# NEAR-SIMULTANEOUS SPECTROSCOPIC AND BROADBAND POLARIMETRIC OBSERVATIONS OF Be STARS 

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#### Abstract

Near simultaneous optical spectroscopic (on four nights) and broadband linear continuum ( $B, V, R$, and $I$ bands) polarimetric (on seven nights) observations of 29 Be stars were carried out during 1993 November-December. The program Be stars displayed wavelength dependence of intrinsic polarizations with no frequency dependence of polarimetric position angles. Some of the Be stars displayed long-term polarization variability. The Be and Be-shell stars could not be distinguished from one another solely on the basis of their polarization values. Full widths at half-maximum of the $\mathrm{H} \alpha$ profiles and the intrinsic linear continuum polarizations are closely correlated with the projected rotational velocities of the program stars. Photospheric-absorption-corrected equivalent widths of $\mathrm{H} \alpha$ profiles $[W(\alpha)]$ and the radii of $\mathrm{H} \alpha$-emitting or -absorbing envelopes ( $R_{e}$ or $R_{a}$ ) are nonlinearly correlated with the intrinsic continuum polarizations of these stars. However, $W(\alpha)$ and $R_{e}$ are linearly correlated. With large uncertainties, there is a trend of spectral dependence of polarization. Detailed discussion of these results is presented in this paper.


Key words: stars: emission-line, $\mathrm{Be}-$ techniques: polarimetric - techniques: spectroscopic

## 1. INTRODUCTION

Rapidly rotating B-type stars of luminosity classes III-V with Balmer emission lines are known as Be stars. Excess IR emission (Wright \& Barlow 1975), optical and near-infrared emission-line profiles (details can be seen in Underhill \& Dozan 1982), and ultraviolet wind lines (Snow 1981; Sonneborn et al. 1988; Grady et al. 1989, and references therein) have all been detected in Be stars. These results suggest the existence of extended circumstellar envelopes around these stars. Intrinsic linear polarization has been detected in Be stars. The measurements of linear polarizations of Be stars were started by Coyne \& Gehrels (1967) and Coyne \& Kruszewski (1969). It has been suggested that the linear polarizations of Be stars may be due to electron scattering in the inner regions of the equatorially flattened circumstellar envelopes (Coyne \& Kruszewski 1969; Capps, Coyne, \& Dyck 1973; Coyne 1976a, 1976b; McLean \& Clarke 1976; Poeckert \& Marlborough 1976; Wood, Bjorkman, \& Bjorkman 1997, and references therein). Also, it has been reported that the polarizations in Be stars are variable on short to long timescales with constant polarimetric position angle, suggesting an axisymmetric geometry of the envelopes (Shakhovskoi 1965; McLean 1979; McLean \& Clarke 1979; Hayes 1980; Bjorkman 1994). In general, it has been found that the maximum polarization exhibited by the Be stars is around 2\% (Coyne \& Gehrels 1967; Poeckert \& Marlborough 1976; McLean \& Brown 1978; Poeckert, Bastien, \& Landstreet 1979; McDavid 1986, 1990, 1994, 1995; McDavid et al. 1996), an exception being $\gamma$ Cas, which has displayed polarization as high as $2.5 \%$ (Coyne 1976a,

[^0]1976b; Poeckert \& Marlborough 1977). These polarizations are frequency-dependent and are correlated with the rotational velocities of the Be stars. To explain this $\sim 2 \%$ polarization limit, different models were constructed by varying the geometry of the envelopes of Be stars from a spherically symmetric "onion-like" geometry (Doazan \& Thomas 1982) to an ellipsoidal geometry (Doazan 1987). However, VLA observations of $\psi$ Per give direct evidence for flat envelopes of Be stars (Dougherty \& Taylor 1992). Subsequent interferometric results also support the view that the equatorial envelopes of Be stars are flat (Quirrenbach et al. 1994a, 1994b, 1997). It has been found in many Be stars that the linear polarization of the star increases during the onset of its shell phase (McLean \& Brown 1978; Arsenijevic, Jankov, \& Djurasevic 1987). Probably during the Be-shell phase, the density of scatterers in the envelope increases, which in turn may increase the polarization of the shell stars. However, statistically it is not clear whether or not the Be-shell stars display higher polarizations than the Be stars.

Significant improvements in polarimetric modeling techniques of Be stars have been made in order to understand the geometry of Be star disks. Based on Monte Carlo modeling of optical continuum spectropolarimetry of Be stars, Wood et al. (1997) obtained two solutions, a geometrically thin and a geometrically thick disk. They have shown that the thin-disk solution is consistent with either a Keplerian or a wind-compressed disk (Bjorkman \& Cassinelli 1993). Also, their thin-disk model can reproduce the multifrequency (far-infrared through ultraviolet) continuumenergy distribution of Be stars. These results provide convincing evidence that the circumstellar disks of Be stars are geometrically thin (Wood et al. 1997). In addition, recent optical interferometric images and spectropolarimetric results of Be stars clearly exclude the geometrically thick-disk option for these stars and lead strongly to the conclusion that the envelope of Be stars are geometrically thin (Quirrenbach et al. 1997). Although now we have a better understanding of the geometry of the disk of Be
stars, it is still important to learn about the physical conditions (velocity, density, and temperature profile) in the disk. Such information may be obtained through simultaneous spectroscopic and polarimetric observations that will enable us to simultaneously probe the different physical regions and parameters of the disks of Be stars.

To find out the polarimetric properties of Be and Be-shell stars and also to search for a possible correlation between the linear polarization and the equivalent width of the $\mathrm{H} \alpha$ emission line, near-simultaneous spectroscopic and broadband polarimetric observations of 29 Be stars were carried out. Results of these observations are presented in this paper. Section 2 describes the observations. Data analysis, results, and discussion are presented in $\S 3$. Section 4 describes the conclusions.

## 2. OBSERVATIONS

The spectra of the program Be stars were obtained on four nights during 1993 November-December, using the Universal Astronomical Grating Spectrograph (UAGS) at the Cassegrain focus of the 1 m reflector of Vainu Bappu Observatory, Kavalur, India, and a few spectra were also obtained using the echelle spectrograph at the coude focus of the same telescope, with a 254 mm camera and a CCD system. Iron-argon or iron-neon and thorium-argon source spectra were used for wavelength calibration. Dome flatfield frames were obtained to remove the pixel-to-pixel quantum efficiency variations. The reciprocal dispersions of the UAGS and echelle spectrographs are $19.6 \AA \mathrm{~mm}^{-1}$ at $\mathrm{H} \alpha\left(0.45 \AA \mathrm{pixel}^{-1}\right)$ and $7.4 \AA \mathrm{~mm}^{-1}$ at $\mathrm{H} \alpha\left(0.14 \AA \mathrm{pixel}^{-1}\right)$, respectively.

Polarimetric observations were carried out on seven nights, during 1993 November-December, using the star and sky chopping polarimeter (developed at the Indian Institute of Astrophysics; Jain \& Srinivasalu 1991) attached at the $\mathrm{f} / 13$ Cassegrain focus of the 1 m reflector of VBO. A dry ice-cooled EMI 9658-R (extended S-20) photomultiplier tube coupled with the Fernie (1974) combination of glass filters [ $B(4400 \AA / 1050 \AA), V(5425 \AA / 1050 \AA), R(6550$ $\AA / 1300 \AA)$, and $I(8150 \AA / 1700 \AA)]$ was used for the observations. The star and the neighboring sky, separated by about $2^{\prime}$, were observed alternately every 20 ms . This was done at 200 orientations of the analyzer. Typical integration times for the program Be stars were in the range of 6-10 minutes. An aperture of $15^{\prime \prime}$ was used in all the observations. Polarimetric observations of each star were carried out on at least two nights, and each star was observed for at least 2-3 times on each night. Both polarized (Hsu \& Breger 1982) and unpolarized standard stars (Serkowski 1974) were observed on each night to measure the zero correction of the position angle and the instrumental polarization, respectively.

## 3. DATA REDUCTIONS AND RESULTS

### 3.1. Spectroscopic Data, Reductions, and Results

Standard IRAF reduction packages and standard reduction techniques for CCD data were used to analyze the spectra. The error in wavelength calibration was around $0.05-0.10 \AA$. Each spectrum was normalized in three to four different ways, using different continuum-fitting functions (second or third order of SPLINE or LEGENDRE functions). Then these three or four spectra were averaged to obtain the final normalized spectrum. This helped to
reduce the error in normalizations. Error in normalization is estimated to be around $2 \%$ of the local continuum. The instrumental broadening was measured by measuring the FWHM of the narrowest line of the comparison spectral lines, and this value of the FWHM was taken as the instrumental broadening of the spectrograph. The values of instrumental broadening for the UAGS and the echelle spectrographs are 0.5 and $0.2 \AA$, respectively, at $\mathrm{H} \alpha$. These values were used to correct for instrumental broadening of the measured FWHM values of Be stars. The errors in equivalent width measurements were computed using the expression of $\sigma(\mathrm{EW})$ given in Ghosh (1988). All the spectra were obtained, within at most 3 to 4 days of the polarimetric observations.

Table 1 shows the HD and the HR numbers and the designated name, the spectral type with reference, the visual magnitude, and the rotational velocity with reference, for each of the program Be stars. It can be seen from this table that the spectral types of these stars have been classified into three groups: $\mathrm{B}, \mathrm{Be}$, and Be -shell. This classification has been done using the $\mathrm{H} \alpha$ profiles of these stars, as discussed below. The spectra of 29 program Be stars, in the $\mathrm{H} \alpha$ region, are displayed in Figure 1. Close examination of $\mathrm{H} \alpha$ profiles of these Be stars reveals the following results:

1. No core-emission component is present in the $\mathrm{H} \alpha$ profile of four Be stars (HD 44506, HD 56014, HD 217675, and HD 224544) after subtracting the photospheric $\mathrm{H} \alpha$ absorption profile (the details of subtraction of photospheric absorption profile will be discussed below) from the observed $\mathrm{H} \alpha$ profiles. The residual $\mathrm{H} \alpha$ profile (observed $\mathrm{H} \alpha$ profiles minus the photospheric $\mathrm{H} \alpha$ absorption profiles) of HD 217675 shows the presence of deep and narrow absorption component and this star has been classified as a Beshell star. The residual H $\alpha$ profiles of HD 44506, HD 56014 and HD 224544 display weak core absorption and, most probably, very weak emission at the wings. We have classified these three stars as weak Be-shell stars.
2. $\mathrm{H} \alpha$ profiles of six Be stars (HD 21641, HD 25940, HD 30076, HD 32991, HD 41335, and HD 217891) are singlepeaked and the $\mathrm{H} \alpha$ profiles of the remaining 19 Be stars are double-peaked. Among these 19 Be stars, only five Be stars (HD 22192, HD 22780, HD 23016, HD 43544, and HD 45542) have displayed narrow absorption line at the center of $\mathrm{H} \alpha$ profile. The sharp absorption line at the center of $\mathrm{H} \alpha$ profile of HD 45542 is due to the telluric line. The values of full width at half-maximum (FWHM) of the absorption lines at the center of $\mathrm{H} \alpha$ profiles of HD 22780, HD 23016, and HD 43544 are in the range of 170 to $200 \mathrm{~km} \mathrm{~s}^{-1}$, which is much broader than the range of absorption-line FWHM values of Be-shell stars ( $50-75 \mathrm{~km} \mathrm{~s}^{-1}$; Srinivasan 1998). Also from the residual $\mathrm{H} \alpha$ profiles (observed $\mathrm{H} \alpha$ profile minus the photospheric $\mathrm{H} \alpha$ absorption profile) we find that the absorption lines at the center of $\mathrm{H} \alpha$ profiles of these three stars are not very deep. Based on these results we suggest that the narrow central reversal feature at the emission peak of $\mathrm{H} \alpha$ profiles of HD 22780, HD 23016, and HD 43544 are not due to the shell absorption and these stars are not Be-shell stars. However, a narrow ( $\sim 70 \mathrm{~km} \mathrm{~s}^{-1}$ ) and relatively deep absorption line is present at the emission peak of $\mathrm{H} \alpha$ profile of HD 22192, and we classify this star as a Be-shell star. Finally we find that there are 24 Be stars, two Be-shell stars, and three weak Be-shell stars are present in our sample (Table 1).

TABLE 1
Program Be Stars for Spectroscopic and Polarimetric Observations

| HD | HR | Name | Spectral Type | Spectral Type Reference | $V \mathrm{mag}^{\text {a }}$ | $\begin{gathered} v \sin i \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $v \sin i$ <br> Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 144......... | 7 | 10 Cas | B9 IIIe | 1 | 5.58 | 170 | 2 |
| $5394 \ldots \ldots$. | 264 | $\gamma \mathrm{Cas}$ | B0 IVe | 3 | 2.39 | 230 | 4 |
| $10516 \ldots .$. | 496 | $\phi$ Per | B2 Vpe | 5 | 4.07 | 493 | 2 |
| $18552 \ldots .$. | 894 |  | B8 Vne | 6 | 6.11 | 320 | 2 |
| 21641 ....... |  |  | B8.5 Ve | 4 | 6.75 | 184 | 2 |
| $22192 \ldots .$. | 1087 | $\psi$ Per | B5 Ve-shell | 5 | 4.23 | 390 | 2 |
| 22780....... | 1113 |  | B7 Vne | 5 | 5.55 | 360 | 2 |
| 23016...... | 1126 | 13 Tau | B9 Vne | 1 | 5.69 | 260 | 4 |
| 25940 ....... | 1273 | 48 Per | B3 Ve | 5 | 4.04 | 233 | 2 |
| $28497 \ldots .$. | 1423 |  | B2 Vne | 7 | 5.60 | 340 | 2 |
| $30076 \ldots .$. | 1508 | 56 Eri | B2 Ve | 5 | 5.90 | 240 | 2 |
| 32991 ....... | 1660 | 105 Tau | B2 Ve | 5 | 5.92 | 220 | 2 |
| 35439 ....... | 1789 | 25 Ori | B1 Vpe | 3 | 4.94 | 327 | 2 |
| 37202 ....... | 1910 | $\zeta \mathrm{Tau}$ | B4 IIIpe | 5 | 3.03 | 310 | 2 |
| 37795 ....... | 1956 | $\alpha \mathrm{Col}$ | B7 IVne | 7 | 2.60 | 180 | 4 |
| 41335 ....... | 2142 |  | B2 Vne | 5 | 5.21 | 414 | 2 |
| 42054 ....... | 2170 |  | B4 Vnne | 8 | 5.83 | 220 | 4 |
| 43285 ....... | 2231 |  | B6 Ve | 5 | 6.07 | 290 | 2 |
| $43544 \ldots .$. | 2249 |  | B2.5 Vne | 5 | 5.92 | 300 | 4 |
| $44506 \ldots .$. | 2288 |  | B3 Ve-shell | 7 | 5.53 | 211 | 2 |
| $45542 \ldots .$. | 2343 | $v$ Gem | B6 IIIe | 5 | 4.14 | 220 | 2 |
| $47054 \ldots .$. | 2418 |  | B8 Ve | 6 | 5.57 | 270 | 2 |
| 48917 ....... | 2492 | 10 Cma | B2 Ve | 7 | 5.20 | 200 | 4 |
| $56014 \ldots .$. | 2745 | 27 Cma | B3 IIIe-shell ${ }^{\text {b }}$ | 8 | 4.65 | 200 | 2 |
| 58715...... | 2845 | $\beta \mathrm{Cmi}$ | B8 Ve | 9 | 2.90 | 265 | 2 |
| $83953 \ldots . .$. | 3858 |  | B5 Ve | 7 | 4.77 | 330 | 2 |
| 217675..... | 8762 | $o$ And | B6 IIIpe-shell | 10 | 3.62 | 333 | 2 |
| 217891..... | 8773 | $\beta$ Psc | B6 Ve | 5 | 4.53 | 160 | 2 |
| 224544...... | 9068 |  | B6 IVe-shell ${ }^{\text {b }}$ | 5 | 6.52 | 260 | (4) |

${ }^{\text {a }}$ From Hoffleit \& Jaschek 1982.
${ }^{\mathrm{b}}$ Weak shell stars.
References.-(1) Cowley 1972; (2) Bernacca \& Perinotto 1970; (3) Morgan, Code, \& Whitford 1955; (4) Hoffleit \& Jaschek 1982; (5) Lesh 1968; (6) Cowley et al. 1969; (7) Houk \& Smith-Moore 1988; (8) Houk 1982; (9) Slettebak 1954; (10) Racine 1968.

To measure the true $\mathrm{H} \alpha$ emission strength of the program Be stars, it is important to correct the observed $\mathrm{H} \alpha$ profiles for the underlying photospheric absorption and for the central reversal at the emission peak. Corrections for the effects of photospheric absorption. were carried out in two ways: (1) theoretically and (2) observationally. Theoretically, we have computed the photospheric $\mathrm{H} \alpha$ profiles of B stars. To carry out such computations we need the values of the effective temperatures, masses, radii, bolometric magnitudes, and luminosities of main-sequence stars in the spectral range $\mathrm{B} 0-\mathrm{B} 9$. These values were collected from the literature, mainly from Popper (1980) and Harmanec (1988). The adopted parameters for the main-sequence B stars that we have collected are very similar to the adopted values of Slettebak, Collins, \& Truax (1992). Using these parameters and also using the Kurucz (1994) model atmosphere code, we computed the theoretical photospheric $\mathrm{H} \alpha$ profiles of B stars of different spectral types, luminosities, and $v \sin i$ values. These theoretical $\mathrm{H} \alpha$ profiles of B stars may be used for underlying photospheric absorption corrections for the program Be stars.

Photospheric absorption can also be corrected by using observed $\mathrm{H} \alpha$ profiles of B stars. For this purpose, we observed 17 non-emission-line B stars of different spectral types and luminosity classes, using the same instrumentation that was used for the program stars. These spectra
were rotationally broadened to correspond to the $v \sin i$ values of 29 Be stars. Rotationally broadened $\mathrm{H} \alpha$ profiles may also be used to correct for photospheric absorptions. Equivalent widths of theoretically computed and rotationally broadened observed $\mathrm{H} \alpha$ profiles of B stars were compared, and it was found that the differences in equivalent widths were in the range $0.3-0.6 \AA$. These results suggest that either theoretical or rotationally broadened observed $\mathrm{H} \alpha$ profiles can be used for photospheric absorption corrections. These photospheric $\mathrm{H} \alpha$ absorption profiles were subtracted from the observed $\mathrm{H} \alpha$ profiles of 29 Be stars. An example of such a correction is shown in Figure 2. The theoretical, photospheric $\mathrm{H} \alpha$ absorption profile is shown in Figure 2 (bottom) and is marked "Theoretical profile" (smooth line). The inner thin line is the observed profile. The theoretical profile has been subtracted from the observed profile, and the "subtracted profile" is shown as the thick line on top of the observed profile.
It has been found from Figure 1 that there are 19 Be stars with central reversal in the emission peak of the $\mathrm{H} \alpha$ profile (double-peak $\mathrm{H} \alpha$ profile). Correction for the central reversal in 19 Be stars has been done through extrapolation (Slettebak et al. 1992). The extrapolated profile is shown with a dashed line in Figure 2. Such correction for the central reversal is not required for the single-peak $\mathrm{H} \alpha$ profile. Corrected $\mathrm{H} \alpha$ profiles were used to measure the


Fig. 1a


Fig. 1c


Fig. 1b


Fig. 1d


Fig. $1 e$
Fig. 1.-Normalized $\mathrm{H} \alpha$ profiles of 29 Be stars that were observed nearly with polarimetric observations. ( $a$ and $b$ ) Coudé echelle spectra of 13 Be stars. $(c-e)$ Cassegrain spectra of the remaining 16 Be stars.


Fig. 2.-Examples of photospheric correction and artificial extrapolation of $\mathrm{H} \alpha$ profile of HD 18522. The smooth line is the theoretical profile. The inner thin line is the observed profile. The subtracted profile (the observed profile minus the theoretical profile) is shown as the thick line. The extrapolated profile (corrected for the central reversal) is shown as the dashed line.

FWHM and equivalent width values that are given in Table 2. Peak-separation ( $D V_{\text {peak }}$ ) values were measured using the observed $\mathrm{H} \alpha$ profiles. These values of FWHM and $D V_{\text {peak }}$ have been used to compute the radii of $\mathrm{H} \alpha$-absorbing $\left(R_{a}\right)$
and $\mathrm{H} \alpha$-emitting envelopes $\left(R_{e}\right)$, respectively, of the program Be stars. The radii of the envelopes of Be stars were computed using the following expressions (Huang 1972):
$R_{e}=\left(\frac{2 v \sin i}{\Delta V_{\text {peak }}}\right)^{1 / j} R_{*} \quad$ for emission-line stars,
$R_{a}=\left(\frac{2 v \sin i}{\mathrm{FWHM}}\right)^{1 /(j+1)} R_{*}$ for absorption-line stars,
where $v$ is the equatorial stellar rotational velocity, $v \sin i$ is the projected rotational velocity of the star, $\Delta V_{\text {peak }}$ is the peak separation between the violet and red emission components of the $\mathrm{H} \alpha$ emission line, FWHM is the full width at half-maximum of the $\mathrm{H} \alpha$ shell-absorption component, $j$ is an exponent that characterizes the rotation law ( $j=0.5$ for Keplerian rotation of the disk and $j=1.0$ for rotation with conservation of angular momentum), and $R_{*}$ is the stellar radius. Computed values of $R_{e}$ and $R_{a}$ (in units $R_{\odot}$ ) are given in Table 2 with probable errors.

### 3.2. Polarimetric Data, Reductions, and Results

The degrees of polarization and polarimetric position angle and their errors were measured by least-squares fitting to the intensity versus the angle data, after the sky background correction. The instrumental polarization was determined by repeated observations of several unpolarized

TABLE 2
Measured Values of $\mathrm{H} \alpha$ Profiles of 29 Be Stars

| HD | $\begin{aligned} & \text { FWHM } \\ & \left(\mathrm{km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{gathered} \Delta V_{\text {peak }} \\ \left(\mathrm{km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\operatorname{EW}(\mathrm{H} \alpha)^{\mathbf{a}}$ <br> (A) | $\begin{gathered} R_{e} \text { or } R_{a} \\ \left(R_{\odot}\right) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| 144 | $218 \pm 06$ | $168 \pm 07$ | $02.07 \pm 0.07$ | $03.7 \pm 0.3$ |
| 5394 | $492 \pm 09$ | $146 \pm 07$ | $38.46 \pm 1.88$ | $33.1 \pm 1.5$ |
| 10516 | $520 \pm 10$ | $207 \pm 09$ | $45.17 \pm 2.32$ | $36.5 \pm 2.5$ |
| 18552 | $340 \pm 08$ | $157 \pm 07$ | $21.23 \pm 1.45$ | $15.6 \pm 0.6$ |
| 21641 | $238 \pm 11$ |  | $11.82 \pm 0.38$ |  |
| $22192{ }^{\text {b }}$ | $376 \pm 13$ | $138 \pm 08$ | $35.61 \pm 1.10$ | $29.8 \pm 1.4$ |
| 22780 | $367 \pm 11$ | $200 \pm 09$ | $11.44 \pm 0.45$ | $16.2 \pm 0.7$ |
| 23016 | $342 \pm 10$ | $259 \pm 10$ | $05.74 \pm 0.34$ | $09.8 \pm 0.6$ |
| 25940 | $249 \pm 11$ | $\ldots$ | $24.15 \pm 0.96$ | $\ldots$ |
| 28497 | $299 \pm 13$ | $214 \pm 09$ | $07.97 \pm 0.63$ | $16.6 \pm 0.9$ |
| 30076 | $335 \pm 12$ |  | $24.85 \pm 1.56$ |  |
| 32991 | $294 \pm 12$ |  | $39.91 \pm 1.72$ |  |
| 35439 | $488 \pm 14$ | $312 \pm 08$ | $05.69 \pm 0.43$ | $15.7 \pm 0.7$ |
| 37202 | $455 \pm 16$ | $154 \pm 10$ | $24.98 \pm 1.20$ | $29.0 \pm 1.6$ |
| 37795 | $242 \pm 10$ | $117 \pm 06$ | $09.62 \pm 0.88$ | $13.7 \pm 0.6$ |
| 41335 | $480 \pm 14$ | $230 \pm 10$ | $37.43 \pm 1.55$ | $30.3 \pm 2.5$ |
| 42054 | $298 \pm 09$ | $137 \pm 08$ | $12.75 \pm 0.69$ | $19.0 \pm 1.5$ |
| 43285 | $415 \pm 13$ | $271 \pm 08$ | $03.21 \pm 0.28$ | $08.0 \pm 0.5$ |
| 43544 | $490 \pm 14$ | $344 \pm 10$ | $06.23 \pm 0.45$ | $09.7 \pm 0.4$ |
| $44506{ }^{\text {c }}$ | $334 \pm 11$ |  | $-01.65 \pm 0.04$ | $07.3 \pm 0.3^{\text {d }}$ |
| 45542 | $309 \pm 09$ | $134 \pm 05$ | $07.94 \pm 0.73$ | $12.6 \pm 0.7$ |
| 47054 | $276 \pm 08$ | $115 \pm 05$ | $11.32 \pm 0.80$ | $15.9 \pm 1.4$ |
| 48917. | $314 \pm 10$ | $121 \pm 06$ | $25.61 \pm 0.94$ | $26.0 \pm 1.7$ |
| $56014{ }^{\text {c }}$ | $443 \pm 12$ |  | $-01.13 \pm 0.06$ | $03.7 \pm 0.4^{\text {d }}$ |
| 58715 | $299 \pm 11$ | $145 \pm 05$ | $07.64 \pm 0.67$ | $12.0 \pm 0.6$ |
| 83953 | $399 \pm 12$ | $167 \pm 07$ | $11.41 \pm 0.83$ | $15.8 \pm 0.8$ |
| $217675^{\text {b }}$ | $251 \pm 08$ |  | $-02.48 \pm 0.04$ | $05.3 \pm 0.3^{\text {d }}$ |
| 217891. | $202 \pm 08$ |  | $21.45 \pm 1.56$ |  |
| $224544^{\text {c }}$. | $498 \pm 14$ |  | $-02.07 \pm 0.03$ | $03.6 \pm 0.3^{\text {d }}$ |

[^1]standard stars on each night. The value of the mean instrumental polarization was found to be $0.10 \%$, and this value was almost constant during the interval of our observations (on seven nights during 1993 November-December). The instrumental polarization ( $\sim 0.1 \%$ ) was vectorially subtracted from the measured polarization of the program stars. The intrinsic polarization and polarimetric position angle were computed after removal of the interstellar polarization. The values of interstellar polarization in different filters were obtained from McLean \& Clarke (1979) and Pockert et al. (1979). The interstellar polarization component was removed through a Serkowski-law fit and then vectorially subtracted using values in each filter. Values of probable errors associated with intrinsic polarization and position angle of the program stars were computed in two ways: (1) according to photon statistics and (2) based on multiple measurements. Usually it has been found that the computed values of probable errors based on multiple measurements are larger than that obtained from photon statistics, and these values of probable errors (based on multiple measurements) are listed in Table 2.

The measured average intrinsic polarizations (polarization measurements of each star were carried out on at least two nights and each star was observed for at least 2-3 times on each night) of the program stars in the $B, V, R$, and $I$ bands with the probable errors are presented in Table 3. It may be seen from this table that six Be stars, including a Be-shell star (HD 22192), displayed polarizations (in the $B$
band) between $0.94 \%$ and $1.57 \%$. The percent of polarization of 19 program stars was around $0.5 \%$, and the remaining four Be stars, including two weak Be-shell stars (HD 56014 and HD 224544), were in low polarization states ( $\sim 0.25 \%$ ). From these results (Table 3) we do not find any distinction in polarization level between Be and Be -shell stars. Polarization variability is quite common in Be stars (Bjorkman 1994; McDavid 1994). However, during the interval of our observations of these 29 Be stars, we could not detect any short-term variations (night to night) in the polarization levels of these stars. To search for long-term polarimetric variations of these stars, we compared our results with the published data. Figure 3 shows show the plots of the $B-, V-, R$-, and $I$-band polarizations versus dates of observations for HD 5394, HD 10516, HD 25940, HD 37202, and HD 217675. Polarimetric data of these five Be stars, between 1984 December and 1993 January, have been obtained from the published data by McDavid (1986, 1990, 1994) and are compared with our results in Figure 3. It can be seen from these plots that HD 5394, HD 10516, HD 25940, and HD 37202 displayed large amplitude polarimetric variations between 1993 January and December. HD 5394 displayed an almost constant level of polarization ( $P^{B} \sim 0.75 \% \pm 0.08 \%$ ) between 1986 and 1992, but this level increased to $1.2 \% \pm 0.1 \%$ between 1992 and 1994 . Figure $3 b$ shows weak polarization variations of HD 10516 between 1985 and 1994. The polarization level of HD 25940 started declining in 1991, and this star exhibited almost

TABLE 3
Measured Intrinsic Polarizations of Program Be Stars

| HD | Polarization (\%) |  |  |  | P.A. <br> (deg) |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $B$ | $V$ | $R$ | I |  |
| 144. | $0.20 \pm 0.06$ | $0.16 \pm 0.05$ | $0.10 \pm 0.05$ | $0.12 \pm 0.05$ | $31 \pm 2$ |
| 5394 | $1.18 \pm 0.10$ | $0.89 \pm 0.07$ | $0.72 \pm 0.05$ | $0.58 \pm 0.05$ | $105 \pm 4$ |
| 10516 | $1.57 \pm 0.11$ | $1.36 \pm 0.10$ | $1.19 \pm 0.09$ | $0.98 \pm 0.08$ | $27 \pm 2$ |
| 18552 | $0.47 \pm 0.05$ | $0.38 \pm 0.05$ | $0.29 \pm 0.05$ | $0.17 \pm 0.05$ | $104 \pm 5$ |
| 21641 | $0.39 \pm 0.06$ | $0.26 \pm 0.05$ | $0.19 \pm 0.06$ | $0.12 \pm 0.06$ | $129 \pm 8$ |
| $22192^{\text {a }}$ | $0.94 \pm 0.06$ | $0.72 \pm 0.05$ | $0.54 \pm 0.04$ | $0.37 \pm 0.04$ | $43 \pm 3$ |
| 22780 | $0.57 \pm 0.05$ | $0.44 \pm 0.05$ | $0.30 \pm 0.04$ | $0.17 \pm 0.04$ | $106 \pm 9$ |
| 23016 | $0.45 \pm 0.04$ | $0.36 \pm 0.04$ | $0.25 \pm 0.04$ | $0.17 \pm 0.04$ | $169 \pm 9$ |
| 25940 | $0.69 \pm 0.06$ | $0.55 \pm 0.05$ | $0.44 \pm 0.05$ | $0.28 \pm 0.04$ | $140 \pm 4$ |
| 28497 | $0.61 \pm 0.06$ | $0.48 \pm 0.05$ | $0.32 \pm 0.04$ | $0.23 \pm 0.04$ | $114 \pm 8$ |
| 30076 | $0.64 \pm 0.07$ | $0.48 \pm 0.05$ | $0.32 \pm 0.05$ | $0.24 \pm 0.05$ | $115 \pm 7$ |
| 32991 | $1.38 \pm 0.09$ | $1.19 \pm 0.09$ | $1.06 \pm 0.08$ | $0.84 \pm 0.07$ | $68 \pm 4$ |
| 35439 | $0.51 \pm 0.08$ | $0.38 \pm 0.07$ | $0.26 \pm 0.05$ | $0.17 \pm 0.05$ | $108 \pm 6$ |
| 37202 | $1.03 \pm 0.09$ | $0.85 \pm 0.08$ | $0.73 \pm 0.09$ | $0.61 \pm 0.08$ | $35 \pm 4$ |
| 37795 | $0.34 \pm 0.06$ | $0.28 \pm 0.05$ | $0.21 \pm 0.05$ | $0.16 \pm 0.05$ | $77 \pm 4$ |
| 41335 | $1.02 \pm 0.11$ | $0.86 \pm 0.11$ | $0.71 \pm 0.09$ | $0.54 \pm 0.08$ | $148 \pm 6$ |
| 42054 | $0.39 \pm 0.05$ | $0.28 \pm 0.05$ | $0.19 \pm 0.04$ | $0.11 \pm 0.04$ | $82 \pm 7$ |
| 43285 | $0.45 \pm 0.06$ | $0.36 \pm 0.07$ | $0.24 \pm 0.07$ | $0.16 \pm 0.06$ | $52 \pm 5$ |
| 43544 | $0.48 \pm 0.07$ | $0.37 \pm 0.06$ | $0.26 \pm 0.07$ | $0.18 \pm 0.05$ | $44 \pm 5$ |
| $44506{ }^{\text {b }}$ | $0.55 \pm 0.07$ | $0.39 \pm 0.05$ | $0.24 \pm 0.05$ | $0.13 \pm 0.05$ | $92 \pm 7$ |
| 45542 | $0.51 \pm 0.08$ | $0.40 \pm 0.06$ | $0.31 \pm 0.06$ | $0.19 \pm 0.05$ | $37 \pm 5$ |
| 47054 | $0.47 \pm 0.05$ | $0.34 \pm 0.05$ | $0.24 \pm 0.05$ | $0.17 \pm 0.05$ | $71 \pm 6$ |
| 48917 | $0.62 \pm 0.09$ | $0.51 \pm 0.09$ | $0.37 \pm 0.07$ | $0.24 \pm 0.06$ | $18 \pm 5$ |
| $56014^{\text {b }}$ | $0.21 \pm 0.06$ | $0.17 \pm 0.05$ | $0.11 \pm 0.05$ | $0.10 \pm 0.05$ | $82 \pm 6$ |
| 58715 | $0.36 \pm 0.07$ | $0.27 \pm 0.07$ | $0.18 \pm 0.07$ | $0.13 \pm 0.05$ | $90 \pm 6$ |
| 83953 | $0.54 \pm 0.07$ | $0.41 \pm 0.08$ | $0.30 \pm 0.07$ | $0.17 \pm 0.05$ | $95 \pm 5$ |
| $217675^{\text {a }}$ | $0.45 \pm 0.07$ | $0.38 \pm 0.07$ | $0.26 \pm 0.06$ | $0.19 \pm 0.06$ | $110 \pm 8$ |
| 217891. | $0.23 \pm 0.07$ | $0.17 \pm 0.06$ | $0.11 \pm 0.05$ | $0.09 \pm 0.05$ | $115 \pm 7$ |
| $224544^{\text {b }}$ | $0.25 \pm 0.07$ | $0.19 \pm 0.08$ | $0.12 \pm 0.07$ | $0.10 \pm 0.06$ | $90 \pm 6$ |

[^2]

Fig. 3.-Measured polarization vs. date of observations for (a) HD 5394, (b) HD 10516, (c) HD 25940, (d) HD 37202, and (e) HD 217675. The four panels in each figure, from the top, are for polarizations in the $B, V, R$, and $I$ filters. The $x$-axis represents the date of the observations in years, and the year labels are located at the beginning of the year. Data points with circles are from Table 3 of the present paper, and the remaining data points are from McDavid (1986, 1990, 1994).
constant polarization between 1985 and 1991; a similar pattern of variations has been found in HD 37202. HD 217675 (Be-shell star) did not vary during 1993 JanuaryDecember. However, the $B$-band polarization of this star decreased by $0.6 \%$ between 1978 and 1984 (Pockert et al. 1979; McDavid 1986) and by $0.25 \%$ between 1984 December and 1993 December. We also compared our results with that obtained by Pockert et al. (1979) and found that the $B$-band polarizations of HD 22192 and HD 28497 decreased by $0.1 \%$ and $0.74 \%$, respectively, and those of HD 30076, HD 32991, HD 41335, HD 45542, HD 58715, and HD 83953 increased by $0.44 \%, 0.65 \%, 0.62 \%, 0.31 \%$, $0.26 \%$, and $0.44 \%$, respectively. These results support the earlier suggestion that Be stars are polarization-variable (Bjorkman 1994; McDavid 1994, and references therein).

We also measured the polarimetric position angles of 29 Be stars, and, from these measurements, we did not find any appreciable variations at different bands or wavelengths. Average values of position angles are given in Table 3, along with the probable errors. The polarimetric position angle is set by the orientation of the disk, and, if the polarization is due to electron scattering modified by hydrogen opacity in the circumstellar disk of Be stars, then the polarimetric position angle will be independent of wavelength (Coyne \& Kruszewski 1969; McLean \& Clarke 1979; Hayes 1980; Bjorkman 1994; Wood et al. 1997, and references therein). Our result that shows the lack of wavelength dependence of the polarimetric position angle of 29 Be stars is thus consistent with the previously published results by different investigators.

Measured polarizations of 29 Be stars (Table 3) are plotted in Figure 4. This figures show the wavelength dependence of polarization in these stars. It may be seen from these figures that the wavelength dependence of polarization is almost similar for all the stars in the present sample. Similar results were also obtained by McDavid (1994) for a sample of eight Be stars. This can also be shown through the plot of normalized polarization $\left(P^{V} / P^{B}\right.$, where $P^{B}$ and $P^{V}$ are the polarizations at the $B$ and $V$ filters, respectively) against $P^{B}$ (Fig. 5). No correlation is evident from this figure between $P^{V} / P^{B}$ and $P^{B}$. This indicates that the values of $P^{V} / P^{B}$ (the normalized dependence of polarization) are almost similar for all of the 29 Be stars. Our present results, along with similar results reported previously by other investigators, indicate that the frequency dependence of polarization is probably almost similar for all the observed Be stars. If the polarizing mechanism of multiple electron scattering is wavelength-independent, the observed polarization wavelength dependence may be due to pre- and postscattering attenuation by opacity sources in the disk. In the optical band, these opacity sources are dominated by the continuum opacity due to hydrogen, so the optical continuum polarization will follow the hydrogen opacity curve (Wood \& Bjorkman 1995; Wood et al. 1996a, 1996b, 1997). The lack of wavelength dependence of polarimetric position angles and the observed polarization wavelength dependence are consistent with previously suggested models for axisymmetric envelopes of Be stars (McLean 1979; McLean \& Clarke 1979; Hayes 1980; Bjorkman 1994).

The Figure $6(t o p)$ shows the plot of $P^{B}$ versus $v \sin i$, and Figure 6 (bottom) shows the plot of normalized polarization versus $v \sin i$. From this figure, it can be seen that $P^{B}$ is correlated with $v \sin i$ (the solid line shows the best corre-
lation between $P^{B}$ and $v \sin i$ ), but the normalized polarization is not correlated with $v \sin i$. These results agree well with those obtained by Brown \& McLean (1977). They suggested that such relations between $P^{B}$ and $v \sin i$ can be explained with the assumption that the Be stars have axisymmetric single-scattering envelopes. However, it is most likely that the disks of Be stars are optically thick that may lead to multiple electron scattering in the envelopes of these stars (Waters \& Marlborough 1992; Bjorkman \& Bjorkman 1994; Hillier 1994; Wood et al. 1996a). We will state below that the linear polarization is not only correlated with $v \sin i$, but also correlated with the $\mathrm{H} \alpha$ emission strength of these stars.

### 3.3. Results and Discussion from Polarimetric and Spectroscopic Data

FWHM values of $\mathrm{H} \alpha$ profiles and $v \sin i$ values are plotted in Figure 7. It may be seen from this figure that these two parameters are correlated (the solid line shows the best correlation between FWHM and $v \sin i$, the correlation coefficient, is 0.793 ). Already we have seen that the $v \sin i$ is also correlated with the linear polarization $\left(P^{B}\right)$. These results again support the previously reported suggestion of a "flattened" disk-type structure of the Balmeremitting envelopes of Be stars (McLean 1979; Dougherty \& Taylor 1992; Quirrenbach et al. 1994a, 1994b, 1997).

Based on nonsimultaneous observations, McLean (1979) and Hirata \& Kogure (1984) suggested that there may be a correlation between $P^{B}$ and $W(\alpha)$, but the nature of the relation between these two parameters was unknown. It is important to mention here that Cotš \& Waters (1987) found an interesting correlation between the $12 \mu \mathrm{~m}$ IR color excess and $P^{B}$. The triangle-like shape of the distribution of these two parameters may be used as an indicator to roughly estimate the inclination angles of the disks of Be stars, even though these two parameters were not observed simultaneously. From near-simultaneous spectroscopic and broadband polarimetric observations, the equivalent widths of $\mathrm{H} \alpha$ profiles [photospheric absorption corrected, $W(\alpha)$ ] and polarizations at the $B, V, R$, and $I$ bands were measured. Figure 8 presents the plot of $W(\alpha)$ versus $P^{B}$. The best fit to the data is shown by the dashed line, and this fit indicates that a nonlinear correlation (from the $F$-test analysis, it has been found that the fit is significant at $99.9 \%$ level) is present between $P^{B}$ and $W(\alpha)$ $\left\{P^{B}=0.474-0.122 W(\alpha)+0.0008[W(\alpha)]^{2}\right\}$. We have also found a similar relation between $P^{B}$ and $R_{e}$. A plot of $R_{e}$ versus $P^{B}$ is shown in Figure 9. It may be noted from this figure that these two parameters are nonlinearly correlated ( $F$-test analysis shows that the correlation is at better than the $99.9 \%$ significance level) and is similar to that of $W(\alpha)$ and $P^{B}$. However, Figure 10 [plot of $W(\alpha)$ vs. $\left.R_{e}\right]$ shows that $W(\alpha)$ is linearly correlated with $R_{e}$. Quirrenbach et al. (1997) have also found, for seven Be stars, that the $\mathrm{H} \alpha-$ emitting disk size is linearly correlated with the $\mathrm{H} \alpha$ emission strength. Results obtained from the present sample, which contains a larger number of Be stars, support the view of Quirrenbach et al. (1997) that the larger the size of the $\mathrm{H} \alpha$-emitting disk, the stronger the $\mathrm{H} \alpha$ emission.

Figures 8 and 9 show the nonlinear correlation between $P^{B}$ and $W(\alpha)$ and between $P^{B}$ and $R_{e}$, respectively. Close examination of the left sides of these two figures suggest that the values of $P^{B}$ were almost constant (around $0.5 \%$ ) when the values of $W(\alpha)$ and $R_{e}$ ranged between $-2.0-12.0 \AA$ and


Fig. 4.-Intrinsic polarization as a function of wavelength for the program stars. The error bars represent the bandwidth in each filter for the wavelength scale and $1 \sigma$ uncertainties in polarization measurements
4.0-18 $R_{\odot}$, respectively. The right sides of these two figures show that the relations between $P^{B}$ and $W(\alpha)$ and $R_{e}$ were almost linear when the values of $P^{B}{ }_{\mathrm{i}} W(\alpha)$, and $R_{e}$ were in the ranges $0.5 \%-1.6 \%, 22.0-40.0 \AA$, and $26.0-36.0 \quad R_{\odot}$, respectively. Such relations may be explained using the emission-line wings of the $\mathrm{H} \alpha$ profiles of these stars. The full width at zero intensity (FWZI) is a measure of the extension of the emission-line wings. However, accurate measurement of FWZI requires high-resolution spectra of these stars. Also each spectra should cover at least $100-150 \AA$ around
$\mathrm{H} \alpha$. We have obtained high-resolution spectra of 13 Be stars (Figs. $1 a$ and $1 b$ ) that each covered only $75 \AA$ around $\mathrm{H} \alpha$. Spectra of the remaining 16 Be stars are low-resolution Cassegrain spectra (Figs. 1c-1e). Therefore, these spectra will not provide very accurate measurement of FWZI values (low-resolution spectra will introduce large uncertainties in measuring FWZI values). However, with all these uncertainties, we measured the FWZI values of $\mathrm{H} \alpha$ profiles of 29 Be stars. We find that the stars with $W(\alpha)$ values up to $12 \AA$ have FWZI values in the range $13 \pm 3$ to $22 \pm 4 \AA$


Fig. 4.-Continued
when the values of $P^{B}$ are around $0.5 \%$. Stars with $W(\alpha)$ values between 20 and $40 \AA$ have very extended $\mathrm{H} \alpha$ profiles wings and FWZI values in the range $33 \pm 4$ to $55 \pm 5 \AA$. All these stars with large $W(\alpha), R_{e}$, and FWZI values have displayed high-level polarizations (the values of $P^{B}$ were in the range $0.5 \%-1.6 \%$ ). Recently McDavid, Bjorkman, \& Baade (1999) have found an increase in polarization ( $P^{B}$ has increased from $0.23 \%$ to $0.56 \%$ ) of $o$ And (HD 217675) with the enhancement of emission-line wings of the $\mathrm{H} \alpha$ profiles, suggesting that the polarization is mainly due to electron scattering in the inner region of the envelope of the Be star. Our results also support this suggestion.

Values of $P^{B}$ versus the spectral types of Be stars are plotted in Figure 11. The two solid lines in this figure show that all the stars except two (HD 23016 and HD 56014) lie


Fig. 5.-Plot of intrinsic polarization in the $B$ band $[P(B)]$ vs. the normalized polarization $[P(V) / P(B)]$.
within the triangular region in the $P^{B}$ versus spectral type plane. The lower solid line suggest a weak correlation between these two parameters, and the upper line shows a strong dependence of $P^{B}$ on the spectral type. In general (from Fig. 11) there is a trend that the Be stars of early spectral types have relatively larger polarizations than the


Fig. 6.-Top: Projected rotational velocities $(v \sin i)$ of the program stars plotted against $P(B)$. The errors in $v \sin i$ are the $5 \%$ errors of the measured values of $v \sin i$. The $1 \sigma$ error bars are for $P^{B}$. The solid line shows the best-correlated fit between the two parameters. Bottom: $P(V) / P(B)$ vs. $v \sin i$.


Fig. 7.-FWHMs of $\mathrm{H} \alpha$ profiles are plotted with $v \sin i$, and the solid line represents the best linear fit to the data. The $1 \sigma$ and $5 \%$ error bars are for FWHM and $v \sin i$, respectively.
late-type ones. Usually the early spectral type Be stars will have more ionizing photon flux than the late-type Be stars. It is also known that the early-type Be stars (hotter Be stars) have higher electron densities in their envelopes than the late-type ones (cooler Be stars) (Slettebak et al. 1992). Since $W(\alpha)$ is proportional to $N_{e}^{2}$, it is expected that the early-type Be stars will usually produce larger $\mathrm{H} \alpha$ emissions than the late-type ones. If the polarization is due to multiple electron scattering with a frequency dependence due to absorption


Fig. 8.-Plot of equivalent widths of $\mathrm{H} \alpha$ profiles $[W(\alpha)]$ vs. $P(B)$ with $1 \sigma$ error bars. The best nonlinear fit to the data is shown by the dashed curve.


FIG. 9.-Computed radii of $\mathrm{H} \alpha$-emitting/absorbing envelopes $\left[R_{e}\left(R_{\odot}\right)\right.$ or $\left.R_{a}\left(R_{\odot}\right)\right]$ of the program Be stars are plotted against $P(B)$ with $1 \sigma$ error bars. The dashed curve shows the best nonlinear fit to the data.


Fig. 10.- $W(\alpha)$ vs. $R_{e}$ with $1 \sigma$ error bars. The best fit to the data is represented by the dashed line.


Fig. 11.- $P(B)$, with $1 \sigma$ error, as a function of spectral type for the program Be stars.
and emission by partially ionized hydrogen (Wood et al. 1996a, 1996b), then it is expected that the early-type Be stars will show larger polarizations. Figure 11 displays the same results. However, considering the uncertainties in spectral types for Be stars, the large errors in polarization measurements, and the small number of stars observed for the present study, it is suggested that this result (obtained from Fig. 11) is not statistically significant and should be used cautiously.

## 4. CONCLUSIONS

Based on the results obtained from near-simultaneous spectroscopic and polarimetric observations of 29 Be stars, the following conclusions may be drawn:

1. A wavelength dependence of the polarization but no frequency dependence of the polarimetric position angle was found for the 29 Be stars. The lack of correlation between $P^{B}$ and the normalized polarization $\left(P^{V} / P^{B}\right)$ suggests that the nature of the wavelength dependence of polarization is similar for all the Be stars. These results are consistent with previously reported results and suggest models with electron-scattering disks with attenuative hydrogen opacities, combined with dilution due to the visible central stars (Wood \& Bjorkman 1995; Wood et al. 1996a, 1996b, 1997).
2. From the comparison of our results with the previously published data, it was found that many Be stars show long-term polarimetric variability, and this is consistent with the earlier reported results (Bjorkman 1994; McDavid 1994).
3. FWHMs of $\mathrm{H} \alpha$ profiles and intrinsic continuum polarizations are both closely correlated with the projected rotational velocities, $v \sin i$, of the program stars. However, no correlation is present between the normalized polarization $\left(P^{V} / P^{B}\right)$ and the $v \sin i$ values. These results are consistent with previously suggested models for axisymmetric envelope of Be stars.
4. There are 24 Be stars and five Be-shell stars (three shell stars and two weak-shell stars) in the present sample. Measured polarization values of these stars (Table 3) do not display any distinction in polarization level between Be and Be-shell stars.
5. Photospheric-absorption-corrected equivalent widths of $\mathrm{H} \alpha$ profiles $[W(\alpha)]$ and radii of $\mathrm{H} \alpha$-emitting envelopes are nonlinearly correlated with $P^{B}$. However, $W(\alpha)$ and $P^{B}$ are linearly correlated. These results are consistent with the suggestion that the polarization is mainly due to electron scattering in the inner region of the envelopes of Be stars (McDavid et al. 1999).

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[^1]:    ${ }^{\text {a }}$ Corrected for photospheric and shell absorption.
    ${ }^{\mathrm{b}}$ Shell stars.
    c Weak shell stars.
    ${ }^{\mathrm{d}}$ Radius of $\mathrm{H} \alpha$-absorbing envelope.

[^2]:    ${ }^{\text {a }}$ Shell stars.
    ${ }^{\text {b }}$ Weak shell stars.

