED of the CSPN with a lower $T_{\rm eff}$ to reproduce the overall observed nebular line fluxes. For instance, we estimated $T_{\rm eff}$ to be $50,560 \pm 2710 \, {\rm K}$ using the [O III]/H β line ratio and the formula established among PNe in the Large Magellanic Cloud by Dopita & Meatheringham (1991).

 Table 9

 BVRIc Band De-reddened Flux Densities of the CSPN's SED Derived from the Residual FEROS Spectrum

λ_c (Å)	Band	$F_{\lambda} (\text{erg s}^{-1} \text{ cm}^{-2} \text{ Å}^{-1})$
4378.1	Johnson-B	$1.21(-14) \pm 1.14(-15)$
5466.1	Johnson-V	$5.69(-15) \pm 8.76(-16)$
6358.0	Cousins-R	$3.58(-15) \pm 8.66(-16)$
7829.2	Cousins-I	$1.63(-15) \pm 7.08(-16)$

Note. The extinction-free *V*-band magnitude (m_V) is 14.51 ± 0.17 , where $F_{\lambda}(m_V = 0)$ is 3.631(-9) erg s⁻¹ cm⁻² Å⁻¹.

Therefore, we utilized the non-local thermodynamic equilibrium (non-LTE) stellar atmospheres modeling code Tlusty (Hubeny 1988)¹⁴ to obtain the SED of the CSPN for our Cloudy model. Using Tlusty, we constructed line-blanketed, plane-parallel, and hydrostatic stellar atmosphere, where we considered the He, C, N, O, Ne, Si, P, S, and Fe abundances. We run a grid model to cover $T_{\rm eff}$ from 43,000 to 53,000 K in a constant 1000 K steps. Here, we adopted the observed nebular $\epsilon(\text{He}), \epsilon(\text{N(CEL})), \epsilon(\text{O(CEL})), \epsilon(\text{Ne}), \text{ and } \epsilon(\text{S}).$ We adopted the expected $\epsilon(C(CEL)) = 7.98$ (see Table 8). As Reindl et al. (2014) reported, there is no significant difference between the nebular and stellar He, C, N, O, S abundances. We adopted stellar $\epsilon(Si) = 7.52$ and $\epsilon(P) = 4.42$ derived by Reindl et al. (2014). From the nebular $\langle [S, Ar/H] \rangle = -0.23$, we adopted $\epsilon(\text{Fe}) = 7.23$. We interpret that 99% of the Fe atoms in the stellar atmosphere are eventually locked as dust grains in the nebula. We set the microturbulent velocity to 10 km s⁻¹ and the rotational velocity to 20 km s⁻¹.

Based on Reindl et al. (2014, 2017), Parthasarathy et al. (1993), and Karakas (2010), the core mass of the CSPN (m_*) is $\sim 0.53-0.6\,M_{\odot}$. Referring to the theoretical post-AGB evolution tracks presented in Figure 4 of Reindl et al. (2017), we adopted $\log g = 5.25 \,\mathrm{cm \ s^{-2}}$ and the distance $D = 2.5 \,\mathrm{kpc}$ to obtain $m_* \sim 0.53$ – $0.6 M_{\odot}$. D has been determined in the range between 826 pc (see Reindl et al. 2017, reference therein) and 5.85 kpc (Frew et al. 2016) thus far. When we adopt $D = 826 \,\mathrm{pc}$, we have to set a very small inner radius of the nebula to reproduce the observed H β flux and by doing so, we overproduced fluxes of higher IP lines and obtained hotter dust temperatures, accordingly causing lower dust continuum fluxes. If D is 5.0 kpc, the situation would become better than the case of $D = 826 \,\mathrm{pc}$, and we can then reproduce the observed line fluxes. However, we must set $\log g \sim 4.5 \, \mathrm{cm \ s^{-2}}$ in order to obtain a value above the m_* range, and Hen3-1357 would be classified as a halo PN not a thin disk PN.

We verified our adopted D of 2.5 kpc. Following Quireza et al. (2007), we can classify Hen3-1357 into a Type II or III PN based on the observed ϵ (He) and N/O ratio. Hen3-1357 would be a thin disk population. Quireza et al. (2007) reported that the average peculiar velocity relative to the Galaxy rotation (ΔV) is \sim 23 km s⁻¹ for Type IIb and \sim 70 km s⁻¹ for Type III and the average height from the Galactic plane (|z|) is \sim 0.225 kpc for Type IIa and \sim 0.686 kpc for Type III, respectively. From the constraint on |z|, we obtained a range of D toward Hen3-1357 between 1.07 and 3.27 kpc. Maciel & Lago (2005) calculated the rotation velocities at the nebula Galactocentric positions calculated for a Galaxy disk rotation curve based on four distance scales. Using their established

 $[\]overline{13}$ For example, when we adopt $T_{\rm eff} = 55{,}000$ K and distance D = 2.5 kpc, the Cloudy model predicted that the respective $I([{\rm Ne~III}] 3869 \,{\rm \AA})$ and $I([{\rm O~III}] 5007 \,{\rm \AA})$ are 134.6 (40.3 in our FEROS observation) and 303.4 (145.5), and the predicted ionization boundary radius was $4.1 \, (1.28 \, {\rm Maybe})$, if we set D > 8.0 kpc, the $T_{\rm eff} = 55{,}000$ model could explain the observed line fluxes. However, If we set $D > 80 \, {\rm kpc}$, the $T_{\rm eff} = 55{,}000 \, {\rm model}$ could explain the observed line fluxes. However, If we set $T_{\rm III} = 100 \, {\rm M}_{\odot}$ the $T_{\rm III} = 100 \, {\rm M}_{\odot}$ and estimate the core mass of the central star to be $T_{\rm III} = 100 \, {\rm M}_{\odot}$.

¹⁴ http://nova.astro.umd.edu

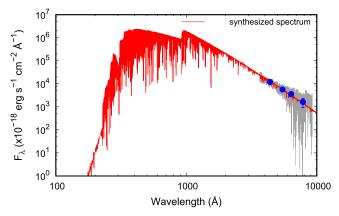


Figure 5. Spectrum of the CSPN synthesized using Tlusty (red line) in $T_{\rm eff}=45,000~{\rm K}$ and $\log g=5.25~{\rm cm~s^{-2}}$. The flux density is scaled down to the $F_{\lambda}=5.69(-15)~{\rm erg~s^{-1}~cm^{-2}~\AA^{-1}}$ at 5466.1 Å. The gray line and blue circles are the same as indicated in Figure 4.

Galaxy rotation velocity based on the distance scale of Cahn et al. (1992), van de Steene & Zijlstra (1995), and Zhang (1995), Equation (3) of Quireza et al. (2007), and our measured LSR radial velocity 12.29 km s⁻¹ (see Section 3.3), we obtained a D versus ΔV plot. Using this plot and the constraint on ΔV , we got another range of D between 1.63 and 4.92 kpc. Thus, we obtained D=1.63-3.27 kpc, with 2.5 kpc in the middle value of this distance range. From the above discussion, we adopted D=2.5 kpc and the absolute V-band magnitude of the CSPN $M_V=2.555$.

Finally, we obtained the synthesized spectra using SYN-SPEC, ¹⁵ as displayed in Figure 5.

4.3. Parameters of the Nebular Gas and Dust Grain

4.3.1. Nebular Elemental Abundances

We adopted elemental abundances listed in Table 8 as a first guess. We refined these abundances to reproduce the observed emission-line intensities. For the other elements unseen in the FEROS and Spitzer/IRS spectra, we referred to the predicted values in the AGB nucleosynthesis model for initially $1.5\,M_\odot$ stars with Z=0.008 by Karakas (2010). For the sake of consistency, we substituted the transition probabilities and effective collision strengths of CELs by the same values applied in our nebular abundance analysis.

In spite of non-detection in the *Spitzer*/IRS spectrum, our Cloudy model with $\epsilon(Si)$ predicted by the AGB nucleosynthesis model overestimated the [Si III] 34.82 μ m line. This indicates that most of the Si atoms exist as amorphous silicate dust grains. Therefore, we took care of the Si and Mg abundances as silicate grain components. Assuming that the nebular [Mg,Si/H] is comparable to the [Mg/H] = -1.69 measured in PN IC4846 (Hyung et al. 2001), we kept $\epsilon(Mg) = 5.86$ and $\epsilon(Si) = 5.84$, respectively. As we discuss later, IC4846 displays amorphous silicate features (e.g., Stanghellini et al. 2012) and very similar elemental abundances to Hen3-1357.

Table 10
The Best-fit Cloudy Model Parameters of Hen3-1357

Parameters of the CSPN	Value
$L_*/T_{\rm eff}/\log g/D$	$330 L_{\odot}/45,550 \text{ K}/5.25 \text{ cm s}^{-2}/2.5 \text{ kpc}$
M_V	2.555
R_*	$0.291 R_{\odot}$
m_*	$0.550M_\odot$
Parameters of the Nebula	Value
$\epsilon(X)$	He:10.97, C:8.18, N:7.89, O:8.58, Ne:8.20
	Mg:5.86, Si:5.84, S:6.74, Cl:4.73, Ar:6.25
	Fe:5.23, Others: Karakas (2010)
Geometry	Spherical symmetry
Shell size	$r_{\rm in}$:0."44 (0.005 pc), $r_{\rm out}$:2."77 (0.034 pc)
Ionization boundary	1."48 (0.018 pc)
radius (r_{ib})	
Filling factor (f)	0.58
$n_{ m H}$	$11\ 610\ \mathrm{cm}^{-3}$
$F(H\beta)$	$9.84(-12) \text{ erg s}^{-1} \text{ cm}^{-2} \text{ (de-reddened)}$
m_g	$3.81(-2)M_{\odot}$
Parameters of the Dust	Value
Grain size	0.01 – $0.50~\mu \mathrm{m}$
T_d	40–150 K
m_d	$1.98(-4)M_{\odot}$
m_d/m_g (DGR)	5.20(-3)

4.3.2. Nebula Geometry, Boundary Conditions, and Gas Filling Factors

We adopted a spherical shell with a uniform hydrogen density. We assumed the ionization boundary radius $(r_{\rm ib})$ of \sim 1." 3 using a plot of count versus size of the circular aperture generated by the archival $HST/{\rm Wide}$ Field Planetary Camera 2 (WFPC2) F487N (H β) image taken on 1996 March 3 (Prop-ID: GO6039, PI: M. Bobrowsky). 85% of the total count is measured within the radius of 1."28. Although the exact size of the nebula in 2006 is unknown, slow nebula shell expansion velocity suggests that the size of the nebula is not largely different since 1996. Here, we measured twice the expansion velocities (2 $V_{\rm exp}$) using Equation (3) of Otsuka et al. (2003, 2009, 2015) and 144 emission lines as summarized in Table 17. To calculate line broadening by gas thermal motion, we adopted a suitable $T_{\rm e}$ for each ion by referring to Table 4. In Hen3-1357, $2V_{\rm exp}$ did not correlate with the IP. We measured the average $2V_{\rm exp} = 14.8 \pm 0.5$ km s⁻¹ among the 39 H I lines, which is consistent with the mean expansion velocity ($V_{\rm exp}$) of 8.4 ± 1.5 km s⁻¹ measured from the 17 lines by Arkhipova et al. (2013).

The filling factor f can be defined as the ratio of an rms density derived from a hydrogen line flux, T_e , and nebula radius to the n_e (CELs) (see, e.g., Mallik & Peimbert 1988; Peimbert et al. 2000). We calculated an rms density of $10.750 \, \mathrm{cm}^{-3}$ from the H β flux of the entire nebula, $T_e = 8060 \, \mathrm{K}$, $r_{ib} = 1\rlap.{''}28$, and a constant n_e/n (H⁺) = 1.15. We estimated f to be 0.47–0.62 using this rms density and the observed n_e (CELs). Here, we set f = 0.55 as a first guess and varied.

4.3.3. Dust Grains and Size Distribution

We assumed spherical-shaped silicate grains and adopted a standard interstellar size distribution $(n(a) \propto a^{-3.5})$, Mathis et al. 1977) with radius $a = 0.01-0.50 \, \mu \text{m}$. We selected the

¹⁵ http://nova.astro.umd.edu/Synspec49/synspec.html

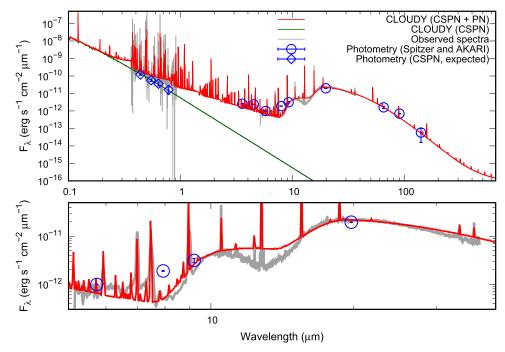


Figure 6. (Upper panel) Comparison between the Cloudy model and observational data of Hen3-1357. The blue diamonds indicate the observed *BVRIc* band flux densities of the CSPN, which are the same values in listed in Table 9. (Lower panel) Closed-up plots in 5-40 μ m. In both panels, we set the spectral resolution of the synthesized Cloudy spectrum to be a constant 600, corresponding to that of *Spitzer/IRS* SH and LH spectra.

Table 11
Comparison of the ICFs between the Observation and the Cloudy Model

Elem.	ICF(obs)	ICF(model)
Не	1.00	1.03
C(RL)	1.48 ± 0.22	1.30
N(RL)	1.48 ± 0.22	1.62
N(CEL)	3.09 ± 0.17	2.69
O(RL)	2.45 ± 0.07	2.23
O(CEL)	1.00	1.04
Ne	1.00	1.01
S	1.00	1.00
Cl	1.00 ± 0.06	1.01
Ar	1.00	1.01
Fe	2.30 ± 0.14	2.07

dielectric function table of astronomical silicate currently recommended by the webpage of B. Draine. ¹⁶

4.4. Model Result

To find the best-fit model, we varied $T_{\rm eff}$, the inner radius of the nebula $r_{\rm in}$, $n_{\rm H}$, $\epsilon({\rm He/C/N/O/Ne/S/Cl/Ar/Fe})$, the dust mass fraction, and f within a given range using the optimize command available in Cloudy.

García-Hernández et al. (2002) found that the distribution of molecular hydrogen H_2 v=1-0 S(1) at $2.122~\mu m$ and v=2-1S (1) at $2.248~\mu m$ is quite homogeneous and extends well beyond the distribution of the H I Br γ line. This suggests that Hen3-1357 has large neutral regions.

Thus, we went to deep neutral gas regions in our model; we continued calculation until any of the model's predicted flux densities at AKARI/FIS 65/90/140 μ m bands reached or exceeded the relevant observed values. The Cloudy model predicted $r_{\rm ib} = 1\rlap.{''}48$ where $T_{\rm e}$ drops below 4000 K. We

stopped our model calculation at the outer radius ($r_{\rm out}$) of 3.4 (-2) pc (2"77). The goodness of fit was determined by the reduced χ^2 value calculated from the following observational constraints: 17 broadband fluxes, 5 broadband flux densities, 104 gas emission fluxes, $r_{\rm ib}$, de-redden $F(H\beta)$ of the entire nebula. Table 10 summarizes the parameters of the best-fit model, where the reduced χ^2 is 33.5.

The SED of the best-fit model, in comparison with the observational data, is presented in Figure 6. From the model result we confirmed that the gas-emission contribution to Spitzer/IRAC 8.0 μ m and AKARI/IRC 9.0/18 μ m bands is 51.8%, 19.1%, and 3.9%, respectively. Thus, the disagreement at the Spitzer/IRAC 8.0 μ m band between the observed photometry and the predicted SED can be explained by considering the gas-emission contribution to the relevant band.

The observed and model-predicted line fluxes, band fluxes, and band flux densities are summarized in Table 18. The intensity of the O II 4075 Å and 4651 Å is the sum of the multiplet V10 and V1 O II lines, respectively. It is noteworthy that we simultaneously reproduced both the observed RL/CEL N and O line fluxes.

The predicted ICF(X) by Cloudy listed in Table 11 is in excellent agreement with the ICF(X) derived in Section 3.7, indicating that our Cloudy model succeeded in explaining the ionization nebula structure and the ICF(X) based on IP is the proper value.

As described in Section 4.2, under the constraints of the CSPN at D=2.5 kpc, we need $T_{\rm eff}=45{,}550$ K and $L_*=330$ L_\odot in order to explain the observed quantities. With D, L_* , and $\log g$, we derived $m_*=0.55$ M_\odot .

The gas mass $(m_g) = 3.81(-2)\,M_\odot$ is the sum of the ionized and neutral gas masses. The ionized gas mass is $5.38(-3)\,M_\odot$ and the remaining is the neutral gas mass. Our derived m_g is close to the ejected mass, which equals $8.9(-2)\,M_\odot$ in initially $1.5\,M_\odot$ stars with Z=0.008 during the last thermal pulse

https://www.astro.princeton.edu/~draine/dust/dust.diel.html

Fe

5.22

Elem. (X)	OD PN			IC4	846			Hen
	Ave.	(a)	(b)	(c)	(d)	(e)	Ave.	3-1357
Не	11.02	10.98	10.96	10.90	11.01		10.96	10.99
C(RL)		7.74	8.37	8.43			8.27	8.16
C(CEL)		7.68	8.45	8.16		7.95	8.15	7.98
N(RL)				8.10			8.10	8.01
N(CEL)	7.78	7.89	7.81	8.09	7.69		7.90	8.05
O(RL)			8.97	8.78			8.89	8.84
O(CEL)	8.42	8.60	8.51	8.59	8.60	8.50	8.56	8.66
Ne	7.78	7.90	7.83	7.77	7.99		7.88	8.19
Mg		5.86					5.86	
S	6.50	6.95	6.63	7.01	6.73		6.86	6.83
Cl	6.15	5.11		5.34	6.14		5.76	5.08
Ar	6.03	6.18	5.96	6.02	6.13		6.08	6.37

Table 12 Comparisons with the $\epsilon(X)$ of IC4846 and the Average $\epsilon(X)$ Value Among Galactic Amorphous Silicate-rich PNe

Note. The $\epsilon(X)$ of Hen3-1357 is the result using the ICFs, except for the CEL C, which is an expected value. The average abundance of Galactic amorphous silicaterich PNe in the Galaxy (OD PN Ave) in the second column is taken from García-Hernández & Górny (2014). On elemental abundances of the PN IC4846 in the third—seventh columns—(a) Hyung et al. (2001), (b) Wesson et al. (2005), (c) Wang & Liu (2007), (d) García-Hernández & Górny (2014), and (e) Delgado-Inglada & Rodríguez (2014). The eighth column is the average among the measurements by (a)–(e).

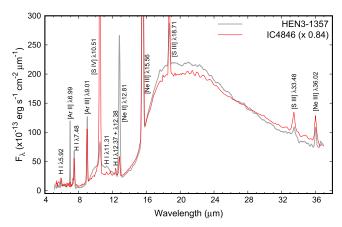


Figure 7. *Spitzer/IRS* spectra of IC4846 and Hen3-1357. The spectral resolution of Hen3-1357 is down to match with that of IC4846. For IC4846, we scaled the flux density up to match with *AKARI/IRC* 9.0/18 μ m bands (0.1311 and 2.038 Jy, respectively; Yamamura et al. 2010). For demonstration, the flux density of this scaled spectrum is further scaled to match with the IRS spectrum of Hen3-1357 by a constant factor of 0.84. See the text for details.

AGB, predicted by Karakas & Lattanzio (2007). We obtained a dust mass (m_d) of 1.98(-4) M_{\odot} .

It is of interest to know how far-IR data impact gas and dust mass estimates in our model. When we stopped model calculations at $r_{\rm ib}$, we obtained $m_g=4.61(-3)~M_{\odot}$ and $m_d=3.79(-5)~M_{\odot}$. This model did not well fit any AKARI far-IR fluxes. To fit the observed far-IR data, we need a larger $r_{\rm out}$. With the AKARI far-IR data, we obviously obtained much greater m_g and m_d . About 80% of the total dust mass is from warm–cold dust components beyond the ionization front. From the model results, we confirmed that the gas-emission contribution to $AKARI65/90/140~\mu m$ bands is 1.4%, 1.08%, and 2.58%, respectively. AKARI far-IR data would be thermal emission from warm–cold dust.

Cox et al. (2011) derived an upper limit of the sum of m_d and $m_g = 0.16\,M_\odot$ within a 3 pc radius using the AKARI/90 μ m and a constant dust-to-gas mass ratio (DGR) = 6.25(-3) for O-rich dust, although the measured dust temperature (T_d) is unknown. Using their results, we calculated an upper limit $m_g = 0.159\,M_\odot$ and $m_d = 9.94(-4)\,M_\odot$, respectively.

Umana et al. (2008) derived the total ionized mass of $\sim 5.7(-2)$ M_{\odot} using the radio data in 2002, assuming D = 5.6 kpc, inner/ outer radii = 0.65/1.3 shallow shell geometry, and f = 1.0. Using the *IRAS* data, they derived $T_d = 137 \pm 2 \,\mathrm{K}$ and $m_d = 2$ (-4) M_{\odot} using the 60 μ m flux density in the case of the silicate. Based on the results and assumptions of Umana et al. (2008), ionized gas and co-existing dust would be $\sim 6.6(-3) M_{\odot}$ and ~ 4.0 (-5) M_{\odot} , respectively, if we adopt D = 2.5 kpc and f = 0.58. These estimated values are consistent with our derived m_g and m_d when we stopped the model at $r_{\rm ib}$. On the dust, Cox et al. (2011) found that the AKARI far-IR flux densities are a factor two lower than predicted from the IRAS data. They interpreted that the far-IR variability in its infrared flux might occur due to recent mass-loss event(s) or evolution of the CSPN. Following the report of Cox et al. (2011) and the dust mass $\sim 4.0(-5) M_{\odot}$ co-existing with the ionized gas by the IRAS data in 1980s, we estimate the dust mass to be $\lesssim 2(-5)$ M_{\odot} in 2006–2007, which is comparable to our derived dust mass of $3.79(-5) M_{\odot}$ within the ionized gas.

5.21

5.21

5. Discussion

It is necessary to verify whether the gas and dust chemistry in Hen3-1357 is consistent with other O-rich gas and dust Galactic PNe. To compare such PNe is an important step in understanding the evolution of Hen3-1357.

García-Hernández & Górny (2014) investigated relations among dust features, elemental abundances, and evolution of the progenitors. In the second column of Table 12, we list the average $\epsilon(X)$ among their amorphous silicate PNe. They found that $\epsilon(He)$ and the N/O ratio in these amorphous silicate-containing PNe are in agreement with the AGB nucleosynthesis model predictions for initially $\sim 1.0\,M_\odot$ stars with Z=0.008. García-Hernández & Górny (2014) suggested that the higher Ne/O ratios in O-rich dust PNe relative to the AGB models may reflect the effect of the PMZ. The observed $\epsilon(He)$ and the CEL N/O ratio of 0.24 ± 0.02 in Hen3-1357 coincide with the average values in their amorphous silicate PN sample. As discussed in Section 3.9, our predicted progenitor mass, initial metallicity, and interpretation for the Ne overabundance in Hen3-1357 follow their results.

We can now understand relations among dust features, nebular abundances, and the progenitor stars' evolution. Moreover, we know that the nebula morphology is connected to the central star's evolution. Using the *HST*/WFPC images as a guide, we tried to find objects showing similar nebula shape, dust features, and elemental abundance patterns to Hen3-1357. To our best knowledge, the point-symmetric PN IC4846 (e.g., Miranda et al. 2001) is very similar to Hen3-1357.

IC4846 clearly shows amorphous silicate features, as reported by Stanghellini et al. (2012). We reduced the BCD of IC4846 (obs AORKEY: 25839616, PI: L. Stanghellini) with the same process applied for Hen3-1357. In Figure 7, we display the Spitzer/IRS spectra of IC4846 and Hen3-1357. The dust features seen in both PNe are very similar, except for the different strengths of the 9 and 18 μ m emission bumps, which might reflect the difference in the grain composition. For IC4846, Stasińska & Szczerba (1999) derived a single $T_d=107$ K and DGR = 1.2(-3) based on the *IRAS* four band fluxes using a modified blackbody function. Tajitsu & Tamura (1998) derived a single $T_d=168$ K using the *IRAS* data. Zhang & Kwok (1991) derived a single $T_d=152$ K and $T_{\rm eff}=47,600$ K by fitting SED from IUE to IRAS data.

In the third to seventh columns of Table 12, we compile nebular abundances of IC4846 measured by prior works. The eighth column gives the average value. Obviously, the abundances in both IC4846 and Hen3-1357 are in excellent agreement even in the RL ϵ (C,N,O) and the Fe-depletion. So far, the ϵ (Mg) and ϵ (Fe) measurements have been performed only by Hyung et al. (2001) using the *IUE* UV spectrum and only by Delgado-Inglada & Rodríguez (2014) using the optical spectra, respectively. The largely depleted [Mg/H] = -1.69 in IC4846 might indicate that most of the Mg atoms are captured by silicate grains. We assumed the similar situation to Hen3-1357 in our Cloudy model.

Hyung et al. (2001) succeeded in reproducing UV-optical gas emission-line fluxes in the photoionization model of IC4846 by setting CSPN's radius to $0.425\,R_\odot$, $T_{\rm eff}=70,000\,\rm K$, $\log g=4.6\,\rm cm\,s^{-2}$, and $D=7\,\rm kpc$, which gave $L_*=3900\,L_\odot$. In comparison to post-AGB evolutionary tracks, they estimated $m_*\sim 0.57\,M_\odot$.

From the above comparisons, we can conclude that Hen3-1357 is an ordinary amorphous silicate-rich and O-rich gas PN. Among amorphous silicate-rich PNe in the Milky Way, IC4846 is very similar to Hen3-1357. Both PNe have evolved from similar progenitor mass stars with Z=0.008. However, the rapid evolution of the central star of Hen3-357 still remains a puzzle.

6. Summary

We performed a detailed chemical abundance analysis and constructed the photoionization model of Hen3-1357 to characterize the PN and obtain a coherent picture of the dusty nebula and CSPN in 2006 based on optical to far-IR data.

We calculated the abundances of the nine elements. The RL C/O ratio indicates that Hen3-1357 is an O-rich PN, supported by the detection of the broad 9/18 μ m amorphous silicate bands in the *Spitzer*/IRS spectrum. The ADF(O²⁺) is less than a typical value measured in PNe. The observed elemental abundances can be explained by AGB nucleosynthesis models of Karakas (2010) for initially 1–1.5 M_{\odot} stars with Z=0.008. The Ne overabundance might be due to the enhancement of ²²Ne isotope in the He-rich intershell.

We did not find significant variation of nebular line intensities between 2006 and 2011, suggesting that the nebular ionization state and elemental abundances are most likely in a steady state during the same period, while the central star is rapidly evolving.

By incorporating the spectrum of the CSPN synthesized by Tlusty as the ionization/heating source of the PN with Cloudy modeling, we succeeded in explaining the observed SED and derived the gas and dust masses, dust-to-gas mass ratio, and core mass of the CSPN. About 80% of the total dust mass is from the warm-cold dust components beyond ionization front.

Through comparison with other Galactic PNe, we found that Hen3-1357 is an ordinary amorphous silicate-rich and O-rich gas PN. IC4846 shows many similarities in PN properties with Hen3-1357.

Although we derived physical properties of the nebula and also provided the range of the progenitor mass, the rapid evolution from post-AGB B1 supergiant in 1971 to a young PN in a matter of 21 years is not yet understood. If the central star has experienced LTP, then it should be H-poor ad He- and C-rich in its present hot post-AGB stage soon after the LTP. However, the nebular and stellar chemical compositions calculated by us and Reindl et al. (2014, 2017) are nearly solar, not at all similar to those of LTP PNe. If the central star has now started returning toward the AGB phase, then very soon it will go through A, F, and G spectral types before it appears as a born-again AGB star. If so, it may show abundances similar to that of LTP PNe in the future. We need to monitor the central star's $T_{\rm eff}$, $\log g$, and chemical composition in order to confirm whether it is evolving back toward the AGB stage. If Hen3-1357 is a binary, rapid evolution might be explained. For that end, monitoring of the radial velocity using stellar absorption profiles in UV wavelength would be necessary. Moreover, comparisons with other Galactic amorphous silicate-rich and O-rich gas PNe such as IC4846 can help us to understand the evolution of Hen3-1357. Thus, further observations of both the nebula and the central star are required for further understanding this PN.

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Software: IRAF (v.2.16), SMART (v.8.2.9: Higdon et al. 2004), IRSCLEAN (v.2.1.1), MOPEX, STARLINK (v.2015A), CLOUDY (v13.03: Ferland et al. 2013), TLUSTY (Hubeny 1988)

Appendix

The following Tables 13–18 support our analysis.

Table 13 (Continued)

The Identified Monite Emission Emiss in the LEROS Spectrum			(Continued)								
$\lambda_{\text{ebs.}} \atop (A)$	Line	$\lambda_{lab.} \ (\mathrm{A})$	$f(\lambda)$	$I(\lambda)$ $(I(H\beta) =$	$\delta I(\lambda) = 100)$	$\lambda_{\text{obs.}}$ (A)	Line	λ _{lab.} (A)	$f(\lambda)$	$I(\lambda)$ $(I(H\beta) =$	$\delta I(\lambda) = 100)$
3697.33	H I (B17)	3697.15	0.328	1.923	0.107	4931.45	[O III]	4931.23	-0.019	0.055	0.003
3704.01	H I (B16)	3703.85	0.327	2.028	0.122	4959.13	[O III]	4958.91	-0.026	145.519	0.380
3705.16	He I	3704.98	0.327	0.965	0.087	4987.58	[Fe III]	4987.21	-0.033	0.016	0.003
3712.12 3722.02	H I (B15) H I (B14)	3711.97 3721.94	0.325 0.323	2.384	0.119	4996.95	ОП	4996.98	-0.035	0.045	0.004
3723.81	Fe II]	3721.94	0.323	4.156 0.474	0.155 0.058	5015.88	Не і	5015.68	-0.040	2.161	0.012
3726.20	[O II]	3726.03	0.323	101.210	2.625	5047.95	He I	5047.74	-0.048	0.168	0.003
3728.96	[O II]	3728.81	0.322	37.647	0.979	5146.79 5159.01	[Fe III]	5146.45 5158.78	-0.071 -0.074	0.027 0.017	0.004 0.002
3734.52	H I (B13)	3734.37	0.321	3.026	0.097	5191.94	[Fe II] [Ar III]	5191.82	-0.074 -0.081	0.017	0.002
3750.31	H I (B12)	3750.15	0.317	4.220	0.124	5198.13	[N I]	5197.90	-0.082	0.363	0.003
3770.79	H I (B11)	3770.63	0.313	4.353	0.115	5200.49	[N I]	5200.26	-0.083	0.228	0.004
3798.05	H I (B10)	3797.90	0.307	5.330	0.133	5270.74	[Fe III]	5270.40	-0.098	0.059	0.002
3819.79	Не 1	3819.60	0.302	1.142	0.033	5517.91	[Cl III]	5517.72	-0.145	0.117	0.003
3833.75	Не і	3833.55	0.299	0.072	0.010	5538.06	[Cl III]	5537.89	-0.149	0.240	0.005
3835.54	H I (B9)	3835.38	0.299	7.597	0.183	5577.64	[O I]	5577.34	-0.156	0.219	0.004
3867.69 3868.92	He I	3867.47 3869.06	0.291 0.291	0.147 40.325	0.008 0.946	5679.81	NII	5679.56	-0.173	0.017	0.002
3871.95	[Ne III] He I	3871.79	0.291	0.078	0.946	5754.83	[N II]	5754.64	-0.185	2.578	0.038
3889.06	H I (B8)	3889.05	0.286	15.997	0.472	5791.58	Сп	5791.69	-0.190	0.021	0.002
3926.71	He I	3926.54	0.277	0.124	0.005	5875.88	He I O I	5875.60	-0.203	14.666 0.026	0.262
3964.90	Не і	3964.73	0.267	0.540	0.012	5958.74 6300.55	[O I]	5958.54 6300.30	-0.215 -0.263	16.129	0.004 0.339
3967.63	[Ne III]	3967.79	0.267	10.000	0.216	6312.32	[S III]	6312.10	-0.263 -0.264	1.031	0.022
3970.23	H I (B7)	3970.07	0.266	16.026	0.341	6364.04	[O I]	6363.78	-0.204 -0.271	5.095	0.022
4009.42	Не 1	4009.26	0.256	0.152	0.006	6527.42	[N II]	6527.24	-0.293	0.019	0.003
4026.37	Не і	4026.20	0.251	1.532	0.031	6548.32	[N II]	6548.04	-0.296	40.956	0.967
4068.77	[S II]	4068.60	0.239	4.471	0.086	6578.31	Сп	6578.05	-0.300	0.050	0.004
4069.74	Оп	4069.62	0.239	0.027	0.003	6583.70	[N II]	6583.46	-0.300	121.454	2.915
4070.04	O II	4069.88	0.239	0.038	0.005	6678.42	Не і	6678.15	-0.313	3.972	0.099
4072.32	OII	4072.15	0.238	0.057	0.003	6716.73	[S II]	6716.44	-0.318	6.066	0.154
4076.02 4076.52	О II [S II]	4075.86 4076.35	0.237 0.237	0.076 1.508	0.005 0.029	6721.76	Оп	6721.39	-0.319	0.009	0.002
4097.45	N III	4097.35	0.237	0.023	0.023	6731.10	[S II]	6730.81	-0.320	12.471	0.319
4101.90	Η I (B6, Hδ)	4101.73	0.230	21.516	0.395	7002.42	O I	7002.12	-0.356	0.051	0.004
4103.19	О п	4103.00	0.229	0.030	0.004	7062.57 7065.50	He I He I	7062.28 7065.18	-0.364 -0.364	0.019 7.846	0.003 0.247
4103.81	N III	4103.39	0.229	0.028	0.004	7136.06	[Ar III]	7135.80	-0.304 -0.374	10.767	0.322
4105.13	Оп	4104.99	0.229	0.040	0.004	7155.53	[Fe II]	7155.16	-0.374 -0.376	0.034	0.003
4119.45	Оп	4119.22	0.224	0.019	0.004	7160.85	He I	7160.61	-0.377	0.027	0.003
4121.00	Не і	4120.81	0.224	0.177	0.005	7254.70	O I	7254.45	-0.390	0.064	0.004
4143.93	Не 1	4143.76	0.217	0.229	0.005	7281.64	Не 1	7281.35	-0.393	0.726	0.023
4153.44	ОП	4153.30	0.214	0.031	0.002	7298.33	Не і	7298.04	-0.395	0.035	0.003
4267.35 4276.00	С II О II	4267.18 4275.99	0.180 0.177	0.103 0.032	0.005 0.005	7319.33	[O II]	7318.92	-0.398	3.998	0.130
4340.64	Η I (B5, Hγ)	4340.46	0.177	46.052	0.579	7320.40	[O II]	7319.99	-0.398	13.487	0.430
4349.64	O II	4349.43	0.154	0.032	0.002	7329.96	[O II]	7329.66	-0.400	7.476	0.239
4363.38	[O III]	4363.21	0.149	2.461	0.030	7331.04 7378.30	[O II] [Ni II]	7330.73 7377.83	-0.400 -0.406	6.987 0.030	0.224 0.003
4367.08	Оп	4366.90	0.148	0.034	0.003	7578.30	He I	7499.85	-0.400 -0.422	0.036	0.003
4368.41	OI	4368.24	0.148	0.036	0.002	7751.42	[Ar III]	7751.10	-0.455	2.630	0.096
4388.11	Не і	4387.93	0.142	0.439	0.006	7816.45	Не і	7816.14	-0.464	0.077	0.003
4437.76	Не і	4437.55	0.126	0.066	0.004	8245.95	H I (P42)	8245.64	-0.516	0.033	0.004
4471.68	Не 1	4471.47	0.115	4.628	0.048	8248.09	H I (P41)	8247.73	-0.516	0.027	0.003
4591.14	N II	4590.85	0.078	0.036	0.005	8250.17	H I (P40)	8249.97	-0.517	0.028	0.001
4630.71 4639.02	N II	4630.54	0.066	0.020	0.003	8252.65	H I (P39)	8252.40	-0.517	0.033	0.002
4642.01	O 11	4638.86 4641.81	0.064 0.063	0.034 0.064	0.004 0.002	8255.36	H I (P38)	8255.02	-0.517	0.027	0.002
4649.33	ОП	4649.13	0.061	0.103	0.002	8258.21	H I (P37)	8257.85	-0.517	0.041	0.002
4651.01	OII	4650.84	0.060	0.034	0.002	8261.20	H I (P36)	8260.93	-0.518	0.042	0.002
4658.33	[Fe III]	4658.05	0.058	0.111	0.002	8264.69 8268.31	He I H I (P34)	8264.62 8267.94	-0.518 -0.519	0.059 0.055	0.003 0.003
4661.83	Оп	4661.63	0.057	0.048	0.002	8272.22	H I (P33)	8271.93	-0.519 -0.519	0.057	0.003
4676.48	Оп	4676.23	0.053	0.032	0.005	8276.60	H I (P32)	8276.31	-0.520	0.070	0.003
4701.86	[Fe III]	4701.53	0.045	0.046	0.003	8281.49	H I (P31)	8281.12	-0.520	0.072	0.004
4711.59	[Ar IV]	4711.37	0.042	0.034	0.003	8286.71	H I (P30)	8286.43	-0.521	0.111	0.005
4713.38	Не і	4713.22	0.042	0.668	0.007	8292.67	H I (P29)	8292.31	-0.521	0.096	0.005
4725.73	[Ne IV]?	4725.64	0.038	0.011	0.002	8299.20	H I (P28)	8298.83	-0.522	0.118	0.005
4734.06	[Fe III]	4733.91	0.036	0.026	0.003	8306.48	H I (P27)	8306.11	-0.523	0.119	0.005
4740.41	[Ar IV]	4740.16	0.034	0.070	0.002	8314.61	H I (P26)	8314.26	-0.524	0.128	0.006
4754.94 4861.52	[Fe III] Η I (B4, Η <i>β</i>)	4754.69 4861.33	0.030 0.000	0.029 100.000	0.004 0.112	8323.76	H I (P25)	8323.42	-0.525	0.143	0.006
4881.20	Η Ι (Β4, Ηβ) [Fe III]	4881.00	-0.000	0.045	0.112	8334.11	H I (P24)	8333.78	-0.526	0.152	0.007
4891.21	о п?	4890.86	-0.003 -0.008	0.043	0.004	8342.74	C III	8342.20	-0.527	0.020	0.002
4922.13	Не і	4921.93	-0.016	1.214	0.004	8345.85 8359.31	H I (P23) H I (P22)	8345.55 8359.00	-0.527 -0.529	0.188 0.220	0.008
4924.78	[Fe III]	4924.54	-0.017	0.027	0.002	8362.07	He I	8361.73	-0.529 -0.529	0.220	0.009
						0302.07	110 1	0501./5	0.549	0.062	0.004

Table 13 (Continued)

		(Continue	u)		
$\lambda_{\text{obs.}}$ (A)	Line	$\lambda_{\mathrm{lab.}} \ \mathrm{(A)}$	$f(\lambda)$	$I(\lambda)$ $(I(H\beta) =$	$\delta I(\lambda)$ = 100)
8374.81	H I (P21)	8374.48	-0.531	0.219	0.009
8392.73	H I (P20)	8392.40	-0.533	0.252	0.011
8397.80	Не І	8397.42	-0.533	0.010	0.001
8413.65	H I (P19)	8413.32	-0.535	0.288	0.012
8434.02	[Cl III]	8434.00	-0.537	0.008	0.001
8438.29	H I (P18)	8437.95	-0.537	0.326	0.014
8444.79	Не І	8444.55	-0.538	0.025	0.003
8446.82	OI	8446.48	-0.538	0.468	0.020
8451.52	Не 1	8451.17	-0.539	0.013	0.003
8467.58	H I (P17)	8467.25	-0.541	0.378	0.016
8486.63	Не І	8480.79	-0.543	0.017	0.002
8500.45	[Cl III]	8500.20	-0.544	0.010	0.004
8502.82	H I (P16)	8502.48	-0.544	0.450	0.020
8545.71	H I (P15)	8545.38	-0.549	0.508	0.023
8579.06	[Cl II]	8578.69	-0.552	0.304	0.014
8582.21	Не І	8581.88	-0.552	0.024	0.003
8598.73	H I (P14)	8598.39	-0.554	0.636	0.028
8617.23	[Fe II]	8616.95	-0.556	0.042	0.002
8648.62	Не І	8648.26	-0.559	0.030	0.002
8665.37	H I (P13)	8665.02	-0.560	0.829	0.037
8680.62	NΙ	8680.28	-0.562	0.017	0.001
8683.85	NΙ	8683.40	-0.562	0.017	0.001
8703.64	NΙ	8703.25	-0.564	0.012	0.001
8727.55	[C I]	8727.12	-0.566	0.014	0.002
8733.82	Не І	8733.44	-0.567	0.037	0.003
8736.36	Не І	8736.04	-0.567	0.012	0.002
8750.82	H I (P12)	8750.47	-0.568	1.042	0.047
8777.05	Не і	8776.83	-0.571	0.053	0.003
8845.72	Не І	8845.39	-0.576	0.055	0.004
8892.21	[Fe II]	8891.91	-0.580	0.016	0.002
8997.34	Не І	8997.00	-0.588	0.055	0.004
9000.05	Не І	8999.75	-0.589	0.022	0.002
9015.29	H I (P10)	9014.91	-0.590	1.624	0.077
9052.33	[Fe II]	9051.95	-0.592	0.011	0.002
9063.71	Не і	9063.32	-0.593	0.060	0.004
9069.29	[S III]	9068.60	-0.594	12.577	0.596
9123.99	[Cl II]	9123.60	-0.598	0.103	0.005
9210.69	Не і	9210.34	-0.604	0.099	0.006

Note. The first column is the wavelength at the observation. The third column is the wavelength at rest in the laboratory.

$\lambda_{ m lab.}$	Line	$I(\lambda)$
(μm)		$(I(H\beta)=100)$
5.92	Ні	0.740 ± 0.042
6.99	[Ar II]	7.435 ± 0.253
7.48	Ні	6.186 ± 0.223
9.01	[Ar III]	12.993 ± 0.471
10.51	[S IV]	7.758 ± 0.266
11.31	Ні	0.277 ± 0.068
12.37	Ηı	1.043 ± 0.034
12.81	[Ne II]	46.711 ± 1.553
14.37	[Cl II]?	0.323 ± 0.040
15.56	[Ne III]	96.699 ± 3.188
17.62	He I?	1.274 ± 0.094
18.71	[S III]	13.864 ± 0.465
33.48	[S III]	3.517 ± 0.272
36.02	[Ne III]	6.180 ± 0.323

Note. The flux density is scaled-up to match with the AKARI/IRC 9.0 μ m band flux density. Then, the fluxes of these identified atomic lines are normalized with respect to the H β flux of the entire nebula $9.83(-12) \pm 7.33$ (-13) erg s⁻¹ cm⁻². See the text for details.

Table 15
Comparison of the Overlapped Line Fluxes between our 2006 and Arkhipova et al. (2013)'s 2011 Observations

λ _{lab.} (Å)	Line	$F(\lambda)$ in 2006	$F(\lambda)$ in 2011	$I(\lambda)$ in 2006	$I(\lambda)$ in 2011
3726/29	[O II]	130.595 ± 0.345	126.8 ± 7.2	138.857 ± 2.801	163.0 ± 9.5
4101.73	В6	20.596 ± 0.031	18.4 ± 2.5	21.516 ± 0.395	21.6 ± 2.9
4340.46	B5	44.700 ± 0.067	45.8 ± 2.2	46.052 ± 0.579	50.9 ± 2.5
4363.21	[O III]	2.392 ± 0.004	4.1 ± 1.6	2.461 ± 0.030	4.6 ± 1.8
4958.91	[O III]	146.232 ± 0.237	150.8 ± 3.8	145.519 ± 0.380	148.0 ± 3.8
5754.64	[N II]	2.671 ± 0.006	3.9 ± 1.1	2.578 ± 0.038	3.3 ± 0.9
5875.60	Не І	15.244 ± 0.115	18.1 ± 0.9	14.666 ± 0.262	15.2 ± 0.7
6300.30	[O I]	16.956 ± 0.021	22.5 ± 0.9	16.129 ± 0.339	17.7 ± 0.7
6312.10	[S III]	1.084 ± 0.003	1.6 ± 0.5	1.031 ± 0.022	1.2 ± 0.4
6363.78	[O I]	5.365 ± 0.09	8.3 ± 0.7	5.095 ± 0.111	6.5 ± 0.6
6548.04	[N II]	43.327 ± 0.054	60.9 ± 1.6	40.956 ± 0.967	46.5 ± 1.3
6583.46	[N II]	128.601 ± 0.168	190.2 ± 5.1	121.454 ± 2.915	144.6 ± 4.2
6678.15	Не І	4.215 ± 0.007	5.6 ± 0.8	3.972 ± 0.099	4.2 ± 0.6
6716.44	[S II]	6.444 ± 0.010	11.3 ± 0.9	6.066 ± 0.154	8.5 ± 0.6
6730.81	[S II]	13.255 ± 0.021	21.6 ± 1.0	12.471 ± 0.319	16.1 ± 0.8
7065.18	Не І	8.410 ± 0.101	10.3 ± 1.1	7.846 ± 0.247	7.4 ± 0.8
7135.80	[Ar III]	11.562 ± 0.018	17.3 ± 0.8	10.767 ± 0.322	12.3 ± 0.6

Note. $F(\lambda)$ and $I(\lambda)$ are normalized to the $F(H\beta)$ and $I(H\beta)$, where they equal 100, respectively.

Ion	$n_{\rm e}~({\rm cm}^{-3})$	<i>T</i> _e (K)
N^0 , O^0	1390	8470
S^+	5710	9280
$C^{2+}(RL)$, $O^{2+}(RL)$, $N^{2+}(RL)$	10,000	8090
He^+	10,000	8160
N^+ , O^+ , Cl^+ , Fe^{2+} , Ar^+	17,520	9280
S^{2+}	21,990	8160
Ar^{2+}	21,990	8540
Ne ²⁺	22,720	8560
$O^{2+}(CEL), S^{3+}, Ar^{3+}$	22,750	9420
Ne ⁺	22,980	8540
Cl ²⁺	23,970	7490

Table 17Twice Expansion Velocities of Hen3-1357

Ion	No. of	Emiss.	IP (eV)	$ \begin{array}{c} 2V_{\rm exp} \\ ({\rm km \ s}^{-1}) \end{array} $
	sample	type	(ev)	(KIII S)
ΗI	39	RL	13.60	14.78 ± 0.45
OI	5	RL	13.62	21.42 ± 1.13
NΙ	3	RL	14.53	18.44 ± 1.42
CII	2	RL	24.38	14.41 ± 1.51
Не І	27	RL	24.59	16.28 ± 0.28
N II	3	RL	29.60	14.19 ± 1.78
O II	16	RL	35.12	16.43 ± 1.32
[C I]	1	CEL	0.00	18.06 ± 1.84
[N I]	2	CEL	0.00	17.52 ± 0.20
[O I]	3	CEL	0.00	14.86 ± 0.08
[Fe II]	3	CEL	7.87	15.25 ± 1.48
[S II]	4	CEL	10.36	14.21 ± 0.03
[Cl II]	2	CEL	12.97	16.94 ± 0.23
[O II]	6	CEL	13.62	13.73 ± 0.05
[N II]	4	CEL	14.53	14.37 ± 0.64
[Fe II]	8	CEL	16.18	17.97 ± 1.49
[S III]	3	CEL	23.33	13.53 ± 0.03
[Cl III]	3	CEL	23.81	14.17 ± 0.92
[Ar III]	3	CEL	27.63	13.09 ± 0.23
[O III]	3	CEL	35.12	14.19 ± 0.26
[Ar IV]	2	CEL	40.74	16.72 ± 0.91
[Ne III]	2	CEL	40.96	14.76 ± 0.04

Table 18
Comparison between the Observed and Model-predicted Line Fluxes, Band Fluxes, and Band Flux Densities

$\lambda_{ m lab.}$	Ion	$I(\text{obs}) $ $(I(\text{H}\beta) = 100)$	$I(\text{model})$ $(I(H\beta) = 100)$
3697.2 Å	Н I (В17)	1.923	1.146
3703.9 Å	H I (B16)	2.028	1.347
3712.0 Å	H I (B15)	2.384	1.606
3721.9 Å	H I (B14)	4.156	1.949
3726.0 Å	[O II]	101.210	133.154
3728.8 Å	[O II]	37.647	54.376
3734.4 Å	H I (B13)	3.026	3.039
3750.2 Å	H I (B12)	4.220	2.408
3770.6 Å	H I (B11)	4.353	3.930
3797.9 Å	H I (B10)	5.330	5.228
3819.6 Å	He I	1.142	1.228
3835.4 Å 3867.5 Å	Н I (B9) Не I	7.597 0.147	7.192 0.107
3869.1 Å	[Ne III]	40.325	35.532
3889.1 Å	H I (B8)	40.323 15.997	10.316
3964.7 Å	He I	0.540	1.055
3967.8 Å	[Ne III]	10.000	10.709
3970.1 Å	H I (B7)	16.026	15.611
4026.2 Å	He I	1.532	2.229
4068.6 Å	[S II]	4.471	4.474
4075.0 Å	O II	0.197	0.134
4076.4 Å	[S II]	1.508	1.450
4101.7 Å	Η I (B6, Hδ)	21.516	25.961
4120.8 Å	He I	0.177	0.209
4143.8 Å	Не і	0.229	0.350
4267.2 Å	Сп	0.103	0.126
4340.5 Å	H I (B5, H γ)	46.052	46.863
4363.2 Å	[O III]	2.461	2.190
4387.9 Å	He I	0.439	0.596
4437.6 Å	Не 1	0.066	0.084
4471.5 Å	Не 1	4.628	4.853
4651.0 Å	ОП	0.315	0.138
4658.1 Å	[Fe III]	0.111	0.222
4701.5 Å	[Fe III]	0.046	0.054
4711.4 Å	[Ar IV]	0.034	0.021
4713.2 Å	Не ї	0.668	0.662
4733.9 Å	[Fe III]	0.026	0.022
4740.2 Å	[Ar IV]	0.070	0.034
4754.7 Å	[Fe III]	0.029	0.025
4881.0 Å	[Fe III]	0.045	0.065
4921.9 Å	Не І	1.214	1.293
4931.2 Å	[O III]	0.055	0.054
4958.9 Å	[O III]	145.519	131.766
4987.2 Å	[Fe III]	0.016	0.011
5015.7 Å	He I	2.161	2.655
5047.7 Å	He I	0.168	0.210
5191.8 Å 5197.9 Å	[Ar III]	0.064 0.363	0.137 0.248
5200.3 Å	[N I] [N I]	0.303	0.152
5270.4 Å	[Fe III]	0.059	0.081
5517.7 Å	[Pe III] [Cl III]	0.039	0.191
5537.9 Å	[Cl III]	0.240	0.325
5577.3 Å	[O I]	0.219	0.142
5679.6 Å	N II	0.017	0.018
5754.6 Å	[N II]	2.578	2.946
5875.6 Å	He I	14.666	15.010
6300.3 Å	[O I]	16.129	7.661
6312.1 Å	[S III]	1.031	1.850
6363.8 Å	[O I]	5.095	2.443
6548.0 Å	[N II]	40.956	44.231
6583.5 Å	[N II]	121.454	130.527
6678.2 Å	He I	3.972	3.982

Table 18 (Continued)

(Continued)				
$\lambda_{ m lab.}$	Ion	$I(\text{obs}) $ $(I(\text{H}\beta) = 100)$	$I(\text{model})$ $(I(\text{H}\beta) = 100)$	
6730.8 Å	[S II]	12.471	7.635	
7065.2 Å	Не І	7.846	7.238	
7135.8 Å	[Ar III]	10.767	19.209	
7281.4 Å	Не І	0.726	0.880	
7319/20 Å	[O II]	17.485	17.826	
7329/30 Å	[O II]	14.463	14.279	
7751.1 Å	[Ar III]	2.630	4.635	
8333.8 Å	H I (P24)	0.152	0.158	
8345.6 Å	H I (P23)	0.188	0.175	
8359.0 Å	H I (P22)	0.220	0.195	
8361.7 Å	He I	0.082	0.098	
8374.5 Å	H I (P21)	0.219	0.219	
8392.4 Å	H I (P20)	0.252	0.248	
8413.3 Å	H I (P19)	0.288	0.284	
8434.0 Å	[Cl III]	0.008	0.013	
8438.0 Å 8467.3 Å	H I (P18)	0.326 0.378	0.328 0.383	
8500.2 Å	H I (P17) [Cl III]	0.378	0.383	
8502.5 Å	H I (P16)	0.450	0.454	
8545.4 Å	H I (P16)	0.430	0.545	
8578.7 Å	[Cl II]	0.304	0.200	
8598.4 Å	H I (P14)	0.636	0.665	
8617.0 Å	[Fe II]	0.042	0.031	
8665.0 Å	H I (P13)	0.829	0.827	
8727.1 Å	[C I]	0.014	0.019	
8750.5 Å	H I (P12)	1.042	1.049	
8891.9 Å	[Fe II]	0.016	0.010	
9014.9 Å	H I (P10)	1.624	1.815	
9052.0 Å	[Fe II]	0.011	0.007	
9068.6 Å	[S III]	12.577	27.975	
9123.6 Å	[Cl II]	0.103	0.052	
$5.92~\mu\mathrm{m}$	Н і	0.740	0.464	
$6.99~\mu\mathrm{m}$	[Ar II]	7.435	1.015	
9.01 μm	[Ar III]	12.993	17.582	
$10.51~\mu\mathrm{m}$	[S IV]	7.758	3.728	
$11.31 \mu \mathrm{m}$	Н І	0.277	0.308	
$12.37~\mu\mathrm{m}$	Н І	1.043	0.971	
$12.81~\mu\mathrm{m}$	[Ne II]	46.711	85.274	
$15.56~\mu\mathrm{m}$	[Ne III]	96.699	54.536	
$18.71~\mu\mathrm{m}$	[S III]	13.864	20.088	
$33.48~\mu\mathrm{m}$	[S III]	3.517	4.012	
$36.02~\mu\mathrm{m}$	[Ne III]	6.180	3.746	
$\lambda_c(\Delta \lambda)$	Band	I(obs)	I(model)	
$\Lambda_c(\Delta \lambda)$	Danu	$(I(H\beta) = 100)$	$(I(H\beta) = 100)$	
3.56(0.68) μm	IRAC-1	17.926	14.099	
4.51(0.86) μm	IRAC-2	20.919	13.128	
5.74(1.26) μm	IRAC-3	12.618	10.021	
7.93(2.53) µm	IRAC-4	48.754	45.385	
9.22(4.10) μm	IRC-S9W	130.819	152.073	
19.81(9.97) μm	IRC-L18W	1990.469	2062.191	
$65.0(20.17) \mu \text{m}$	FIS-N60	327.889	327.959	
90.0(39.90) μm	FIS-WS	283.292	219.030	
140.0(54.74) μm	FIS-WL	32.158	25.831	
$\lambda_c(\Delta \lambda)$	Band	I(obs)	I(model)	
		$(I(H\beta)=100)$	$(I(H\beta) = 100)$	
8.20(0.30) μm	IRS-1	1.613	2.279	
9.55(0.10) μm	IRS-2	3.008	4.012	
	IRS-3	21.065	29.324	
$10.95(0.50) \mu \text{m}$	113-3	21.003	27.324	
$10.95(0.50) \mu m$ $14.95(0.50) \mu m$	IRS-4	29.190	41.669	

Table 18 (Continued)

$\lambda_{\mathrm{lab.}}$	Ion	$I(\text{obs}) $ $(I(\text{H}\beta) = 100)$	$I(\text{model})$ $(I(H\beta) = 100)$
18.10(0.60) μm	IRS-6	128.928	132.281
$22.50(1.00) \mu m$	IRS-7	215.444	217.328
29.50(1.00) μm	IRS-8	127.541	150.879
λ_c		$F_{\nu}({ m obs})$	$F_{\nu}(\text{model})$
		(Jy)	(Jy)
9.60 μm		0.097	0.110
17.60 μ m		2.209	1.898
$25.00 \ \mu \text{m}$		3.718	3.746
$27.00 \mu m$		3.695	3.943
29.00 μ m		3.790	4.060

Note. $\Delta\lambda$ indicates the bandwidth of each band. The predicted F_{ν} at IRAC-1/2/3/4 bands is 8.56, 1.01(+1), 8.62, and 3.70(+1) mJy, respectively. The F_{ν} at IRC-S9W/L18W bands is 1.03(+2) and 2.66(+3) mJy, respectively. The F_{ν} at FIS-N90/WS/WL is 2.25(+3), 1.46(+3), and 3.03(+2) mJy, respectively.

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